somebody make a fancy title page

Introduction

somebody write an introduction

bl.a. mention

- where we get the forward model from and what it does (this will not be explained in the following section)

1 Validation of Forward Model

The forward model computes from a set of oceanic and atmospheric parameters the brightness temperatures expected to be measured by a satellite radiometer. The input parameters are listed in Table 1, and the output parameters include values for both horizontal and vertical polarization at 6.93 GHz, 10.65 GHz, 18.70 GHz, 23.80 GHz, and 36.50 GHz.

	Forward Model		Reference Data	
	Abbrev.	Unit	Abbrev.	Unit
Ice concentration	C_is	fraction	ci	fraction
MY-fraction	F_MY	fraction		
Ice temperature	T_is	K	skt	K
Water vapour	V	mm (columnar)	tcwv	kg/m^2
Cloud liquid water	L	mm (columnar)	tclw	kg/m^2
Wind speed	W	m/s	ws	m/s
Sea surface temperature	T_ow	°C	sst	K

Table 1: Atmospheric and oceanic parameters entered into the forward model

This forward model was validated by comparing its results to reference data from ESA's "Sea Ice Climate Change Initiative".

1.1 Description of the Reference Data

The reference data consists of brightness temperatures at the relevant polarizations and frequencies as measured by the AMSR2 radiometer onboard the GCOM-W1 satellite. The measured data is paired with validated sea ice concentrations and numerical weather predictions for the atmospheric and oceanic parameters at the same geocoded locations at near simultaneous time. There are two different data sets: one with an ice concentration of 0, the other one with an ice concentration of 1. When using this reference data package to validate the forward model, several points have to be taken into account:

Firstly, the forward model was developed for the AMSR-E instrument. By using the atmospheric and oceanic parameters as input in the forward model in order to compare the output with the AMSR2 measured brightness temperatures, we assume that any calibration differences between AMSR-E and AMSR2 are negligible.

Secondly, the reference data does not contain information about the multi-year ice fraction needed as input in the forward model. For the data set with an ice concentration of 0, the MY fraction is irrelevant. It is therefore possible to validate the forward model for the open water datapoints. For the data set with an ice concentration of 1, a multi-year ice concentration of 0.5 was found to produce reasonable outputs of the forward model. This dataset can therefore be used as a coherency check, but not to validate the model.

Thirdly, the wind speed is given in the reference data as a u-component, v-component, and as a composite of the two. To simplify the validation procedure, we used the composite value for the wind speed as the input in the forward model.

The parameters "water vapour" and "cloud liquid water", which are given in the columnar units of kg/m^2 in the reference data, were converted to mm, indicating the height of water vapor or cloud liquid water if condensed uniformly across the column. $1\,kg/m^2$ corresponds to $1\,mm$ [3].

1.2 Validation Procedure

For the data set with an ice concentration of 0, the atmospheric and oceanic parameters were entered into the forward model, and the difference of the modelled brightness temperatures with respect to the reference data was recorded. The reference file has 6987 data points, all of which were used. For the data set with an ice concentration of 1, the atmospheric and oceanic parameters were entered together with a guessed value for the multi-year ice fraction. This value was chosen to be constant for all datapoints to simplify the validation process. To save computation time, only the first 1000 data points were used.

1.3 Validation Results

The discrepancies for the no ice condition are shown in Figure 1, and those for the ice condition are shown in Figure 2. Later in this report, the forward model will be used to develop an estimation of the impact a certain discrepancy in brightness temperature has on the modelled atmospheric and oceanic parameters.

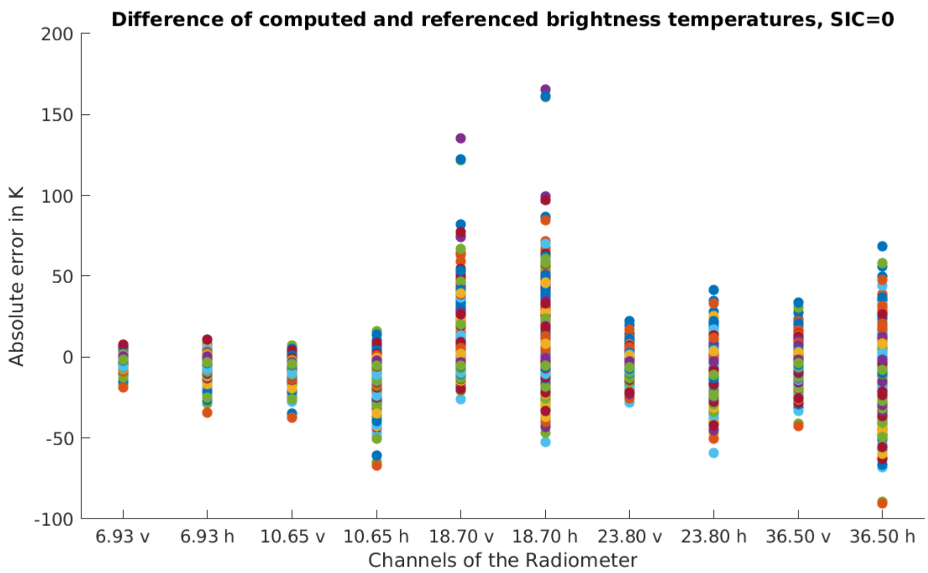

Figure 1: Modelled brigthness temperatures compared to the no ice dataset

For the no ice condition, the discrepancies in channels 10.65 h, 18.70 v and h, 23.80 h, and 36.50 h exceed $\pm 50\,K$. A histogram of the error distribution of these channels was plotted, see Figure 3. The modelled brightness temperatures appear to have an offset of approx. $-8\,K$, with a tendency to a higher offset for the higher frequencies. For the channels 10.65 h and 18.70 v, 90 % of the errors lie within $\pm 10\,K$ off the offset (mean error) of that channel. For the channels 18.70 v and 23.80 h, 90 % of the errors lie within $\pm 20\,K$ off the offset, and for the channel 36.50 h, 90 % of the errors lie within $\pm 30\,K$ off the offset.

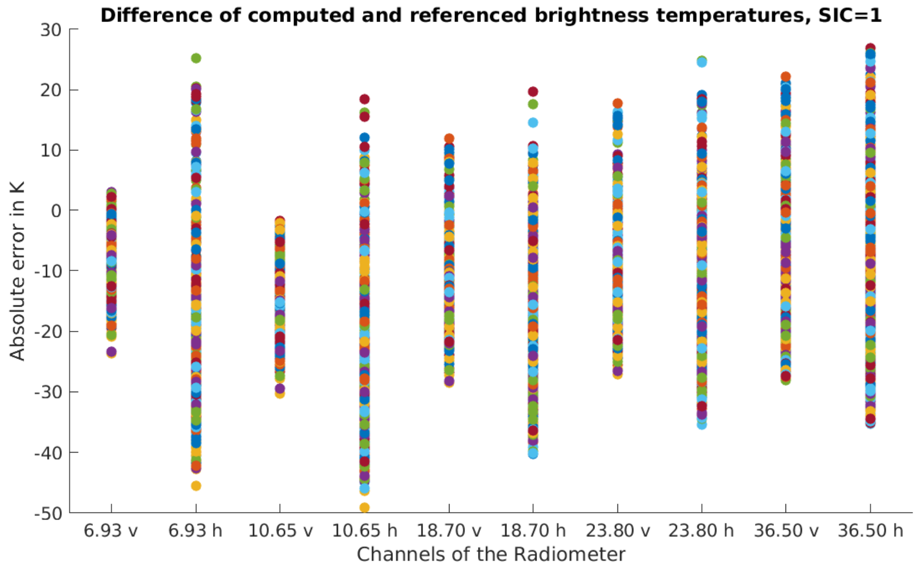

Figure 2: Modelled brigthness temperatures compared to the dataset with an ice concentration of 1

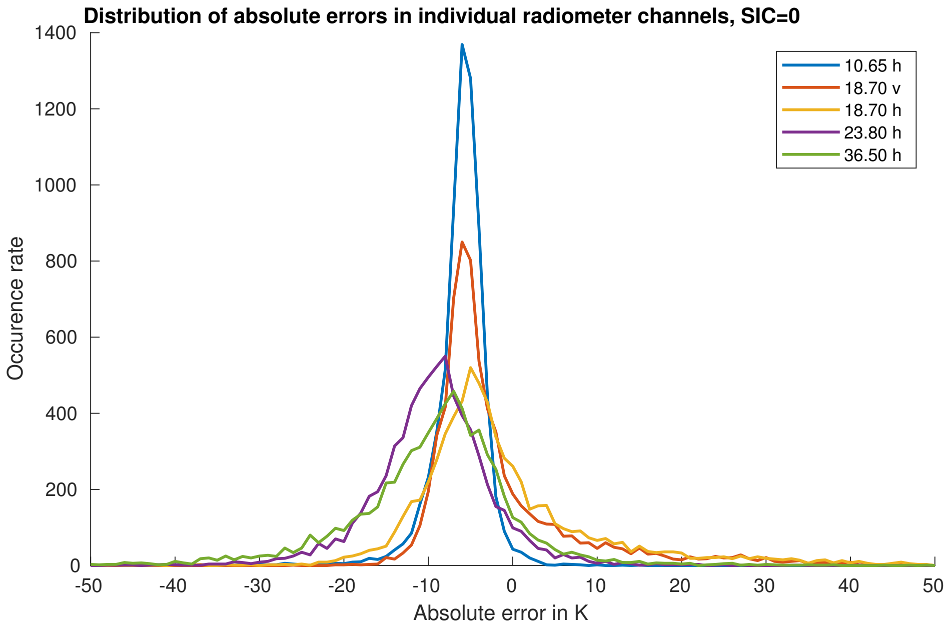

Figure 3: Distribution of the errors of the modelled brightness temperatures compared to the no ice dataset; only some channels are shown

The absolute error of the modelled data compared to the dataset with an ice concentration of 1 appears smaller than for the comparison to the dataset with the no ice condition. However, the minimization of this error was used as the criterion to find the best guess for the multi-year ice concentration. It is therefore not feasible to use this set of errors as a means of describing the accuracy of the forward model.

2 Development of Inverse Model

To compute the oceanic and atmospheric parameters from the set of brightness temperatures measured by the satellite radiometer, an inverse model was developed using estimation theory. The inverse model essentially employs the forward model to compute an estimate of the brightness temperatures from an estimate of the geophysical parameters, then compares the estimated brightness temperatures to the measured brightness temperatures, and finally improves the estimate for the geophysical parameters based on the result of the comparison. Once the estimated brightness temperatures come close enough to the measured ones, the geophysical parameters last inputted are considered a good estimate and delivered as the result of the inverse modelling. This is explained in more detail in the next subsection.

The inverse model was then validated [...]

2.1 Algorithm of the inverse model

The input of the inverse model function is a 10 element vector $T_{\mathrm{B,m}}$ containing the brightness temperatures measured for each of the radiometer channels. For a graphical overview of the elements of the function, see figure 4.

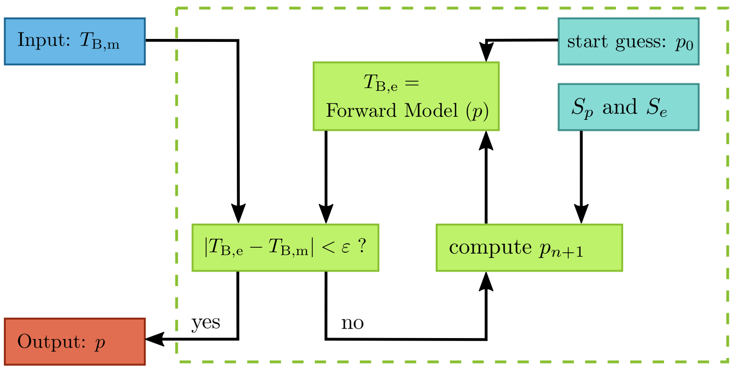

Figure 4: Blockdiagramm of the inverse model function

The inverse model enters a 7 element vector p containing estimates of the geophysical parameters listed in table 1 into the forward model and retrieves a 10 element vector $T_{\mathrm{B,e}}$ containing estimated brightness temperatures for each channel. In the first iteration, p is a generic guess, which was found from climate models and is hard coded into the inverse model function. The estimated brightness temperatures $T_{\mathrm{B,e}}$ are then compared to the measured brightness temperatures $T_{\mathrm{B,m}}$.

If the estimated and the measured brightness temperatures do not agree within a range of ε, a vector p_{n+1} for the (n+1)$^{\mathrm{th}}$ iteration is computed from the vector p_n of the n$^{\mathrm{th}}$ iteration as follows:

$$p_{n+1} = p_n + \left(S_p^{-1} + M_n^T S_e^{-1} M_n\right)^{-1} \cdot \left(M_n^T S_e^{-1}(T_{\mathrm{B,m}} - T_{\mathrm{B,e,n}}) + S_p^{-1}(p_0 - p_n)\right)$$

Herein, S_p is the 7 by 7 covariance matrix of the start guess of the geophysical parameters. Small values on the diagonal of this matrix correspond to a high confidence in the start guess and cause p_{n+1} to be close to p_0. S_e is the 10 by 10 covariance matrix of the brightness temperatures measured by the radiometer. Small values on the diagonal of this matrix correspond to a high confidence into the measurement accuracy, and much weight is assigned to the difference between the estimated and measured brightness temperatures, accordingly.

M_n is a 7 by 10 matrix, and it contains the partial derivatives of the brightness temperatures with respect to the geophysical parameters. This matrix is computed for every iteration. To find the element in the i^{th} line and j^{th} column of M, the i^{th} geophysical parameter is perturbed slightly, the forward model is called for the altered vector p, and the resulting perturbation of the brightness temperature in the j^{th} channel is recorded. The partial derivative is then obtained by dividing the brightness temperature perturbation by the perturbation of the geophysical parameter. Large values in M correspond of a high sensitivity of the radiometer to changes in the geophysical parameters.

The partial derivatives are only valid for those values of p at which they were computed - i.e. those of the past iteration. The inverse model extrapolates these derivatives to find p_{n+1} for the next iteration. If the relations of the geophysical parameters and the brightness temperatures were entirely linear, this extrapolation would be entirely accurate and only one iteration would be needed to find the suitable vector p. The less linear the system is, the less accurate is the extrapolation, and the more iterations are needed.

If the estimated and the measured brightness temperatures do agree within a range of ε, the current p is outputted as a sufficiently accurate estimation of the geophysical parameters.

References

[1] Dorthe Hofman-Bang, Forward algorithm, September 2003. http://www.seaice.dk/exercises/task3/Matlab/FW_funktion2_is.m [accessed: 18/11/2017]

[2] Round Robin Data Package Manual, Version 2.0/, July 2017. Ref: SICCI SIC RRDP-07-17. http://www.seaice.dk/undervisning/Sotiris/SICCI_RRDB_Manual_v2.01_20170717.docx [accessed: 18/11/2017]

[3] (unit conversion) http://www.remss.com/measurements/atmospheric-water-vapor/ [accessed: 18/11/2017]

[4] C. Elachi, Introduction to the Physics and Techniques of Remote Sensing. John Wiley and Sons, 1987. (section 6.5+7.3)