

Mathematical Foundations of Data Sciences



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Chapter 18

Optimal Transport

TODO.

Refs [\[37, 33\]](#)

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