$\begin{array}{c} {\rm Team\ Control\ Number} \\ {\bf 201906177} \end{array}$

Problem Chosen

 \mathbf{A}

ShuWei Cup

Summary

keyword: sweet spot; corked bat; coefficient of restitution;

Contents

1	Intr 1.1 1.2	Poduction Background	1 1 1
2	Pro	blem Analysis	1
3	Syn 3.1 3.2	nbol and Assumptions Symbol Description	2 2 2
4		ablishment and solution of the model	3
-	4.1	The model of Problem 1	3
	1.1	4.1.1 Establishment of model	3
		4.1.2 Solution of Grey Markov Model	5
		4.1.3 Conclusion	8
	4.2	The model of Problem 2	8
		4.2.1 Establishment of model	8
		4.2.2 Calculation of predictors	8
		4.2.3 TOPSIS	9
		4.2.4 Results and Conclusion	10
	4.3	The model of Problem 3	11
		4.3.1 Establishment of model	11
		4.3.2 Solution of model	12
	4.4	The model of Problem 4	12
	4.5	A letter to the medical department	12
5	Sen	sitivity Analysis	14
6	Stre	engths and Weaknesses	14
	6.1	Strengths	14
	6.2	Weaknesses	14
7	Cor	nclusion	14

Team # 201906177 page1 of 15

1 Introduction

1.1 Background

With the rapid development of China's economy and the deepening trend of aging, people's demand for hospital health services is also getting higher and higher. Therefore, it is of great significance to establish an appropriate model to study the trend of aging in the future and the trend of people's demand for medical care. At the same time, the establishment of a reasonable competition and cooperation mechanism between private and public hospitals can also maximize the utilization of resources.

1.2 Work

The problem requires us to make rational use of network resources?answer the following questions

- 1. The aging trend of China and the people's medical needs to make a reasonable forecast.
- 2. Take a province as an example to analyze the most common disease in the future.
- 3. According to the medical needs of patients, an optimal queuing method is proposed to equalize the number of queues between different hospitals and different departments of the same hospital.
- 4. Put forward the best cooperation and competition strategy between private hospital and public hospital.
- 5. Write recommendations for relevant medical departments and prepare "14 five-year plans" for their reference.

2 Problem Analysis

Analysis of task one According to the relevant data from 2009 to 2018 in the National Bureau of statistics, the group first selects appropriate indicators and then establishes a grey prediction model to predict and analyze the population aging trend and residents' medical needs of the epidemic in 2009-2018. Then, through the Markov model, the data from 2009-2018 simulates the distribution of residual in each interval and calculates the expectation of the predicted residual in 2019-2021 Value. Finally, the prediction results and residual expectation are made to be different, and the inherent deviation of traditional grey prediction is corrected.

Team # 201906177 page 2 of 15

Through the combination of the two models, the goal of scientific prediction of the future development of population aging and the trend of residents' medical needs is achieved.

Analysis of task two According to the second question, we are asked to analyze the most common diseases in a specific province in the future . we took the Hubei province as an example to collect data on common diseases such as heart disease, and established a model with Markov model. And calculated The number of cases, growth rate of cases, growth rate of deaths and death rate of each disease, Then substituted the five index data into the principal component analysis model. The disease with the highest score was the most common disease in the province in the future.

Analysis of task three The question three ask us to propose a common queuing theory method and figure its related optimal queuing for this kind of queuing problem. Via referring to the operational mode of the real world hospital, we choose to adopt the $M/M/c/\infty$ model as the required theory. Then we acquire the hospital statistics and abstract the data into the parameter in model. Finally, to get the social cost to be lowest, we manage to find the optimized systems design for the queuing model.

Analysis of task four

Analysis of task five

3 Symbol and Assumptions

3.1 Symbol Description

symbols	definitions
$\overline{v_i}$	velocity of ball before collision
v_f	velocity of ball after collision
V_f	velocity of bat after collision
\mathring{S}	the shear modulus the bat
Y	Young; s modulus of the bat

3.2 Fundamental assumptions

1. The hourly wage of patient could be considered as the cost dissipated in queuing. And the hourly wage of doctor could be seen as the cost of cost of service.

Team # 201906177 page3 of 15

4 Establishment and solution of the model

4.1 The model of Problem 1

4.1.1 Establishment of model

GM(1,1) The total number of cases in 2009-2018 is time series:

$$X^{(0)} = [x^{(0)}(1), x^{(0)}(2), \cdots, x^{(0)}(10)]$$

Generate a 1-AGO sequence by one accumulation:

$$X^{(1)} = [x^{(1)}(1), x^{(1)}(2), \cdots, x^{(1)}(10)]$$

In the formula: $x^{(1)}(k) = \sum_{i=1}^{k} x^{(1)}(i), k = 1, 2, \dots, 10$. Establish a differential equation based on the 1-AGO sequence as:

$$\frac{dX^{(1)}}{dt} + aX^{(1)} = u \tag{1}$$

In the formula: a is Develop grayscale, u is Endogenous control grayscale. Let $\widehat{\alpha}$ be the parameter vector to be estimated and $\widehat{\alpha} = [a, u]^T$, be found by least squares method:

$$\widehat{\alpha} = (B^T B)^{-1} B^T Y_n \tag{2}$$

Solving equation 1 , The preliminary prediction model for the k+1 aging is available:

$$\widehat{X}(k+1) = \left[X^{(0)}(1) - \frac{u}{a}\right]e^{-ak} + \frac{u}{a}, k = 1, 2, \dots, 10$$
(3)

Similarly, the death number is taken as the vector $X^{(0)} = [x^{(0)}(1), x^{(0)}(2), \dots, x^{(0)}(10)]$ Bring in the model to obtain the 2019-2021 death number grayscale prediction value.

Markov correction The Markov model is used to estimate the state and state probability of the GM(1,1) prediction error term, and the predicted value of the predicted state is used to correct the GM(1,1) prediction value. The state is divided by the 2009-2018 forecast data and the real data residual, and the residual sequence is:

$$\varepsilon = [\varepsilon(1), \varepsilon(2), \cdots, \varepsilon(10)]$$

Team # 201906177 page4 of 15

Absolute maximum residual value $\delta_{max} = \max_{1 \leq i \leq 10} |\varepsilon(i)|$. The prediction error is divided into three states. Let $\lambda = \frac{\delta_{max}}{6}$. The status is $E_1 : (-3\lambda, -\lambda), E_2 : (-\lambda, \lambda)$ and $E_1 : (\lambda, 3\lambda)$. The formula for calculating the initial state probability vector is:

$$\begin{cases}
 p_{Ek} = \frac{n_{Ek}}{13} \\
 t_0 = [p_{E1}, p_{E2}, p_{E3}]
\end{cases}$$
(4)

In the formula: n_{Ek} is number of E_k occurrences in 2008-2019. Replace the probability E_k of its occurrence with the frequency at which the state p_{Ek} appears. And construct the state transition matrix as:

$$P = \left(\begin{array}{ccc} P_{11} & P_{12} & P_{13} \\ P_{21} & P_{22} & P_{23} \\ P_{31} & P_{32} & P_{33} \end{array}\right)$$

In the formula: P_{ij} is E_i transition probability transferred to E_j after a period. That is, the Markov model can be expressed as:

$$t_{k+1} = t_k \cdot p \tag{5}$$

Let the middle value of the status interval be $\overline{E}_1, \overline{E}_2$ and \overline{E}_3 , so the error expectation of GM(1,1) in the kth year is: .

$$\eta = \begin{bmatrix} p_{E1} & p_{E2} & p_{E3} \end{bmatrix} \cdot \begin{bmatrix} \overline{E}_1 \\ \overline{E}_2 \\ \overline{E}_3 \end{bmatrix}$$
 (6)

When the predicted value of GM(1,1) for the number of patients in the k year is $\widehat{x}(k)$, Modified grey Markov combination forecast model $\overline{x}(k)$ Can be recorded as?

$$\overline{x}(k) = \widehat{x}(k) - \eta \tag{7}$$

Forecast result evaluation index Root mean square error (RMSE), average phase error absolute value (MAPE), and Nash efficiency coefficient (NSE) are commonly used to measure prediction results. The RMSE can evaluate the high-value predictions of the number of patients and the number of deaths. The calculation formula is:

RMSE =
$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - y_i^*)^2}$$

Team # 201906177 page 5 of 15

The smaller the root mean square error, the higher the reliability of the model and the more accurate the result.

MAPE is used to evaluate the prediction results of the stationary part of the prediction data. The calculation formula is:

MAPE =
$$\frac{1}{n} \sum_{i=1}^{n} \left| \frac{y_i - y_i^*}{y_i} \right| \times 100\%$$

The value obtained by MAPE is an absolute value, which is a relative index. When two MAPE values are compared, the smaller the value, the higher the reliability of the model.

The NSE can be used to evaluate the predictive power of the model. The formula is as follows:

$$NSE = 1 - \frac{\sum_{i=1}^{n} (y_i - y_i^*)^2}{\sum_{i=1}^{n} (y_i - \overline{y})^2}$$

The closer the NSE value is to 1, the better the model quality and the higher the model's credibility. Close to 0, indicating that the simulation result is close to the average level of observations, that is, the overall result is credible, but the simulation error is large. Far less than 0, the model is not credible.

4.1.2 Solution of Grey Markov Model

The predicted values of the Chinese elderly population forecast for 2009-2018 by GM(1,1) are as follows:

$$\widehat{X}(k+1) = 266856.0905e^{0.042782k} - 255354.5841, k = 1, 2, \dots, 10$$
(8)

The error status range is shown in the table 1.

Table 1: The age range division of the elderly

Status	E_1	E_2	E_3	
Residual interval	[-469, -221]	(-221, 221]	(221, 469]	

According to the error interval range, the predicted number of elderly people in 2009-2018 is classified into the error interval as shown in the table 2.

From this, the initial state probability vector t_0 is obtained, and the transfer matrix P is:

Team # 201906177 page 6 of 15

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Table 7.	-1 h_{Δ} a_{Δ}	rango	division	\cap t	tho	Alderiv
Table 2:	THE age	range	di visioni	OI	ULIC	CIUCITY

year	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018
Residual interval	E_2	E_2	E_1	E_2	E_3	E_2	E_1	E_1	E_2	E_2

$$t_0' = [3/10, 3/5, 1/10]$$

$$P' = \begin{pmatrix} 1/3 & 2/3 & 0 \\ 1/4 & 5/8 & 1/8 \\ 0 & 1 & 0 \end{pmatrix} \tag{9}$$

The predicted solution obtained by gray prediction and Markov correction is shown in the figure $\,1$.

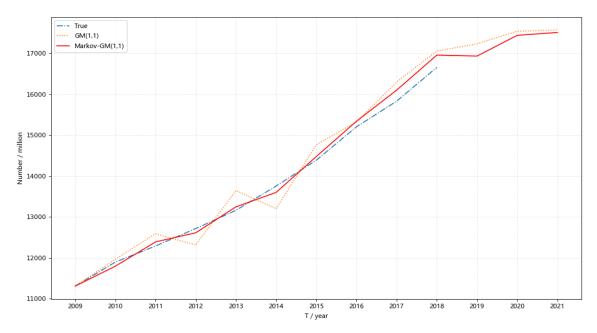


Figure 1: Comparison curve of prediction value of the number of the elderly

Similarly, the calculation of the medical demand forecast value for 2009-2018 is obtained as follows:

$$\widehat{X}(k+1) = 258.7846e^{-0.043809k} - 246.9258, k = 1, 2, \dots, 10$$
(10)

The error status range is shown in the table 3.

The medical demand forecast is classified into the error interval as shown in the table 4.

Team # 201906177 page7 of 15

Table 3: Medical demand status interval division

Q :	E_1	E_2	E_3
Residual interval	[-164.45, -58.74]	(-58.74, 58.74]	(58.74, 164.45]

Table 4: Medical demand error status interval

year	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018
Residual interval	E_2	E_3	E_1	E_2	E_3	E_1	E_1	E_3	E_2	E_2

From this, the initial state probability vector t_0 is obtained, and the transfer matrix P is:

$$t_0' = [3/10, 2/5, 3/10]$$

$$P' = \begin{pmatrix} 0 & 1/2 & 1/2 \\ 1/8 & 3/4 & 1/8 \\ 1/2 & 1/2 & 0 \end{pmatrix}$$
 (11)

The predicted solution obtained by gray prediction and Markov correction is shown in the figure $\,2$.

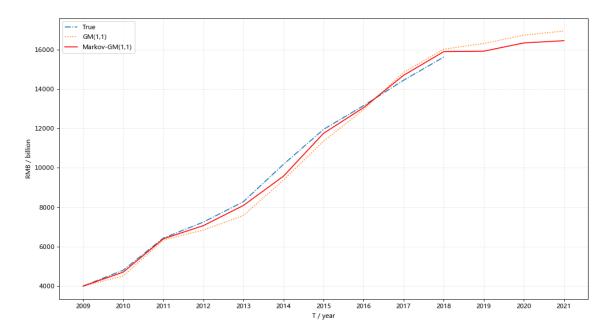


Figure 2: Comparison curve of medical demand forecast

Team # 201906177 page8 of 15

4.1.3 Conclusion

According to the direct comparison of the prediction solution curves in Figure 1 and figure 2, the predicted value corrected by Markov model has higher fitting degree and consistent volatility compared with the traditional gray prediction value, and can reflect the actual value fluctuation better than the traditional gray model prediction value. The prediction indexes of the two models are shown in table 5:

Table 5: Test of prediction results

Test parameters	RMSE	MAPE	NSE
GM(1,1) for elderly people	3040.04	0.0213	0.9455
Markov-GM(1,1) for elderly people	1238.64	0.0095	0.9900
GM(1,1) for medical demand	265.88	0.0628	0.8178
Markov-GM(1,1) for medical demand	101.13	0.0273	0.9736

From the above prediction results, it can be concluded that the RMSE of the number of patients and the number of deaths calculated by using the modified grey Markov model is smaller than that of the traditional grey model, which shows that the modified results are more reliable. The MPAE value of the modified model is closer to 0and the NSE value is closer to 1compared with the traditional model, which shows that the improved gray Markov model has a higher fitting degree and better prediction effect, which is suitable for the short-term prediction of the number of infectious diseases and deaths.

4.2 The model of Problem 2

4.2.1 Establishment of model

According to the different data of each year, we modified the grey markov model of the first question.

$$\begin{cases}
\overline{x}(k) = \widehat{x}(k) - \eta \\
\widehat{X}(k+1) = [X^{(0)}(1) - \frac{u}{a}]e^{-ak} + \frac{u}{a}, k = 1, 2, \dots, 13 \\
\eta = \begin{bmatrix} p_{E1} & p_{E2} & p_{E3} \end{bmatrix} \cdot \begin{bmatrix} \overline{E}_1 & \overline{E}_2 & \overline{E}_3 \end{bmatrix}^T
\end{cases} (12)$$

The revised predicted number of patients in year k was $\overline{x}(k)$, $\widehat{x}(k)$ is the traditional predicted value of GM(1,1), η is the expected error of GM in year k.

4.2.2 Calculation of predictors

We set X_i as the incidence data of 13 diseases from 2009 to 2021 in hubei province, $X_i = [x_{i1}, x_{i2}, x_{i3}, x_{i4}, x_{i5}](i = 1, 2, \dots, 13)$, The prediction results are obtained by

Team # 201906177 page9 of 15

using markov model. Similarly, Put the death toll data $X'_i = [x'_{i1}, x'_{i2}, x'_{i3}, x'_{i4}, x'_{i5}](i = 1, 2, \dots, 13)$ into the forecasting results $X'_i = [x'_{i1}, x'_{i2}, x'_{i3}, x'_{i4}, x'_{i5}, x'_{i6}](i = 1, 2, \dots, 13)$.

According to the prediction, the growth rate of the number of cases, the growth rate of the number of deaths and the mortality rate of the sick population in 2019 are respectively:

$$\begin{cases}
\delta_{i} = \frac{x_{i6} - x_{i5}}{x_{i5}} \times 100\% \\
\delta'_{i} = \frac{x'_{i6} - x'_{i5}}{x'_{i5}} \times 100\% \\
\eta_{i} = \frac{x'_{i6}}{x'_{i6}} \times 100\%
\end{cases}$$
(13)

Get the decision attribute vector of each group:

$$d_i = [x_{i6}, x'_{i6}, \delta_i, \delta'_i, \eta_i]$$

Similarly, the number of morbidity and mortality of various diseases in Hubei province were brought into the model to obtain the decision attribute vectors of various diseases $d'_i (i = 1, 2, \dots, 13)$.

4.2.3 TOPSIS

Let the disease multi-attribute decision matrix $A = (a_{ij})_{13\times 5}$ be expressed as:

$$A = [d_1^T, d_2^T, \cdot, , d_{13}^T]^T$$

Normalize A to obtain normalized decision matrix $B = (b_{ij})_{13 \times 5}$, where:

$$b_{ij} = a_{ij} / \sqrt{\sum_{i=1}^{13} a_{ij}^2}, i = 1, 2, \dots, 13; j = 1, 2, \dots, 5$$

It is assumed that regions with high growth rates of the number of patients and deaths need to focus on prevention and control, construct weight vectors:

$$W = [0.15, 0.3, 0.15, 0.3, 0.1] \tag{14}$$

The weighted canonical matrix, positive ideal solution, negative ideal solutioncan be obtained as follows: $C = (c_{ij})_{13\times 5}$, $C^* = [c_1^*, c_2^*, c_3^*, c_4^*, c_5^*]$, $C^0 = [c_1^0, c_2^0, c_3^0, c_4^0, c_5^0]$, where in:

Team # 201906177 page10 of 15

$$\begin{cases} c_{ij} = w_j \cdot b_{ij}, i = 1, 2, \dots, 13; j = 1, 2, \dots, 5 \\ c_j^* = \max_i(c_{ij}), j = 1, 2, \dots, 5 \\ c_j^0 = \min_i(c_{ij}), j = 1, 2, \dots, 5 \end{cases}$$

Calculating the distance from each disease attribute decision vector to the positive and negative ideal solution. The distance from d_i to the positive ideal solution and from d_i to the negative ideal solution is:

$$\begin{cases} s_j^* = \sqrt{\sum_{j=1}^n (c_{ij} - c_j^*)^2}, i = 1, 2, \dots, 13 \\ s_j^0 = \sqrt{\sum_{j=1}^n (c_{ij} - c_j^0)^2}, i = 1, 2, \dots, 13 \end{cases}$$

Calculating the comprehensive evaluation index of each program:

$$f_i^* = s_i^0 / (s_i^0 + s_i^*), i = 1, 2, \cdots, 13$$
 (15)

Obtain the order of key prevention and control diseases according to f_i^* (range from large to small). Similarly, the decision vector $d_i'(i=1,2,\cdots,13)$ of each disease can be brought into TOPSIS model to obtain the priority of disease prevention and control

4.2.4 Results and Conclusion

The number of cases and deaths of each occupation were put into the grayscale markov model to obtain the predicted values, as shown in table 6.

disease/10*thousand	2009	2010	• • •	2019	2020	2021
Immunodeficiency	1.5686	1.5021		1.3377	1.2777	1.2673
Endocrine disease	20.3322	18.129		20.3322	19.2462	18.6414
Nervous system	6.8927	5.8433		8.6325	8.9582	7.8506
Heart disease	128.8231	129.1872		149.45	153.454	155.6778
infectious disease	7.9431	7.421		5.437	4.824	4.534

Table 6: Predicted results of patients with various diseases

Calculate the positive ideal solution and the negative ideal solution as:

$$C^0 = [0.0066, 0.0048, 0.0653, 0.0261, 0.0331] \\ C^* = [-0.1856, -0.1847, -0.0809, -0.1163, -0.0929]$$

That is, the comprehensive evaluation index of the disease of 13 is shown in the figure 3:

Team # 201906177 page11 of 15

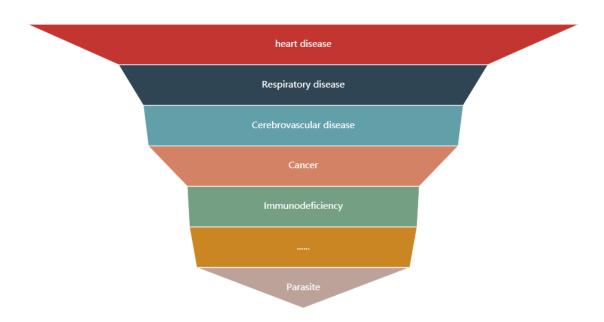


Figure 3: TOPSIS scores for different diseases

4.3 The model of Problem 3

4.3.1 Establishment of model

 $M/M/c/\infty$ model As the theory of $M/M/c/\infty$ illusteate:

$$\begin{cases}
P_0 = \left[\sum_{k=0}^{-1} \frac{1}{k!} \left(\frac{\lambda}{\mu} \right)^k + \frac{1}{c!} \cdot \frac{1}{1-\rho} \cdot \left(\frac{\lambda}{\mu} \right)^c \right]^{-1} \\
P_n = \left\{ \frac{1}{n!} \left(\frac{\lambda}{\mu} \right)^n P_0 \quad (n \leq c) \\
\frac{1}{c!c^{n-c}} \left(\frac{\lambda}{\mu} \right)^n P_0 \quad (n > c)
\end{cases}
\end{cases}$$
(16)

In the above expression, n is the amount of patient p_n is the probability of number of patient reach n in the moment t. C represents the amount of doctors in an outpatient department. λ means the average arrival rate of patients. And the μ means the average inspection rate of the doctor.

Based on this theory, the following relation is set up:

$$\begin{cases}
L_s = L_q + \frac{\lambda}{\mu} \\
L_q = \sum_{n=c+1}^{\infty} (n-c) P_n = \frac{(c_{\rho})^c \rho}{c!(1-\rho)^2} P_0
\end{cases}$$
(17)

In the above expression, L_s is the average length of the queuing which means the number of patient waiting in the system. Depending on it, we could derive the

Team # 201906177 page12 of 15

expression of average waiting time W_q and average time of stay W_s :

$$\begin{cases}
W_q = \frac{L_q}{\lambda} \\
W_s = \frac{L_s}{\lambda}
\end{cases}$$
(18)

4.3.2 Solution of model

Optimized systems design For $M/M/c/\infty$ system, the expection of the social cost per hour in the steady state is set up as Z. And Z could be calculated as the following expression:

$$z = c_s \cdot c + c_w \cdot L_s \tag{19}$$

In this expression, C is the number of doctors in the outpatient department. C(s) represents the average hourly wage of the doctors while C(w) represents the patient's. L_s is the amount of patient waiting in the system witch is function of C. Thus Z is the function of Z. To get the optimal solution of Z which make Z the minimum, we adopt the marginal analysis to solve it. And accroding to the feature that Z is the minimum, the following relation exists:

$$\begin{cases}
Z(c^*) \leqslant Z(c^* - 1) \\
Z(c^*) \leqslant Z(c^* + 1)
\end{cases}$$
(20)

Take expression (15) into expression (16) to gain:

$$L(C^*) - L(C^* + 1) \leqslant \frac{C(s)}{C(w)} \leqslant L(C^* - 1) - L(C^*)$$
 (21)

Thus, we utilize the ergodic algorithm to obtain the value of C^* .

4.4 The model of Problem 4

4.5 A letter to the medical department

Dear Medical leaders:

According to our modeling research, the aging trend in China is increasingly strengthened, and the majority of people's medical needs are increasingly high. It is estimated that the aging population over 65 will reach 170 million in 2021, which means that China will enter the aging society. According to the data, China's aging is on the rise, and meeting the medical and old-age needs of the elderly will be a huge social problem. Therefore, we should take measures as soon as possible in the field of gerontology scientific research, clinical medicine, rehabilitation nursing and public health policy, health management to actively carry out the diagnosis and treatment

Team # 201906177 page13 of 15

of the elderly related diseases difficult critical illness, demonstration and promotion of appropriate and effective high-level diagnosis and treatment technology; We will carry out teaching and training of high-level geriatric medical personnel, and train backbone clinical technicians and academic leaders. Undertake national geriatric medicine clinical translational research, in view of the elderly health has a major impact on disease organizations to carry out the relevant scientific research, in a timely manner to translate into clinical application and scientific research achievements at home and abroad for the next "five-year plan", and establish a medical, nursing, scientific research, teaching, prevention, management and policy making of the "seven" function of the major disease prevention and health management at the core of the organization.

Strengthening cooperation between public and private hospitals is the focus of improving medical efficiency. In order to alleviate the "three difficulties" of patients in public hospitals, such as difficulty in seeing a doctor, difficulty in hospitalization and difficulty in operation, public hospitals and private hospitals can cooperate and learn from each other. The cooperation between public hospitals and private hospitals includes public hospitals exporting management and technology to private hospitals, public hospitals borrowing beds from private hospitals, public hospitals hosting private hospitals, private hospitals or private capital participating in public hospitals. The cooperative hospital carries out standardized management and operation according to the standards of public hospitals to provide medical services for ordinary patients. At the same time, public hospitals' technical advantages, talent advantages and management advantages are utilized to enhance the popularity and credibility of private hospitals, improve the management and technical level of private hospitals, and create a win-win situation for public hospitals, private hospitals, patients and the society. It is suggested to set up a hospital management group with large public hospitals as the leading role to promote the development of private hospitals or small hospitals and at the same time make rational use of resources.

Finally, according to the model in question 2, we can predict the key disease prevention of each province in the next few years, and the corresponding province can take emergency measures on the medical problems that should be solved most, strengthen the prevention and treatment of related diseases, establish an appropriate medical insurance system, and the corresponding hospital should also make preparations in advance. I believe that with the hard work of all medical staff, China's medical environment will be better and better.

This is for your reference only.

Team # 201906177 page14 of 15

5 Sensitivity Analysis

6 Strengths and Weaknesses

6.1 Strengths

- 1. Vibration of bat is taken into account so that the accuracy of the model can be fairly good.
- 2. Physical explanation is put forward besides the model for a better understanding of the collision process.
- 3. Figures are used for explanation of the problem, thus making it more intuitive and easier to understand.

6.2 Weaknesses

- 1. The ball is actually nonlinear when deformation of the ball go beyond a certain limit. The approximation of linear model turned to be flawed when the force applied on the ball become very large.
- 2. Effective coefficient of restitution can not be calculated accurately. This affect the accuracy of the result of the model.

7 Conclusion

Team # 201906177 page15 of 15

References

[1] Saad Ahmed Javed, Sifeng Liu. Correction to: Predicting the research output/growth of selected countries: application of Even GM (1, 1) and NDGM models[J]. Scientometrics, 2019, 120(3).

- [2] ???,???,??????????????[J].?????,2018(15):74-75.
- [3] Yawen Wang, Zhongzhou Shen, Yu Jiang. Analyzing maternal mortality rate in rural China by Grey-Markov model[J]. Medicine, 2019, 98(6).
- [4] Saad Ahmed Javed, Sifeng Liu. Correction to: Predicting the research output/growth of selected countries: application of Even GM (1, 1) and NDGM models[J]. Scientometrics, 2019, 120(3).
- [5] ??,???,??????GM(1,N)-Markov??????[J].?????,2019(03):43-48.
- [6] ???,???,???,???GM(1,1)???????GM(1,1)?????????[J].??????,2011,45(09):1075-1079.
- [7] Kate Childs, Christopher Davis, Mary Cannon, Sarah Montague, Ana Filipe, Lily Tong, Peter Simmonds, Donald Smith, Emma C. Thomson, Geoff Dusheiko, Kosh Agarwal. Suboptimal SVR rates in African patients with atypical Genotype 1 subtypes: implications for global elimination of Hepatitis C[J]. Journal of Hepatology, 2019.
- [8] Yuyan Cao. Failure Prognosis for Electro-Mechanical Ac-Based Improved SMO-SVR tuators Method[A]. on ??????????????????????!EEE????????.Proceedings of 2016 IEEE Chinese Guidance, Navigation and Control Conference (IEEE CGNCC2016)[C].2016:6.