# Microeconometrics

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Material available on





# Generalized method of moments

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## I heavily draw on the material presented in:

► Lee, D. S., & Lemieux, T. (2010). Regression discontinuity designs in economics. *Journal of economic literature*. 48(2), 281–355.

#### Issues

- intuition
- ▶ identification
- interpretation
- estimation

## Key points

- RD designs can be invalid if individuals can precisely manipulate the assignment variable.
  - discontinuity rules might generate incentives
- ▶ If individuals even while having some influence are unable to **precisely** manipulate the assignment variable, a **consequence** of this is that the variation in treatment near the threshold is randomized as though from a randomized experiment.
  - contrast to IV assumption

## **Key points**

- RD designs can be analyzed and tested like randomized experiments.
- Graphical representation of an RD design is helpful and informative, but the visual presentation should not be tilted toward either finding an effect or finding no effect.
- Nonparametric estimation does not represent a "solution" to functional form issues raised by RD designs. It is therefore helpful to view it as a complement to - rather than a substitute for - parametric estimation.

## **Key points**

► Goodness-of-fit and other statistical tests can help rule out overly restrictive specifications.

#### **Baseline**

A simple way to estimating the treatment effect  $\tau$  is to run the following linear regression.

$$Y = \alpha + D\tau + X\beta + \epsilon$$
,

where  $D \in [0, 1]$  and we have D = 1 if  $X \ge c$  and D = 0 otherwise.

# **Baseline setup**

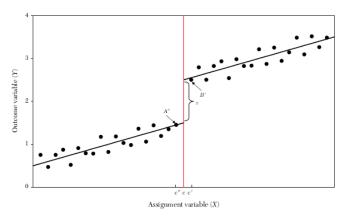


Figure 1. Simple Linear RD Setup

## **Potential outcome framework**

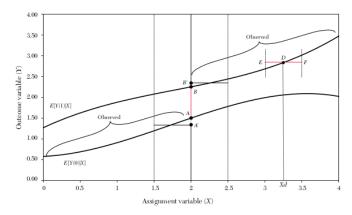


Figure 2. Nonlinear RD

#### Potential outcome framework

$$E[Y_i(1) - Y_i(0) | X = c]$$

⇒ average treatment effect at the cutoff

#### **Alternatives**

Consider the standard assumptions for matching:

- ignorability
  - trivially satisfied by research design
- common support
  - cannot be satisfied and replaced by continuity

#### **Alternatives**

Lee and Lemieux (2010) emphasize the close connection of RDD to randomized experiments.

How does the graph in the potential outcome framework change?

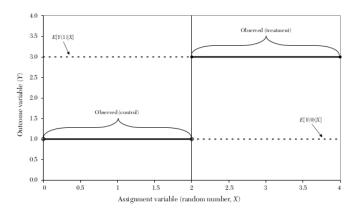


Figure 3. Randomized Experiment as a RD Design

Continuity, the key assumption of RDD, is a consequence of the research design and not simply imposed.

# **Identification**

## Question

► How do I know whether an RD design is appropriate for my context? When are the identification assumptions plausable or implausable?

#### **Answers**

- × An RD design will be appropriate if it is plausible that all other unobservable factors are "continuously" related to the assignment variable.
- ✓ When there is a continuously distributed stochastic error component to the assignment variable - which can occur when optimizing agents do not have precise control over the assignment variable - then the variation in the treatment will be as good as randomized in a neighborhood around the discontinuity threshold.

## Question

▶ Is there any way I can test those assumptions?

#### **Answers**

- No, the continuity assumption is necessary so there are no tests for the validity of the design.
- √ Yes. As in randomized experiment, the distribution of observed baseline covariates should not change discontinuously around the threshold.

## Simplified setup

$$Y = D\tau + W\delta_1 + U$$
$$D = I[X \ge c]$$
$$X = W\delta_2 + V$$

► *W* is the vector of all predetermined and observable characteristics.

What are the source of heterogeneity in the outcome and assignment variable?

## Simplified setup

The setup for an RD design is more flexible than other estimation strategies.

- ▶ We allow for W to be endogenously determined as long as it is determined prior to V.
- ► We take no stance as to whether some elements  $δ_1$  and  $δ_2$  are zero (exclusion restrictions)
- We make no assumptions about the correlations between W, U, and V.

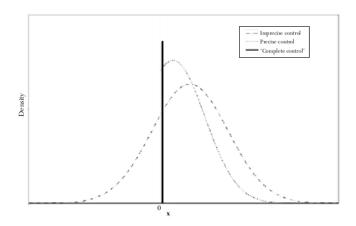


Figure 4. Density of Assignment Variable Conditional on  $W=w,\,U=u$ 

#### **Local randomization**

**Definition** We say individuals have imprecise control over X when conditional on W = w and U = u the density of V (and hence X) is continuous.

## **Applying Baye's rule**

$$Pr[W = w, U = u \mid X = x]$$
  
=  $f(x \mid W = w, U = u)$   $\frac{Pr[W = w, U = u]}{f(x)}$ 

**Local randomization** If individuals have imprecise control over X as defined above, then  $\Pr[W = w, U = u \mid X = x]$  is continuous in x: the treatment is "as good as" randomly assigned around the cutoff.

 $\Rightarrow$  the **behavioral** assumption of imprecise control of X around the threshold has the **prediction** that treatment is locally randmized.

## **Consequences**

- ▶ testing prediction that  $Pr[W = w, U = u \mid X = x]$  is continuous in x
- irrelevance of including baseline covariates

# Interpretation

## **Questions**

► To what extent are results from RD designs generalizable?

#### **Answers**

- x The RD estimate of the treatment effect is only applicable to the subpopulation of individuals at the discontinuity threshold and uninformative about the effect everywhere else.
- √ The RD estimand can be interpreted as a weighted average treatment effect, where the weights are relative ex ante probability that the value of an individual's assignment variable will be in the neighborhood of the threshold.

## Accounting for treatment effect heterogeneity

$$Y = D\tau(W, U) + W\delta_1 + U$$

What is creating treatment effect heterogeneity?

## Accounting for treatment effect heterogeneity

$$\lim_{\epsilon \downarrow 0} E(Y \mid X = c + \epsilon) - \lim_{\epsilon \uparrow 0} E(Y \mid X = c + \epsilon) = ?$$

## Alternative evaluation strategies

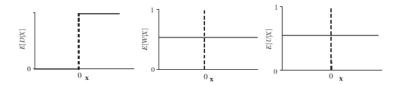
- randomized experiment
- regression discontinuity design
- matching on observables
- instrumental variables

How do the (assumed) relationships between the observables and unobservable differ?

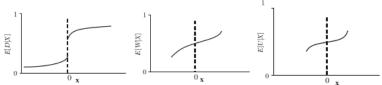
## **Endogenous dummy variable**

$$Y = D\tau + W\delta_1 + U$$
$$D = I[X \ge c]$$
$$X = W\delta_2 + V$$

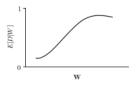
## A. Randomized Experiment

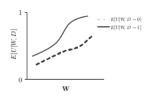


## B. Regression Discontinuity Design



### C. Matching on Observables





#### D. Instrumental Variables



# **Estimation**

We will explore issues in estimation using a Python notebook.

http://bit.ly/2WGjWNI

# **Checklist**

### Recommendations

- ► To assess the possibility of manipulations of the assignment variable, show its distribution.
- Present the main RD graph using binned local averages.
- Graph a benchmark polynomial specification.

### Recommendations

- Explore the sensitivity of the results to a range of bandwidth, and a range of orders to the polynomial.
- Conduct a parallel RD analysis on the baseline covariates.
- Explore the sensitivity of the results to the inclusion of baseline covariates.

### Resources

### **Technical**

► Hahn, J., Todd, P. E., & van der Klaauw, W. (2001). Identification and estimation of treatment effects with a regression-discontinuity design. *Econometrica*, 69(1), 201–209.

### **Applications**

- Lee, D. S. (2008). Randomized experiments from nonrandom selection in us house elections. *Journal of Econometrics*, 142(2), 675–697.
- ► Thistlethwaite, D. L., & Campbell, D. T. (1960). Regression-discontinuity analysis: An alternative to the ex-post facto experiment. *Journal of Educational Psychology*, 51(6), 309–317.

# **Appendix**

# References

- Hahn, J., Todd, P. E., & van der Klaauw, W. (2001). Identification and estimation of treatment effects with a regression-discontinuity design. *Econometrica*, 69(1), 201–209.
- Lee, D. S. (2008). Randomized experiments from non-random selection in us house elections. *Journal of Econometrics*, 142(2), 675–697.
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