难度: 1星: 省三必会。2星: 省二尽可能会,省一必会。3星:省一尽可能会。4星:国2以上要会

二分

整数二分 (利用lowerbound+upperbound解题):

模板: https://www.lanqiao.cn/problems/18492/learning/

最大通过数: https://www.lanqiao.cn/problems/3346/learning/ 2星

第k小的和: https://www.lanqiao.cn/problems/17098/learning/4星

123: https://www.langiao.cn/problems/1591/learning/ 4星

二分模版

```
#include <iostream>
 2
 3
    using namespace std;
 5
    const int N = 1e5 + 10;
 6
 7
    int n, q;
 8
    int a[N];
9
10
    int main()
11
12
        cin >> n >> q;
13
14
        for(int i = 1; i \le n; i ++) cin >> a[i];
15
16
        while(q --)
17
        {
             int t, 1, r, x;
18
19
            cin >> t >> 1 >> r >> x;
20
            if(t == 1)
21
22
                 while(1 < r)
23
                 {
24
                     int mid = 1 + r \gg 1;
25
                     if(a[mid] >= x) r = mid;
                     else l = mid + 1;
26
27
28
                 if(a[1] != x) cout << -1 << end1;
                 else cout << 1 << endl;</pre>
29
30
             }
             else if(t == 2)
31
32
33
                 while(1 < r)
34
                 {
35
                     int mid = 1 + r + 1 >> 1;
                     if(a[mid] \le x) 1 = mid;
36
37
                     else r = mid - 1;
38
39
                 if(a[1] != x) cout << -1 << end];
```

```
40
                  else cout << 1 << endl;</pre>
41
             }
42
             else if(t == 3)
43
             {
44
                 while(1 < r)
45
46
                      int mid = 1 + r \gg 1;
47
                      if(a[mid] >= x) r = mid;
48
                      else l = mid + 1;
49
                  if(a[1] < x) cout << -1 << endl;
50
51
                  else cout << l << endl;</pre>
52
             }
53
             else
54
             {
55
                 while(1 < r)
56
                  {
57
                      int mid = 1 + r \gg 1;
58
                      if(a[mid] > x) r = mid;
59
                      else l = mid + 1;
                  }
60
61
                  if(a[1] \ll x) cout \ll -1 \ll end];
62
                  else cout << 1 << endl;</pre>
63
             }
64
65
         return 0;
66
    }
```

```
import java.io.BufferedReader;
2
    import java.io.IOException;
 3
    import java.io.InputStreamReader;
    import java.io.PrintWriter;
    import java.util.StringTokenizer;
6
7
    public class Main {
8
9
        public static void main(String[] args) {
             int t=1;
10
11
            while(t-->0) solve();
12
13
            out.flush();
14
        }
        static int N=(int)(1e5+10);
15
16
        static int a[]=new int[N];
17
        static int n;
        static int getL(int a[],int 1,int r,int x){
18
19
          while(l<r){</pre>
             int mid=1+r>>1;
20
21
            if(x<=a[mid]){</pre>
22
               r=mid;
23
            }else{
24
               l=mid+1;
             }
25
26
27
          if(a[1]!=x) return -1;
          return 1;
28
        }
29
```

```
30
         static int getR(int a[],int 1,int r,int x){
31
           while(1< r){
32
             int mid=1+r+1>>1;
33
             if(x<a[mid]){</pre>
34
               r=mid-1;
35
             }else{
36
               1=mid;
37
             }
38
           }
39
           if(a[1]!=x) return -1;
40
           return 1;
41
         }
42
         static int lower_bound(int a[],int l,int r,int x){
43
           if(a[r] < x) return -1;
44
           while(1< r){
45
             int mid=1+r>>1;
             if(x<=a[mid]){</pre>
46
47
               r=mid;
             }else{
48
49
               l=mid+1;
50
             }
51
           }
52
           return 1;
53
         }
54
         static int upper_bound(int a[],int 1,int r,int x){
           if(a[r] \le x) return -1;
55
           while(1< r){
56
             int mid=1+r>>1;
57
58
             if(x<a[mid]){</pre>
59
               r=mid;
60
             }else{
61
               l=mid+1;
62
             }
63
           }
64
           return 1;
65
        }
         static void solve(){
66
67
           n=in.nextInt();
           int q=in.nextInt();
68
69
           for(int i=1;i<=n;i++){</pre>
70
             a[i]=in.nextInt();
71
           }
           while(q-->0){
72
73
             int op=in.nextInt();
74
             int l=in.nextInt();
75
             int r=in.nextInt();
76
             int x=in.nextInt();
77
             if(op==1){
78
               out.println(getL(a,l,r,x));
79
             }else if(op==2){
80
               out.println(getR(a,1,r,x));
81
             }else if(op==3){
               out.println(lower_bound(a,1,r,x));
82
             }else{
83
84
               out.println(upper_bound(a,1,r,x));
             }
85
86
           }
87
         }
```

```
88
         static FastReader in = new FastReader();
 89
         static PrintWriter out=new PrintWriter(System.out);
 90
         static class FastReader{
 91
             static BufferedReader br;
 92
             static StringTokenizer st;
 93
             FastReader(){
 94
                  br=new BufferedReader(new InputStreamReader(System.in));
 95
             }
 96
             String next(){
 97
                  String str="";
 98
                  while(st==null||!st.hasMoreElements()){
 99
                      try {
100
                          str=br.readLine();
101
                      } catch (IOException e) {
102
                          throw new RuntimeException(e);
103
                      }
104
                      st=new StringTokenizer(str);
105
                  }
106
                  return st.nextToken();
107
             }
             int nextInt(){
108
109
                  return Integer.parseInt(next());
110
             }
             double nextDouble(){
111
112
                  return Double.parseDouble(next());
113
             long nextLong(){
114
115
                  return Long.parseLong(next());
116
             }
117
         }
118
     }
```

```
1
    def main():
 2
        import sys
 3
        input = sys.stdin.read
 4
        data = input().split()
 5
 6
        idx = 0
 7
        n = int(data[idx])
 8
        q = int(data[idx + 1])
 9
        idx += 2
10
        a = [0] * (n + 1)
11
12
        for i in range(1, n + 1):
             a[i] = int(data[idx])
13
            idx += 1
14
15
        for _ in range(q):
16
17
            t = int(data[idx])
18
             l = int(data[idx + 1])
             r = int(data[idx + 2])
19
             x = int(data[idx + 3])
20
             idx += 4
21
22
             if t == 1:
23
                 while 1 < r:
24
                     mid = (1 + r) // 2
25
```

```
26
                     if a[mid] >= x:
27
                          r = mid
28
                     else:
                         1 = mid + 1
29
                 if a[1] != x:
30
31
                     print(-1)
32
                 else:
33
                     print(1)
             elif t == 2:
34
35
                 while 1 < r:
                     mid = (1 + r + 1) // 2
36
37
                     if a[mid] \leftarrow x:
                         1 = mid
38
39
                     else:
                          r = mid - 1
40
                 if a[1] != x:
41
42
                     print(-1)
43
                 else:
44
                     print(1)
             elif t == 3:
45
46
                 while 1 < r:
                     mid = (1 + r) // 2
47
48
                     if a[mid] >= x:
49
                         r = mid
50
                     else:
51
                         1 = mid + 1
52
                 if a[1] < x:
53
                     print(-1)
54
                 else:
55
                     print(1)
             elif t == 4:
56
                 while 1 < r:
57
58
                     mid = (1 + r) // 2
59
                     if a[mid] > x:
60
                          r = mid
61
                     else:
62
                          1 = mid + 1
                 if a[1] <= x:
63
64
                     print(-1)
65
                 else:
66
                     print(1)
67
    if __name__ == "__main__":
68
69
        main()
```

最大通过数

```
#include<bits/stdc++.h>
 2
    using namespace std;
 3
    #define int long long
 4
    const int N=2e5+5;
 5
    int a[N],b[N];
 6
    signed main()
 7
       \verb"ios::sync_with_stdio(0), \verb"cin.tie(0)", \verb"cout.tie(0)";"
 8
9
       int n,m,k;
10
       cin>>n>>m>>k;
```

```
11
       for(int i=1;i<=n;i++)
12
         cin>>a[i];
13
14
         a[i] += a[i-1];
15
16
       for(int i=1;i<=m;i++)</pre>
17
18
         cin>>b[i];
19
         b[i]+=b[i-1];
20
       }
21
       int ans=0;
22
       for(int i=0;i<=n;i++)</pre>
23
24
         if(a[i]>k)
25
           break;
         int x=upper_bound(b,b+1+m,k-a[i])-b-1;
26
27
         ans=max(i+x,ans);
28
       }
29
       cout<<ans;</pre>
30
       return 0;
31 }
```

```
import java.util.*;
 2
 3
    public class Main {
 4
        public static void main(String[] args) {
 5
             Scanner sc = new Scanner(System.in);
 6
             int n = sc.nextInt(), m = sc.nextInt(), k = sc.nextInt();
 7
 8
             long[] a = new long[n + 1];
 9
            long[] b = new long[m + 1];
10
             for (int i = 1; i <= n; i++) {
11
12
                 a[i] = sc.nextLong() + a[i - 1];
13
             }
14
15
             for (int i = 1; i <= m; i++) {
                 b[i] = sc.nextLong() + b[i - 1];
16
17
             }
18
            int ans = 0;
19
20
             for (int i = 0; i <= n; i++) {
                 if (a[i] > k) break;
21
22
                 int x = upperBound(b, k - a[i]) - 1;
23
                 ans = Math.max(i + x, ans);
             }
24
25
26
             System.out.println(ans);
27
             sc.close();
        }
28
29
30
        private static int upperBound(long[] arr, long key) {
             int left = 0, right = arr.length;
31
32
             while (left < right) {</pre>
33
                 int mid = (left + right) / 2;
34
                 if (arr[mid] <= key) left = mid + 1;</pre>
35
                 else right = mid;
```

```
36 }
37 return left;
38 }
39 }
40
```

```
1 import bisect
2
3 n, m, k = map(int, input().split())
4 | a = [0] + list(map(int, input().split()))
5
   b = [0] + list(map(int, input().split()))
7
   # 前缀和计算
8 for i in range(1, n + 1):
9
      a[i] += a[i - 1]
10 for i in range(1, m + 1):
      b[i] += b[i - 1]
11
12
13 ans = 0
14 for i in range(n + 1):
15
      if a[i] > k:
16
           break
17
      x = bisect.bisect_right(b, k - a[i]) - 1
18
      ans = max(i + x, ans)
19
20 print(ans)
21
```