

# Mathematical Foundations of Data Sciences



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## Chapter 18

# Optimal Transport

TODO.

Refs [\[37, 33\]](#)



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