# Introduction to Object-Oriented Programming Recursion

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## Recursion

- A recursive processes or data structure is defined in terms of itself
- A properly written recursive function must
  - handle the base case, and
  - convergence to the base case.
- Failure to properly handle the base case or converge to the base case (divergence) may result in infinite recursion.

## The Factorial Function

A mathematical definition: For a non-negative integer *n*:

$$fac(n) = \begin{cases} 1 & \text{if } n \leq 1 \\ n * fac(n-1) & \text{otherwise} \end{cases}$$

- This definition tells us what a factorial is.
- Defined in cases: a base case and a recursive case

Factorial is defined in terms of itself

## A Recursive Factorial Function

Mathematics provides a rigorous framework for dealing with notions of what is, computation provides a rigorous framework for dealing with notions of how to. – SICP

To translate the mathematical definition of factorial (what a factorial *is* into a computational defiinition (*how to* compute a particular factorial), we need to

- identify the base case(s), and
- figure out how to get our computation to converge to a base case. For factorial, the solution is straightforward:

```
public static int fac(int n) {
    if (n <= 1) {
        return 1;
    } else {
        return n * fac(n - 1);
    }
}</pre>
```

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## The Substitution Model of Function Evaluation

- Functions are evaluated in an eval-apply cycle: function arguments are evaluated (which may in turn require function evaluation), then the function is applied to the arguments.
- The substitution model of evaluation is a tool for understanding function evaluation in general, and recursive processes in particular.

#### Here's fac(5):

```
fac(5)
5 * fac(4)
5 * 4 * fac(3)
5 * 4 * 3 * fac(2)
5 * 4 * 3 * 2 * fac(1)
5 * 4 * 3 * 2 * 1
5 * 4 * 3 * 2
5 * 4 * 6
5 * 24
120
```

## **Activation Records**

- Recursive subprograms cannot use statically allocated local variables, because each instance of the subprogram needs its own copies of local variables
- Most modern languages allocate local variables for functions on the run-time stack.
- The system provides a stack pointer pointing to the next available storage space on the stack.
- Subprogram instances use a frame pointer that points to their activation record, or stack frame, which contains its copies of local variables

## **Activation Record Example**

Consider this simplified example code (type annotations elided for brevity):

```
void main(args) {
  foo();
int foo()
  int r = 3;
  return fac(r);
int fac(n) {
  if (n <=1) {
    return 1
  } else {
    return n * fac(n-1)
```

The stack just before fac returns with 6:

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main frame	args = in main	
foo frame	r = 3 in foo	
	return value (TBD)	
fac(3) frame	parameter n = 3 in fac	
	return value (TBD)	
fac(2) frame	parameter n = 2 in fac	
	return value (TBD)	
fac(1) frame	parameter n = 1 in fac	
	return value (1 by definition)	

#### Stack Overflow

- The run-time stack is finite in size.
- If you put too many activation records on the stack (for example by calling a recursive function with a "large" argument), you will overflow the stack.

```
$ java Fac 10000
facLoop(10000) = 0
Exception in thread "main" java.lang.StackOverflowError
   at Fac.facIter(Fac.java:35)
   at Fac.facIter(Fac.java:38)
   at Fac.facIter(Fac.java:38)
...
```

#### Three ways to deal with this:

- limit input size (brittle how do you know limit on a particular machine?),
- increase stack size (brittle how do you know how big), or
- replace recursion with iteration.

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## Looping is Imperative Recursion

```
public static int facLoop(int n) {
   int factorialAccumulator = 1;
   for (int x = n; x > 0; x--) {
      factorialAccumulator *= x;
   }
   return factorialAccumulator;
}
```

- The base case is the termination condition for the loop.
- The loop variable converges to the termination condition.
- We "accumulate" the answer in the loop.

Recursive definitions are often more natural, but imperative/iterative definitions often perform better.

### Tail Recursion - Recursive Iteration

```
private static int facTail(int n) {
    return facHelper(n, 1);
}
private static int facIter(int n, int accum) {
    if (n <= 1) {
        return accum;
    } else {
        return facIter(n - 1, n * accum);
    }
}</pre>
```

Tail call optimization creates an iterative, rather than a recursive process:

```
facTail(5);
facIter(5, 1);
facIter(4, 5);
facIter(3, 20);
facIter(2, 60);
facIter(1, 120);
120
```

Note: Java does not optimize tail calls, but many-other languages

# **Closing Thoughts**

- Remember: A properly written recursive function must
  - handle the base case, and
  - convergence to the base case.
- Today we learned recursive processes. We'll also learn recursive data structures.