



[Course](#) > [Week 4](#) > [Proble...](#) > Finding...

Finding Lyapunov Functions

Finding Lyapunov Functions

0.0/15.0 points (graded)

Consider the system given by

$$\begin{aligned}\dot{x}_1 &= x_2 - x_1^3 \\ \dot{x}_2 &= -x_2^3 - x_1.\end{aligned}$$

Find a Lyapunov function $V(x_1, x_2)$ for this system in order to prove global asymptotic stability to the origin. Type in your answer in the MATLAB window below.

```
1 syms x1 x2 real;  
2 V = ; % Type in your answer here in terms of x1 and x2  
3
```

Unanswered

```
% For this question, the easiest way to obtain a Lyapunov function is to guess.  
% The simplest possible Lyapunov function one could guess is  $V(x) = x_1^2 + x_2^2$ .  
% Since this function is positive definite, we only need to check that its derivative  
% is negative definite. The time derivative is  $-2x_1^4 - 2x_2^4$ , which is clearly negative definite.
```

```
syms x1 x2 real;  
V = x1^2 + x2^2;
```

Run Code

Submit

You have used 0 of 3 attempts

i Answers are displayed within the problem

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