



Name: Islam, Rafiqul

Id: 17-34438-1

Sec: A

1. *single-link* clustering

	BOS+NY+DC	MIA	CHI	SEA	SF	LA	DEN
BOS+NY+DC	0						
MIA	1075	0					
CHI	671	1329	0				
SEA	2684	3273	2013	0			
SF	2799	3053	2142	808	0		
LA	2621	2687	2054	1121	379	0	
DEN	1616	2037	996	1307	1235	1059	0

To update the distance matrix  $\min[\text{dist}(LA, SEA), \text{BOS} + NY + DC]$

$$\min[\text{dist}(LA, BOS+NY+DC), (SEA, BOS+NY+DC)]$$

$$= \min[2621, 2799] = 2621$$

To update the distance matrix  $\min[\text{dist}(LA, SF), MIA]$

$$\min[\text{dist}(LA, MIA), (SF, MIA)]$$

$$= \min[2687, 3053] = 2687$$

To update the distance matrix  $\min[\text{dist}(LA, CHI), SF]$

$$\min[\text{dist}(LA, CHI), (SF, CHI)] = \min[2054, 2142]$$

$$= 2054$$

To update the distance matrix  $\min[\text{dist}(LA, SEA), SF]$

$$\min[\text{dist}(LA, SEA), (SF, SEA)]$$

$$= \min(2684, 1121, 808) = 808$$

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To update the distance matrix  $\min[\text{dist}((LA, SF), DEN)$   
 $\cdot \min[\text{dist}((LA, DEN), (SF, DEN))] = \min[1059, 1235]$

$$= 1059$$

	BOB+NY+DC	MIA	CHI	SEA	SF+LA	DEN
BOB+NY+DC	0					
MIA	1075	0				
CHI	671	1329	0			
SEA	2684	3273	2013	0		
SF+LA	9621	2687	2054	808	0	
DEN	1616	2037	996	1307	1059	0

To update the distance matrix

$$\min[\text{dist}((BOB+NY+DC), CHI), MIA]$$

$$\min[\text{dist}((BOB+NY+DC), MIA), (CHI, MIA)]$$

$$= \min[1075, 1329] = 1075$$

To update the distance matrix

$$\min[\text{dist}((BOB+NY+DC), CHI), SEA]$$

$$= \min[\text{dist}((BOB+NY+DC), SEA), (CHI, SEA)]$$

$$= \min[2684, 2013] = 2013$$



To update the distance matrix  $\min[\text{dist}((BOS+NY+DC), CHI), SF+LA]$

$$= \min[\text{dist}((BOS+NY+DC), SF+LA), (CHI, SF+LA)]$$

$$= \min[2621, 2054] = 2054$$

To update the distance matrix  $\min[\text{dist}((BOS+NY+DC), DEN), CHI, DEN]$

$$= \min[\text{dist}((BOS+NY+DC), DEN), (CHI, DEN)]$$

$$= \min[1616, 996] = 996$$

	$BOS+NY+DC+CHI$	MIA	SEA	SF+LA	DEN
$BOS+NY+DC+CHI$	0				
MIA	1075	0			
SEA	2013	3273	0		
SF+LA	2054	2687	808	0	
DEN	996	2037	1307	1059	0

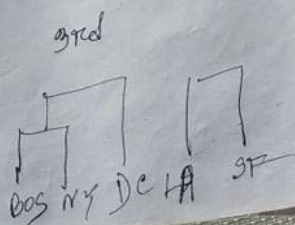
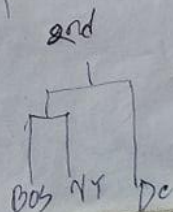
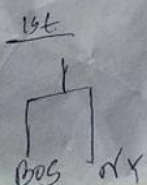


2. *average-link*

clustering

	BOS	NY	DC	MIA	CHI	SEA	SF	LA	DEN
BOS	0								
NY	206	0							
DC	420	222	0						
MIA	1504	1308	1075	0					
CHI	963	802	671	1329	0				
SEA	2976	2815	2684	3273	2013	0			
SF	2095	2934	2799	3053	2142	808	0		
LA	2979	2886	2621	2687	2054	1131	379	0	
DEN	1949	1771	1616	2037	226	1307	1235	1059	0

	BOS+NY	DC	MIA	CHI	SEA	SF	LA	DEN
BOS+NY	0							
DC	222	0						
MIA	1308	1075	0					
CHI	802	671	1329	0				
SEA	2815	2684	3273	2013	0			
SF	2934	2799	3053	2142	808	0		
LA	2886	2621	2687	2054	1131	379	0	
DEN	1771	1616	2037	226	1307	1235	1059	0





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	BOS+NY+DC	MIA	CHI	SEA	SF	LA	DEW
BOS+NY+DC	0						
MIA	1075	0					
CHI	671	1329	0				
SEA	2684	3273	2013	0			
SF	2799	3053	2142	880	0		
LA	2621	2687	2054	1121	1379	0	
DEW	1696	2037	906	1307	1235	1059	0

The distance matrix is  $\text{Avg}[\text{dist}(\text{LA}, \text{SF}), \text{BOS+NY+DC}]$   
 $\text{dist}(\text{LA}, \text{SF}) = \frac{1}{2} (\text{dist}(\text{LA}, \text{BOS+NY+DC}) + \text{dist}(\text{SF}, \text{BOS+NY+DC}))$

$$= \frac{1}{2} (2621 + 2799) = 2715$$

The distance matrix is  $\text{Avg}[\text{dist}(\text{LA}, \text{SF}), \text{MIA}]$

$$\text{dist}(\text{LA}, \text{SF}, \text{MIA}) = \frac{1}{2} (\text{dist}(\text{LA}, \text{MIA}) + \text{dist}(\text{SF}, \text{MIA}))$$

$$= \frac{1}{2} (2687 + 3053) = 2870$$

The distance matrix is  $\text{Avg}[\text{dist}(\text{LA}, \text{SF}), \text{CHI}]$

$$\text{dist}(\text{LA}, \text{SF}, \text{CHI}) = \frac{1}{2} (\text{dist}(\text{LA}, \text{CHI}) + \text{dist}(\text{SF}, \text{CHI}))$$

$$= \frac{1}{2} (2054 + 2142) = 2098$$

The distance matrix is  $\text{Avg}[\text{dist}(\text{LA}, \text{SF}), \text{SEA}]$   
 $\text{dist}(\text{LA}, \text{SF}, \text{SEA}) = \frac{1}{2} (\text{dist}(\text{LA}, \text{SEA}) + \text{dist}(\text{SF}, \text{SEA}))$

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$$\text{dist}(\text{SF}, \text{SEA}) = \frac{1}{2}(1131 + 808) = 269.5$$

BOS + NY + DC

MIA 1075

CHI 1671

SEA 2684

LA SF 2715

DEN 1616

0

1329 0

3273 2013 0

2870 2008 269.5 0

2037 996 1307 1147 0

To update the distance matrix  $\text{dist}(\text{LA}, \text{SF})$

$$\text{dist}(\text{LA}, \text{SF}) = \frac{1}{2}(\text{dist}(\text{LA}, \text{DEN}) + \text{dist}(\text{SF}, \text{DEN}))$$

$$= \frac{1}{2}(1235 + 1050) = 1147$$

To update the distance matrix  $\text{dist}(\text{BOS} + \text{NY} + \text{DC}, \text{MIA})$

$$\text{dist}(\text{BOS} + \text{NY} + \text{DC}, \text{MIA}) = \frac{1}{2}(\text{dist}(\text{BOS} + \text{NY} + \text{DC}, \text{CHI}) + \text{dist}(\text{BOS} + \text{NY} + \text{DC}, \text{SEA}))$$

$$= \frac{1}{2}(1075 + 1329) = 1202$$



6 To update the distance Matrix  $AVG \left[ \text{dist}((B03 + NY + DC), CHI) \right]$

$$\begin{aligned} \text{dist} \left[ ((B03 + NY + DC), CHI), SEA \right] &= \frac{1}{2} \left[ \text{dist}((B03 + NY + DC), SEA) + \text{dist}(CHI, SEA) \right] \\ &= \frac{1}{2} (2684 + 2013) \\ &= 2348.5 \end{aligned}$$

To update the distance Matrix  $AVG \left[ \text{dist}((B03 + NY), CHI), LA + SF \right]$

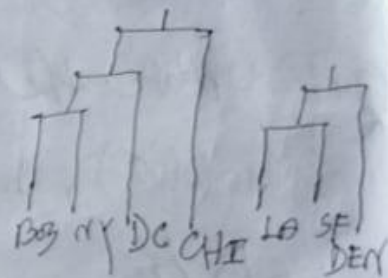
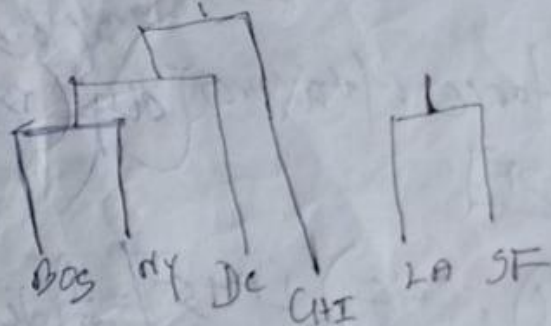
$$\begin{aligned} \text{dist} \left[ ((B03 + NY + DC), CHI), LA + SF \right] &= \frac{1}{2} \left[ \text{dist}((B03 + NY + DC), LA + SF) + \text{dist}(CHI, LA + SF) \right] \\ &= \frac{1}{2} (2715 + 2098) = 2406 \end{aligned}$$

To update the distance Matrix  $AVG \left[ \text{dist}((B03 + NY), CHI), DEN \right]$

$$\begin{aligned} \text{dist} \left[ ((B03 + NY + DC), CHI), DEN \right] &= \frac{1}{2} \left[ \text{dist}((B03 + NY + DC), DEN) + \text{dist}(CHI, DEN) \right] \\ &= \frac{1}{2} [1616 + 1796] = 1206 \end{aligned}$$

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	BOB	BOB+NY+DC+CHI	MIA	SEA	LA+SF	DEN
BOB+NY+DC+CHI	0					
MIA	1202		0			
SEA	2348		1329	0		
LA+SF	2406		3273	2013	0	
DEN	1306		2034	1307	1147	0
	426				546	



To update distance matrix  $\text{avg}[\text{dist}((\text{LA+SF}), \text{DEN}), (\text{BOB+NY+DC+CHI})]$

$$\begin{aligned}
 & \text{dist}((\text{LA+SF}), \text{DEN}), (\text{BOB+NY+DC+CHI}) \\
 &= \frac{1}{2} [\text{dist}((\text{LA+SF}), (\text{BOB+NY+DC+CHI})) + \text{dist}(\text{DEN}, (\text{BOB+NY+DC+CHI}))] \\
 &= \frac{1}{2} (2406 + 1306) = 1856
 \end{aligned}$$



To update the distance matrix  $AVG[dist((LA+SF), DEN)]$

$$dist((LA+SF), DEN), MIA = \frac{1}{2} [dist((LA+SF), MIA) + dist(MIA, DEN)]$$

$$= \frac{1}{2} (3273 + 2037) = 2655$$

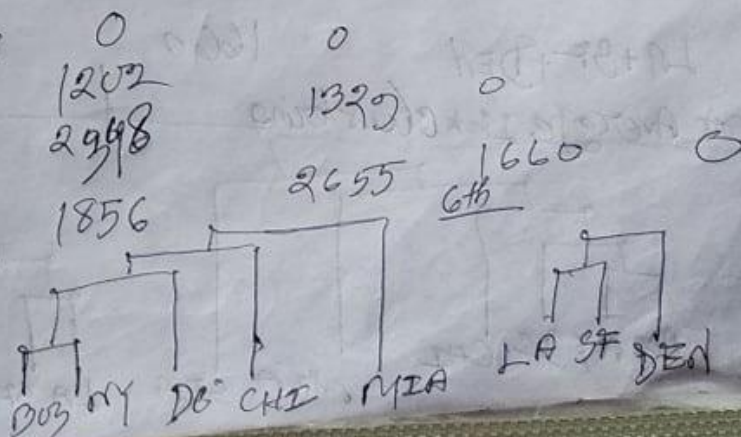
To update the distance matrix  $AVG[dist((LA+SF), DEN), SEA]$

$$dist((LA+SF), DEN), SEA = \frac{1}{2} [dist((LA+SF), SEA) + dist(DEN, SEA)]$$

$$= \frac{1}{2} (2013 + 1307) = 1660$$

BOB+NY+DC+CHI MIA SEA LA+SF+DEN

BOB+NY+DC+CHI  
MIA  
SEA  
LA+SF+DEN







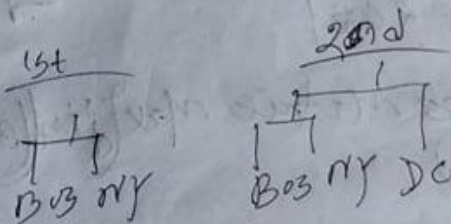
### 3. *complete-link*

clustering

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BOS+NY+DC MIA CHZ SEA SF LA DEN

BOS+NY+DC	0						
MIA	1075	0					
CHZ	671	1320	0				
SEA	2684	3273	2013	0			
SF	2799	3053	2142	808	0		
LA	2621	2687	2054	1121	370	0	
DEN	1616	2037	206	1307	1235	1059	0



To update the distance matrix  $\max[\text{dist}(\text{BOS+NY+DC}, \text{CHZ}), \text{MIA}]$

$$= \max[\text{dist}((\text{BOS+NY+DC}), \text{MIA}), (\text{CHZ}, \text{MIA})]$$

$$= \max[1075, 1320] = 1320$$

To update the distance matrix  $\max[\text{dist}(\text{BOS+NY+DC}, \text{CHZ}), \text{SEA}]$

$$= \max[\text{dist}((\text{BOS+NY+DC}), \text{SEA}), (\text{SEA}, \text{CHZ})]$$

$$= \max[2684, 2013] = 2684$$



To update the distance matrix  $\max[\text{dist}((BOS + NY + DC), CHI), SF]$

$$\max[\text{dist}((BOS + NY + DC), SF), (CHI, SF)]$$

$$= \max[2800, 2142] = 2800$$

To update the distance matrix  $\max[\text{dist}((BOS + NY + DC), LA), CHI]$

$$\max[\text{dist}((BOS + NY + DC), LA), (CHI, LA)]$$

$$= \max[2621, 2054] = 2621$$

To update the distance matrix  $\max[\text{dist}((BOS + NY + DC), DEN), CHI]$

$$\max[\text{dist}((BOS + NY + DC), DEN), (CHI, DEN)]$$

$$= \max[1616, 996] = 1616$$

	$BOS + NY + DC + CHI$	MIA	SEA	SF	LA	DEN
$BOS + NY + DC + CHI$	0					
MIA	1920	0				
SEA	2689	3273	0			
SF	2800	3053	808	0		
LA	2621	2687	1121	920	0	
DEN	1616					0

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	BOB+NY+DC	MIA	CHI	SEA	SF	LA	DEN
BOB+NY+DC	0						
MIA	1075	0					
CHI	671	1329	0				
SEA	2684	3273	2018	0			
SF	2799	3053	2142	808	0		
LA	2621	2687	2054	1131	370	0	
DEN	1616	2037	996	1307	1235	1059	0

To update the distance matrix  $\max[\text{dist}(LA, SF), \text{BOB+NY+DC}]$   
 $\cdot \max[\text{dist}(LA, \text{BOB+NY+DC}), \text{dist}(SF, \text{BOB+NY+DC})]$   
 $= \max[2621, 2799] = 2799$

To update the distance matrix  $\max[\text{dist}(LA, SF), \text{MIA}]$   
 $\cdot \max[\text{dist}(LA, \text{MIA}), \text{dist}(SF, \text{MIA})] = \max[2687, 2053]$   
 $= 2053$

To update the distance matrix  $\max[\text{dist}(LA, SF), \text{CHI}]$   
 $\cdot \max[\text{dist}(LA, \text{CHI}), \text{dist}(SF, \text{CHI})]$   
 $= \max[2054, 2142] = 2142$

To update the distance matrix  $\max[\text{dist}(LA, SF), \text{SEA}]$   
 $\cdot \max[\text{dist}(LA, \text{SEA}), \text{dist}(SF, \text{SEA})] = \max[1131, 808]$   
 $= 1131$



To update the distance matrix  $\max[\text{dist}(SF, LA)]$

$$\max[\text{dist}(SF, DEN), (LA, DEN)]$$

$$= \max[1235, 1059] = 1235$$

	BOB+NY+DC	MIA	CHI	SEA	SF+LA	DEN
BOB+NY+DC	0					
MIA	1075	0				
CHI	671	1329	0			
SEA	2684	3273	2013	0		
SF+LA	2799	3053	2142	1131	0	
DEN	1616	2037	226	1307	1235	0

To update the distance matrix  $\max[\text{dist}((BOB+NY+DC), CHI), MIA]$

$$\max[\text{dist}((BOB+NY+DC), CHI), (CHI, MIA)]$$

$$= \max[1075, 1329] = 1329$$

To update the distance matrix  $\max[\text{dist}((BOB+NY+DC), SEA), (CHI, SEA)]$

$$\max[\text{dist}((BOB+NY+DC), SEA), (CHI, SEA)]$$

$$= \max[2684, 2013] = 2684$$

To update the distance matrix  $\max[\text{dist}((BOB+NY+DC), SF+LA), (CHI, SF+LA)]$

$$\max[\text{dist}((BOB+NY+DC), SF+LA), (CHI, SF+LA)]$$

$$= \max[2799, 2142] = 2799$$

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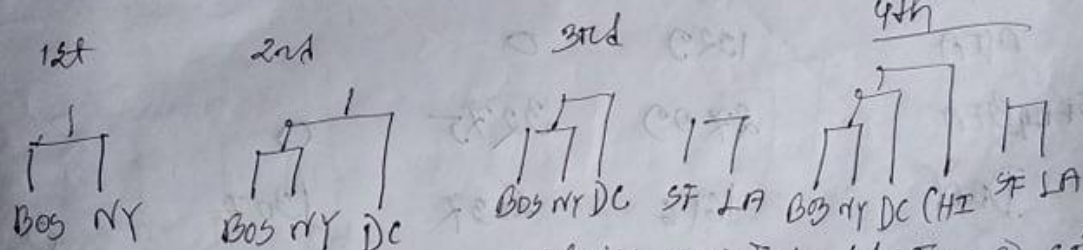


To update the distance matrix  $\max[\text{dist}((\text{BOS}+\text{NY}+\text{DC}), \text{CHI}), \text{DEN}]$

$$= \max[\text{dist}(\text{BOS}+\text{NY}+\text{DC}), \text{DEN}], (\text{CHI}, \text{DEN})]$$

$$= \max[1616, 0000] = 1616$$

	BOS+NY+DC+CHI	MIA	SEA	SF+LA	DEN
BOS+NY+DC+CHI	0				
MIA	1329	0			
SEA	2684	3283	0		
SF+LA	2709	3053	1121	0	
DEN	1616	2037	1307	1235	0



To update the distance matrix  $\max[\text{dist}((\text{SF}+\text{LA}), \text{SEA}), \text{dist}((\text{BOS}+\text{NY}+\text{DC}+\text{CHI}), \text{SEA})]$

$$= \max[2709, 2684] = 2709$$

To update the distance matrix  $\max[\text{dist}((SF+LA), SEA), MIA]$

$$= \max[\text{dist}((SF+LA), MIA), (SEA, MIA)]$$

$$= \max[2059, 3273] = 3275$$

To update the distance matrix  $\max[\text{dist}((SF+LA), DEN), SEA]$

$$\max[\text{dist}((SF+LA), DEN), (SEA, DEN)]$$

$$= \max[1235, 1307] = 1307$$

$BOB + \alpha\gamma + DC + CHI$	MIA	$SF+LA+SEA$	DEN
$BOB + \alpha\gamma + DC + CHI$	0		
MIA	1329	0	
$SF+LA+SEA$	2799	3275	0
DEN	1616	2037	1307

To update the distance matrix  $\max[\text{dist}((SF+LA+SEA), DEN), BOB + \alpha\gamma + DC + CHI]$

$$\max[\text{dist}((SF+LA+SEA), DEN), (BOB + \alpha\gamma + DC + CHI, DEN)]$$

$$= \max[2799, 1616] = 2799$$



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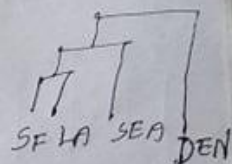
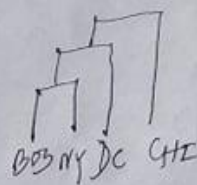
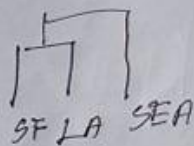
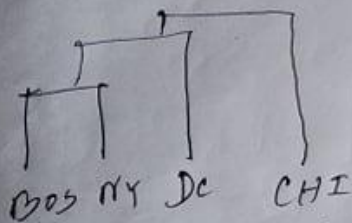
To update the distance matrix  $\max[\text{dist}(\text{DEN}, (\text{SF} + \text{LA} + \text{SEA}))$   
 $\text{MIA}]$

$$\max[\text{dist}(\text{SF} + \text{LA} + \text{SEA}, \text{MIA}), [\text{MIA}, \text{DEN}]]$$

$$= \max[32 \times 5, 203 \times] = 32 \times 5$$

	BOS + NY + DC + CHI	MIA	SF + LA + SEA + DEN
BOS + NY + DC + CHI	0		
MIA	1329	0	
SF + LA + SEA + DEN	2799	3275	0

5th



7th

