

Syntax

Action Fields	f_i	$::=$	$f_{a_1} \mid \cdots \mid f_{a_k}$	
Result Fields	f_r	$::=$	$f_{r_1} \mid \cdots \mid f_{r_k}$	
Fields	f	$::=$	$f_i \mid f_r$	
Actions	i	$::=$	$\{f_{a_1} = v_{a_1}, \dots, f_{a_k} = v_{a_k}\}$	
Results	r	$::=$	$\{f_{r_1} = v_{r_1}, \dots, f_{r_k} = v_{r_k}\}$	
Predicates	a, b	$::=$	0 <i>Identity</i> $ $ 1 <i>False</i> $ $ $f = n$ <i>Test</i> $ $ $a + b$ <i>Sum</i> $ $ $a \cdot b$ <i>Product</i> $ $ $\neg a$ <i>Negation</i>	
Policies	p, q	$::=$	a <i>Test</i> $ $ $act(p)$ <i>Slice Actions</i> $ $ $res(p)$ <i>Slice Results</i> $ $ inj_i <i>Injection Action</i> $ $ inj_r <i>Injection Result</i> $ $ $f \leftarrow n$ <i>Update</i> $ $ $p + q$ <i>Choice</i> $ $ $p \cdot q$ <i>Sequential Concatenation</i> $ $ p^* <i>Kleene Star</i>	

Semantics

$$\begin{aligned}
\llbracket \cdot \rrbracket &: P(A) \times P(R) \rightarrow P(A) \times P(R) \\
\llbracket 0 \rrbracket(-, -) &\triangleq (\emptyset, \emptyset) \\
\llbracket 1 \rrbracket(is, rs) &\triangleq (is, rs) \\
\llbracket f = n \rrbracket(is, rs) &\triangleq (\text{filter } (f = n) \text{ } is, \text{filter } (f = n) \text{ } rs) \\
\llbracket a + b \rrbracket(is, rs) &\triangleq \text{let } (is_a, rs_a) = \llbracket a \rrbracket(is, rs) \\
&\quad \text{let } (is_b, rs_b) = \llbracket b \rrbracket(is, rs) \\
&\quad (is_a \cup is_b, rs_a \cup rs_b) \\
\llbracket a \cdot b \rrbracket(is, rs) &\triangleq \text{let } (is_a, rs_a) = \llbracket a \rrbracket(is, rs) \\
&\quad \text{let } (is_b, rs_b) = \llbracket b \rrbracket(is, rs) \\
&\quad (is_a \cap is_b, rs_a \cap rs_b) \\
\llbracket \neg a \rrbracket(is, rs) &\triangleq \text{let } (is', rs') = \llbracket a \rrbracket(is, rs) \\
&\quad (is - is', rs - rs') \\
\llbracket act(p) \rrbracket(is, rs) &\triangleq \text{let } (is', rs') = \llbracket p \rrbracket(is, rs) \text{ in } (is', rs) \\
\llbracket res(p) \rrbracket(is, rs) &\triangleq \text{let } (is', rs') = \llbracket p \rrbracket(is, rs) \text{ in } (is, rs') \\
\llbracket inj_i(i) \rrbracket(is, rs) &\triangleq (\{i\} \cup is, rs) \\
\llbracket inj_r(r) \rrbracket(is, rs) &\triangleq (is, \{r\} \cup rs) \\
\llbracket f \leftarrow n \rrbracket(is, rs) &\triangleq (\text{map } (f \leftarrow n) \text{ } is, \text{map } (f \leftarrow n) \text{ } rs) \\
\llbracket p + q \rrbracket(is, rs) &\triangleq \text{let } (is_p, rs_p) = \llbracket p \rrbracket(is, rs) \\
&\quad \text{let } (is_q, rs_q) = \llbracket q \rrbracket(is, rs) \\
&\quad (is_p \cup is_q, rs_p \cup rs_q) \\
&\quad \dots\dots\dots \\
\llbracket p \cdot q \rrbracket(is, rs) &\triangleq \text{let } (is', rs') = \llbracket p \rrbracket(is, rs) \\
&\quad \llbracket q \rrbracket(is', rs') \\
\llbracket p^* \rrbracket \varphi &\triangleq ()?
\end{aligned}$$