Cost of Capital Calculator

Overview and Assumptions

The Cost of Capital Calculator model produces estimates of the marginal effective tax rates on new investment under the baseline tax policy and user-specified tax reforms. These effective rate calculations take two forms. The marginal effective tax rate (METR) provides the tax wedge on new investment at the level of the business entity. The marginal effective total tax rate (METTR) includes individual level taxes in the measure of the tax wedge on new investment. One can think of the former as indicating the effect of taxes on incentives to invest from the perspective of the firm and the latter as representing effect of taxes on incentives to invest from the perspective of the saver.

As Fullerton (1999) notes, calculations of METRs depend on several assumptions. These include those relating to equilibrium in capital markets. discount rates, inflation rates, investor expectations, churning, how investments are financed, how risk is treated, and whether one believes the "old view" or "new view" of dividend taxes better represents investment incentives. Cost of Capital Calculator's equilibrium assumptions include the assumption that the marginal investment earns an after-tax rate of return equal to the market rate of return, returns across asset types are equalized, investors' risk-adjusted returns from debt and equity are equalized. Real discount rates and inflation rates are taken from the Congressional Budget Offices forecasts of nominal interest rates and inflation. Cost of Capital Calculator assumes no uncertainty in investment returns. We use historical data on the time equities are held and how investment is financed to inform effective tax rates on capital gains and financial policy decisions, respectively. Cost of Capital Calculator assumes the "old view" of dividend taxation in our calculations of the METTRs, implying that dividend taxes affect investment incentives.

The methodology to calculate METRs and METTRs follows closely Ozanne and Burnham (2006).

One should note that these METR and METTR calculations include only federal tax policy (current law or the user specified proposal) and therefore exclude the effects of state and local tax policy on investment incentives. Integrating such policies is a worthwhile project, but the results here are generally sufficient for comparing alternative federal tax proposals.

This guide is organized as follows. Section 1 and Section 2 describe how the cost of capital and effective tax rates are computed. Next, we describe how we measure fixed assets by asset type, industry, and tax treatment in Section 3. The methodology to allocate land and inventories across industry and tax treatment is described in Sections ?? and ??. Finally, we discuss how the values of the model parameters are determined in Section ??.

1 Marginal Effective Tax Rates

The marginal effective tax rate is calculated as the expected pre-tax rate of return on a marginal investment minus the real after-tax rate of return to the business entity, divided by the pre-tax rate of return on the marginal investment. That is:

$$METR_{i,m,j} = \frac{\rho_{i,m,j} - (r'_{m,j} - \pi)}{\rho_{i,m,j}},$$
(1.1)

where the subscripts i, m, and j refer to the type of asset, the production industry, and the tax entity type (e.g., C-corporation, partnership, S-corporation). The parameter $\rho_{i,m,j}$ is the pre-tax rate of return on the marginal investment, $r'_{m,j}$ is the business entity's nominal after-tax rate of return and π is the rate of inflation (so that $r_{m,j} - \pi$ is the real after-tax rate of return). It is assumed that the business entity discounts future cash flow by the rate $r_{m,j}$ (the prime in $r'_{m,j}$ differentiates the after-tax rate of return from the firm's discount rate). By definition, the marginal investment is the investment whose before tax return is equivalent to the cost of capital, $\rho_{i,m,j}$. The cost of capital is given by:

$$\rho_{i,m,j} = \frac{(r_{m,j} - \pi + \delta_i)}{1 - u_j} (1 - u_j z_i) + w_{i,m,j} - \delta_i, \tag{1.2}$$

where δ_i is the rate of economic depreciation, u_j is the statutory income tax rate at the first level of taxation (e.g., at the business entity level for C-corporations and at the individual level for pass-through business entities), z_i is the net present value of deprecation deductions from a dollar of new investment, and $w_{i,m,j}$ is the property tax rate.

We calculate the cost of capital, $\rho_{i,m,j}$, separately for each type of asset, production industry, and tax treatment (corporate or non-corporate). The after-tax rate of return is given by:

$$r'_{m,j} - \pi = f_{m,j} [i - \pi] + (1 - f_{m,j}) E_j, \tag{1.3}$$

where $f_{m,j}$ represents the fraction of the marginal investment financed with debt by firms in industry m and of tax entity type j.

At times users may be interested in the variation in METRs across asset types, in which case we can use the METR calculation outlined above. At other times users may wish to view the variation in METRs across industry. In this case, we compute a weighted average cost of capital for each production industry and tax treatment as follows:

$$\rho_{m,j} = \frac{\sum_{i=1}^{I} \widetilde{FA}_{i,m,j} \rho_{i,j}}{\sum_{i=1}^{I} \widetilde{FA}_{i,m,j}},$$

$$(1.4)$$

where the subscripts i, m, and j, refer to the asset type, production industry, and tax entity type. The calculation of the variable $\widetilde{FA}_{i,m,c}$ is discussed below.

With the cost of capital for all fixed assets in an industry-tax treatment grouping, we then compute the METR of the industry and tax treatment as:

$$METR_{m,j} = \frac{\rho_{m,j} - (r'_{m,j} - \pi)}{\rho_{m,j}},$$
(1.5)

2 Marginal Effective Total Tax Rates

METTRs include taxation at all levels, at the business entity and the individual to whom the returns from investment ultimately accrue. The METTR is computed as:

$$METTR = \frac{\rho_{i,m,j} - s_{m,j}}{\rho_{i,m,j}} \tag{2.1}$$

In equation above, $s_{m,j}$ is the overall after-tax return to savers from an investment in a business entity operating in production industry m and organized as a entity of type j. We compute this return as:

$$s_{m,j} = f_{m,j} s_{d,m,j} + (1 - f_{m,j}) s_{e,m,j}, (2.2)$$

where $f_{m,j}$ is the fraction of the investment that is financed with debt (and corresponds to the same fraction used in the calculation of the cost of capital noted above) and $s_{d,m,j}$ and $s_{e,m,j}$ are the after-tax returns to the saver from debt and equity, respectively. These in turn are found as:

$$s_{d,m,j} = \alpha_{d,ft,j} \times [i(1 - \tau_{int} - \pi)] + \alpha_{e,td,j} \times s_{d,td,j} + \alpha_{d,nt,j} \times (i - \pi)$$

$$(2.3)$$

Here, $\alpha_{d,ft,j}$, $\alpha_{d,td,j}$, and $\alpha_{d,nt,j}$ are the fraction of debt of entities of tax treatment j held in fully taxable, tax deferred, and non-taxable accounts. The variable $s_{d,td,j}$ are the after-tax returns of tax-deferred debt investors in entities of type j. The tax rate on interest income is τ_{int} and the nominal interest rate and inflation are given by i and π .

The return on tax deferred accounts is:

$$s_{d,td,j} = \frac{1}{Y_{td,j}} ln \left[(1 - \tau_{td,j}) e^{iY_{td,j}} + \tau_{td,j} \right] - \pi$$
(2.4)

The after-tax return on equity investments are given by:

$$s_{e,j} = \alpha_{e,ft,j} \times s_{e,ft,j} + \alpha_{e,td,j} \times s_{e,td,j} + \alpha_{e,nt,j} \times E_j \tag{2.5}$$

Here, $\alpha_{e,ft,j}$, $\alpha_{e,td,j}$, and $\alpha_{e,nt,j}$ are the fraction of equity held in fully taxable, tax deferred, and non-taxable accounts. The variables, $s_{e,ft,j}$ and $s_{e,td,j}$ are the after-tax returns of fully taxable and tax-deferred investors, respectively.

The return on fully taxable accounts is given by:

$$s_{e,ft,j} = (1 - m_j)E(1 - \tau_{div}) + g_j, \tag{2.6}$$

where m_j are the fraction of earnings that are retained by entity of type j, τ_{div} is the dividend tax rate on the marginal equity investor, and g_j is the real return paid on retained earnings after the capital gains tax on the marginal equity investor.

¹If one subscribes to the "new view", that dividend taxes do not affect investment incentives, then the first term in this equation would be zero. We use the subscript j by the parameters m and g, but note that these parameters only apply to business entities who can retain earnings (typically, these are those with an entity level tax).

The return on tax deferred accounts is:

$$s_{e,td,j} = \frac{1}{Y_{td,j}} ln \left[(1 - \tau_{td}) e^{(\pi + E_j)Y_{td,j}} + \tau_{td} \right] - \pi$$
 (2.7)

2.1 Computing After-Tax Capital Gains

Capital gains are not taxed until those gains are realized through the sale of stock. The ability to defer the tax liability from gains complicates the calculation of the after-tax gains that accrue to investors. Further complicating this calculation is that, under current law, short and long term gains are taxed at differential rates and the basis for capital gains is "stepped-up" on equity passed along to decedents upon death. Note, we'll omit the tax entity type subscript here since this calculation only applies to those entity types that can retain earnings, namely C-corporations under current tax law.

$$g = \omega_{scg} \times g_{scg} + \omega_{lcg} \times g_{lcg} + \omega_{xcg} \times mE, \tag{2.8}$$

wehre ω_{scg} , ω_{lcg} , and ω_{xcg} are the fractions of capital gains that are held for less than one year, more than one year but not until the owner's death, and those held until death, respectively. The variables g_{scg} and g_{lcg} are the after-tax, real, annualized returns to short and long term capital gains.

$$g_{scg} = \frac{1}{Y_{scg}} \times ln \left[(1 - \tau_{scg})e^{(\pi + mE)Y_{scg}} + \tau_{scg} \right] + \pi$$

$$(2.9)$$

and

$$g_{lcg} = \frac{1}{Y_{lcg}} \times ln \left[(1 - \tau_{lcg}) e^{(\pi + mE)Y_{lcg}} + \tau_{lcg} \right] + \pi$$
 (2.10)

3 Computing Fixed Assets by Industry and Entity Type

In the computation of $\rho_{m,j}$, we need to have a measure of fixed assets by industry and tax treatment for each asset type, $\widetilde{FA}_{i,m,j}$. To make this calculation, we work with two different sources of data. The first is the BEA's Detailed Data for Fixed Assets and Consumer Durable Goods. These data allow us to identify the stock of fixed assets by industry for each asset type. Call this variable $FA_{i,m}$. The second source of data we draw upon are the IRS Statistics of Income (SOI) data from business entity tax returns. From these data, we use information on depreciable assets and accumulated depreciation, aggregated by industry and tax entity type to compute a measure of the total stock of fixed assets by industry and tax treatment, $FA_{m,j}^{\tau}$. The superscript τ is used to denote that these asset values come from tax data. Measuring assets from tax returns is not ideal for two reason. First, there are reporting issues. These line items do not affect tax liability and so are often not reported with as much accuracy as items related to income. Relatedly, balance sheet reporting is often limited to businesses above a certain size. The second reason is that, for the previously cited and other reasons, measures of asset from tax returns may not line

up with BEA totals. We thus use the asset totals computed from tax returns only to help apportion the BEA asset totals across tax treatment. Namely, we compute the variable $\widehat{FA}_{i,m,j}$ as follows:

$$\widetilde{FA}_{i,m,j} = FA_{i,m} \times \frac{FA_{m,j}^{\tau}}{\sum_{j=1}^{J} FA_{m,j}^{\tau}}$$

$$(3.1)$$

This calculation makes the implicit assumption that the mix of asset types (i.e., the percent of total assets that each asset i comprises) is the same across different tax entities within an industry.

We define the set of tax entity types to be the following five entity types:

- 1. C-corporations
- 2. S-corporations
- 3. Corporate partners
- 4. Non-corporate partners
- 5. Sole proprietorships

Investments by C-corporations and corporate partners face the corporate income tax treatment and thus will be defined a "corporate". Investments by other entity types face the individual income tax and will thus be defined as "non-corporate".

3.1 Handling Varying Industry Specificity Between BEA and SOI Data

The BEA data in the detailed fixed asset tables are the only source of data on asset types by industry. The level of industry detail in the BEA data differs from that in the SOI data. To account for this, and to identify cost of capital as the finest levels of industry detail, we make the assumption that the mix of fixed assets remains the same across the children of any parent industry. The total amount of BEA assets by asset type can then be allocated across tax treatment and SOI minor industry using Equation 3.1.

3.2 SOI Data by Entity Type

We use IRS Statistics of Income (SOI) data on corporations, partnerships, and sole proprietorships. These data come with varying levels of specificity. Data on corporations are available at what the SOI call "minor industry" level. This encompass 196 industry classifications. Data on partnerships and sole proprietorships are generally available at the "major" industry level. These approximate the 3-digit NAICS codes and encompass 81 industry classifications. Data on S-corporations are available at the "sector" level, with 21 sector classifications. We note our methodologies below to attribute these data to the minor industry level for each entity type. Once data for each entity type is allocated across minor industry, we utilize cross-walks to related the SOI industry codes to BEA and NAICS codes, allowing one to group industries at varying levels of detail across different classification systems.

²Pages 2-6 of the Corporation Source Book outline these industry classifications.

3.2.1 C and S Corporation Data

Tax data on subchapter C corporations come from the data files for the *SOI Tax Stats - Corporation Source Book* for 2011. The link to those files is here. Specifically, we use the 2011sb1.csv and 2011sb3.csv files to find the aggregate amounts by industry for the following variables from Form 1120 and associated schedules: depreciable assets and accumulated depreciation. Note that the 2011sb1.csv file contains data from all Form 1120 returns (which includes both C and S corporations). Thus, in calculating aggregates for subchapter C corporations only, we net out the totals by industry and line item for S corporations using the 2011sb3.csv data.

Note that the level of industry detail in 2011sb1.csv and 2011sb3.csv differ, with the former reporting variables as fine as the 6-digit NAICS level and the latter reporting variables at the 2-digit level. In order to infer S corporation data at a finer level of industry detail, we make the assumption that the each variable is distributed across minor industries within a major industry in the same way for all corporations as it they are for S corporations. Letting x_{m1} be a variable of interest reported for all corporations in detailed industry m1 (e.g., these may correspond to a 6-digit NAICS code) from 2011sb1.csv and x_{m2} be the same variable reported for all corporations at the less detailed industry level (e.g., 2-digit NAICS). We thus assume that the variable x (which could be depreciable assets or accumulated depreciation) for S corporations can be allocated across detailed industry categories m1 as:

$$x_{m1,s} = \frac{x_{m1}}{x_{m2}} \times x_{m2,s},\tag{3.2}$$

where $m1 \in m2$. Variables allocated in this way are then used when differencing out data from 2011sb1.csv and 2011sb3.csv to find the amounts for C corporations.

Using these data, we calculate the stock of fixed assets for C corporations in industry m as reported on tax returns, $FA_{m,c}^{\tau}$, as the difference between the aggregate amounts of depreciable assets and accumulated depreciation for that industry. We then calculate the stock of fixed assets for S-corporations in industry m as reported on tax returns, $FA_{m,s}^{\tau}$, as the difference between the aggregate amounts of depreciable assets and accumulated depreciation for that industry for S-corporations.

3.2.2 Partnership Data

For partnerships, we draw upon the SOI Tax Stats - Partnership Statistics by Sector or Industry. There are three files we use to get measures of partnership assets in 2012. From the 12pa01.xls file, we pull aggregate depreciation deductions by industry. From 12pa03.xls, we collect aggregate values for depreciable assets and accumulated depreciation. Finally, we use 12pa05.xls to help us allocate the total partnership capital stock between corporate, individual, and tax exempt partners (we discuss this further below).

Using these data, we calculate the stock of fixed assets for partnerships in industry m as reported on tax returns, $FA_{m,p}^{\tau}$, as the difference between the aggregate amounts of depreciable assets and accumulated depreciation for that industry.

Allocating Partnership Capital Across Types of Partners: Partners in partnerships may be corporations, individuals, partnerships, tax-exempts, or other organizations. Because these partners face different tax treatment, we need to allocate shares of partnership assets to each of these entity types. We do this by using ratios of depreciable assets

to net income/loss by industry. We then use these ratios to distribute the share of total assets across partner type using the net income/loss going to partners of a given type in each industry. The assumption is that the ratio of assets to income/loss is the same across types of partners within a given industry. This certainly misses some of the variation in the ownership structure of partnership assets and in the distribution of partnership income, but is a method that allows us to attribute partnership assets across partner types.

File 12pa03.xls provides data on depreciable assets by industry. Denote these by $FA_{m,p}^{\tau}$. Using 12pa05.xls, we gather the aggregate amounts of net income or losses distributed to partners by partner type t and industry m2, Net Income(Loss) $_{m2,t}$. Net income and losses attributed to partners by type from the 12pa05.xls data do not total to the same values of net income and losses reported in 12pa03.xls because not all partnerships report their allocations. Therefore, we make an intermediate calculation to determine the share of all attributable gains/losses accrue to which types of partners. Note that the data from 12pa05.xls differ in the level of industry detail from the data in 12pa01.xls and 12pa03.xls. For notational clarity, let m1 be the more detailed classifications and m2 be the less detailed classifications. Using these two pieces of information together, we find the total amount of fixed assets by industry and partner type as:

$$FA_{m1,p,t}^{\tau} = \underbrace{\frac{abs(\text{Net Income})_{m2,t}}{\sum_{t} abs(\text{Net Income}_{m2,t})}}_{\text{From 12pa05.xls}} \times \underbrace{FA_{m1,p}^{\tau}}_{\text{From 12pa03.xls}},$$
(3.3)

where $m1 \in m2$ and t denotes partner type (individual, corporate, partnership, tax-exempt, other). An implicit assumption here is that that share of net gains or losses attributed to each partner type is the same across each sub-industry within a major industry (i.e., the attribution across all $m_1 \in m_2$ is identical).

When allocating capital across tax treatment, we will attribute the capital owned by corporate partners to the corporate sector, we will exclude assets held by tax-exempts, and the remainder will be attributed to the non-corporate sector. One can also break out assets by entity type, rather than the more coarse, corporate/non-corporate groupings.

Finally, since partnership data do not identify depreciable assets for each minor industry, we use data from S-corporation assets at the minor industry level to attribute assets from the major industry reported in the partnership data to the corresponding minor industries that are its children. The attribution takes the form described in Equation 3.2. This imputation is only done for minor industries for which the partnership data do not report depreciable asset totals.

3.2.3 Sole Proprietorships

We divide sole proprietorships into two groups: non-farm sole proprietors, who file a Schedule C of Form 1040, and farm sole proprietorships, who file Schedule F of Form 1040.

Non-farm Sole Proprietorships: Our data for non-farm sole proprietorships come from the SOI Tax Stats - Non-farm Sole Proprietorship Statistics for 2011. Specifically, we use the file 11sp01br.xls. These data do not record the value of depreciable assets for sole proprietorships, but they do contain depreciation deductions for sole proprietors. Thus we impute the value of depreciable assets and land using the assumption that the ratio of depreciable assets to depreciation deductions is the same within a particular industry for

sole proprietorships and partnerships. Specifically, we find the stock of fixed assets for sole proprietors to be:

$$FA_{sp}^{\tau} = \frac{\text{Depreciable Assets}_{m,p}}{\text{Depreciation Deductions}_{m,p}} \times \text{Depreciation Deductions}_{m,sp}, \tag{3.4}$$

where m denotes industry and the subscripts p and sp represent partnership and sole proprietorship, respectively.

Farm Sole Proprietorships: The SOI do not provide detailed data on farm sole proprietors. Thus for these businesses, we use Table 67 of the 2012 Census of Agriculture (COA). The COA reports the values of land and structures (together) and the value of machinery and equipment. These values are reported separately by type of organization (e.g., sole proprietorship, partnership). To find the value of depreciable assets that is comparable to those for non-farm sole proprietors as reported in tax data, we must adjust these data so that we have a separate accounting of land and structures. We use tax data to help us to impute this decomposition.

Let R_{sp} be the value of land and structures held by sole proprietor farms in the COA and let Q_{sp} be the value of machinery and equipment held by sole proprietor farms in the COA. Let R_p and Q_p be the analogous values for farm partnerships in the COA. By an accounting identity, it must be the case that $R_i + Q_i = FA_i + LAND_i$ for entity of type $i \in sp, p$. We thus find the ratio of land to capital held by partnerships in the agriculture industry; $\frac{LAND_{ag,p}^{\tau}}{LAND_{ag,p}^{\tau} + FA_{ag,p}^{\tau}}$, where the subscript ag denotes the industry used is agriculture and the subscript p denotes partnership returns. Next, this ratio is multiplied by the value for land and structures, R_p , and machinery and equipment. Q_p for partnerships in the COA. The result is an imputation for the value of land held by farm partnerships:

$$LAND_{p} = \frac{LAND_{ag,p}^{\tau}}{LAND_{ag,p}^{\tau} + FA_{ag,p}^{\tau}} \times (R_{p} + Q_{p})$$
(3.5)

To then get an imputation for the value of land held by farm sole proprietorships, we assume that the distribution in the value of land per acre is the same for farm sole proprietorships as it is for farm partnerships. That is, $\frac{\text{LAND}_p}{A_p} = \frac{\text{LAND}_{sp}}{A_{sp}}$, where A_p and A_{sp} denote the acreage held by farm partnerships and farm sole proprietorships, as reported in the COA. We use this assumption to solve for $LAND_{sp}$, given our imputed value for $LAND_p$ and data on A_p and A_{sp} .

We solve for the imputed value of fixed assets held by farm sole proprietorships as:

$$FA_{sp} = R_{sp} + Q_{sp} - \text{LAND}_{sp} \tag{3.6}$$

We then add the values of FA_{sp} to the value for fixed assets that we found for non-farm sole proprietorships in the agriculture industry, $FA_{aq,sp}^{\tau}$.

Lastly, since sole proprietorship data do not allow us to directly identify depreciable assets for each minor industry, we use data from partnership assets at the minor industry level to attribute assets from the major industry as inferred from the sole proprietorship data to the corresponding minor industries that are its children. The attribution takes the form described in Equation 3.2. This imputation is only done for minor industries for which the sole proprietorship data do allow us to identify depreciable assets.

4 Parameterization

4.1 Nominal Discount Rates

The nominal discount rate, $r_{m,j}$, used by the business represents the cost of funds to the business. These funds may come from equity, either through retained earnings or new equity issues, or from debt. The cost of equity is given by E_j (and varies by tax treatment), the cost of debt is given by the nominal interest rate i (and is the same for all businesses). The variable E_j represents the expected real rate of return that investors can expect if they invest in any business of entity type j. In general, interest payment deductions may be deductible. In the case of deductibility, the cost of debt is $i(1 - u_j)$, where u_j is the statutory tax rate on business income at the first level. We assume that the cost of funds for the marginal investment is a weighted average of the cost of funds from these two sources, debt and equity. In particular:

$$r_{m,j} - \pi = f_{m,j} \left[i(1 - u_j) - \pi \right] + (1 - f_{m,j}) E_j, \tag{4.1}$$

where $f_{m,j}$ represents the fraction of the marginal investment financed with debt by firms in industry m and of tax entity type j. Changes to interest deductibility are reflected by changes in the cost of funds and thus the discount rate. Likewise, systems like an allowance for corporate equity will affect the cost of funds and the discount rate.

4.1.1 Measuring Debt by Industry and Tax Treatment

We measure total debt from the Financial Accounts of the United States. In particular, we use the following tables to capture debt, which we measure separately for corporate financial and nonfinancial businesss, noncorporate business, and household mortgage debt:

- B.100: Value of owner-occupied houses:
- L.103: Liabilities of nonfinancial corporations, by type of instrument;
- L.104: Liabilities of nonfinancial noncorporate business, by type of instrument;
- L.208: Total liabilities (financial corporations);
- L.223: Corporate equity outstanding, by sector (nonfinancial, financial);
- L.218: Home mortgages (households); and
- L.229: Proprietors equity in noncorporate business

To allocate debt across tax treatment, we use SOI Tax Stats Data. The Financial Account Data combine both S corporations and C corporations in the "corporation" definition. We thus use SOI data to identify the portion of debt and equity attributable to S corporations. Debt is assigned in proportion to interest deductions. Equity is assigned in proportion to the sum of capital stock, additional paid-in capital, and retained earnings minus treasury stock. The resulting S corporation amounts were subtracted from corporate totals (leaving the amount for C corporations) and added to noncorporate businesses. We do the same to allocate the noncorporate across sole proprietorships and partnerships. We

further allocate the amount of debt and equity attributable to corporate partnerships using a similar method.

Specifically, we make the following calculations:

Let $debt_{corp}$ be the total amount of nonfinancial corporate debt reported in the Financial Accounts of the Untied States Table L.103, variable FL104122005. We then allocate this total across S-corporations and C-corporations and industry m as follows:

$$debt_{m,c} = debt_{corp} \frac{INTRST_PD_{m,c}}{\sum_{S \in c,s} \sum_{m=1}^{M} INTRST_PD_{m,S}}$$

$$(4.2)$$

Note that we exclude finance from the industries above since we have their debt and equity separately.

$$debt_{m,s} = debt_{corp} \frac{INTRST_PD_{m,s}}{\sum_{S \in s,c} \sum_{m=1}^{M} INTRST_PD_{m,S}}$$

$$(4.3)$$

Similarly, for equity. Let $X = CAP_STCK + PD_CAP_SRPLS + RTND_ERNGS_APPR + COMP_RTND_ERNGS_UNAPPR - CST_TRSRY_STCK$ and $equity_{corp}$ be total non-financial corporate equity from the Financial Accounts of the United States Table L.223, series LM103164103. For C-corps, we have:

$$equity_{m,c} = equity_{corp} \frac{X_{m,c}}{\sum_{S \in c,s} \sum_{m=1}^{M} X_{m,S}}$$

$$(4.4)$$

And for S-corps:

$$equity_{m,s} = equity_{corp} \frac{X_{m,s}}{\sum_{S \in c,s} \sum_{m=1}^{M} X_{m,S}}$$

$$\tag{4.5}$$

For financial businesses, we use Table L.208, series FL794122005 for corporate debt and Table L.224 series LM793164105 for equity. Here we can split the financial business amount across subindustries in finance (to the extent the SOI data contain such detail) and between S corp and C corp. The methodology is the same as above, replacing the industry list with the list of finance subindustries and using the total equity and debt for financial businesses reported in the Financial Accounts.

For the corporate financial services industry, we use Table L.208 series FL794122005 for debt and Table L.223 series LM793164105 for equity.

Noncorporate, nonfinancial debt totals come from Table L.104, series FL114123005. For non-corporate debt, we can divide between partnerships and sole props by industry using

$$debt_{m,j} = debt_{noncorp} \frac{INTRST_PD_{m,j}}{\sum_{m=1}^{M} INTRST_PD_{m,j}}, \text{ where } j \in p, sp$$

$$(4.6)$$

Noncorporate equity total comes from Table L.229, series FL152090205. We can see partners' capital accounts for partnerships, but for sole props we don't have a good measure

of the equity of proprietors. We thus make the assumption that the equity of sole proprietors is distributed across industries in the same way that the equity of partnerships is.

$$equity_{m,p+sp} = equity_{noncorp} \frac{PCA_{m,p}}{sum_{m=1}^{M} PCA_{m,p}}$$

$$(4.7)$$

Where $PCA_{p,m}$ are the "partnership capital accounts" for partnerships in industry m. $equity_{m,p+sp}$ denotes the total amount of equity for partnerships and sole proprietorships in industry m. We then find total non-corp equity for industry m as $equity_{NC,m} = equity_{p+sp,m} + equity_{s,m}$.

We then calculate the fraction of investment financed with debt by industry m and entity type j as: $f_{m,j} = \frac{debt_{m,j}}{equity_{m,j} + debt_{m,j}}$. Due to the data limitations stemming from data on sole proprietors, we calculate the ratio for partnerships and sole proprietorships as being: $f_{m,p} = f_{m,sp} = \frac{debt_{m,p} + debt_{m,sp}}{equity_{m,p+sp}}$ The exception here are financial, noncorporate businesses (see issue above with debt for these businesses). Because of this limitation, we let $f_{finance,j} = f_{finance,s}, \forall j \in \{p, sp\}$ (i.e., we take the financial policy of S-corp financial businesses and apply it to all non-corporate financial businesses).

4.2 NPV of Depreciation Deductions

The net present value of depreciation deductions is solved for using the discount rate derived above. Specifically, we have:

$$z_{i} = \int_{0}^{Y} z_{i}(y)e^{-r_{m,j}y}dy, \tag{4.8}$$

where Y is the number of years the asset is depreciated over, y is time in years, $z_i(y)$ is the dollar value of deprecation deductions in year y per dollar invested in asset of type i, and e is the mathematical constant. The function $z_i(y)$ reflects tax policy regarding deprecation schedules.

Under straight-line depreciation, the remaining depreciable value of \$1\$ invested at any time y is given by:

$$V(y) = 1 - \frac{y}{Y},\tag{4.9}$$

The net present value of straight-line depreciation can thus be found as:

$$z_{sl} = \int_{Y}^{0} \frac{e^{-ry}}{Y} dy \tag{4.10}$$

which, when integrated, yields:

$$z_{sl} = \frac{e^{-rY}}{Yr} \tag{4.11}$$

where Y is the recovery period of the asset. With a declining balance method of deprecation, the remaining depreciable value of \$1 invested at any time y is given by:

$$V(y) = e^{-\beta y},\tag{4.12}$$

where β is the rate of decline in value. Under the declining balance method of depreciation, this rate determined by the rate of acceleration of the straight-line deprecation method for an asset with a recovery period of Y years. Letting b denote the degree of acceleration of straight-line depreciation, we have $\beta = \frac{b}{Y}$. For example, for a 200% declining balance method of an asset with a recovery period of 5 years, $\beta = \frac{2}{5} = 40\%$.

To determine when it is advantageous for a filer to switch from the declining balance method to the straight-line method, we must find the point at which the slope of the declining balance method falls below the slope of the straight-line method. It is at this point that the depreciation deductions from the straight line method exceed those of the declining balance method. The slope of the remaining depreciable value under the declining balance method is given by:

$$\sigma_{db} = \frac{dV}{dy} = -\beta e^{-\beta y} \tag{4.13}$$

The slope of the straight line function depends upon the depreciable basis remaining at the switch. Therefore, the slope of the depreciable basis for the straight line method is given by:

$$\sigma_{sl} = \frac{dV}{du} = \frac{e^{-\beta Y^*}}{Y^* - Y},\tag{4.14}$$

where Y^* is the optimal time to switch. We can thus solve for Y^* as the point in time at which the slope of the two functions are equal. The Y^* that solves this is given by:

$$Y^* = Y\left(1 - \frac{1}{b}\right) \tag{4.15}$$

We can now find the present value of depreciation deductions under a declining balance with switch to straight line depreciation method. To do this, we find the integrals over the two methods for their respective portions of the recovery life. We find the present value of deprecation deductions, z_{dbsl} , to be:

$$z_{dbsl} = \int_0^{Y^*} \beta e^{-(\beta+r)y} dy + \int_{Y^*}^{Y} \frac{e^{-\beta Y^*}}{Y^* - Y} e^{-ry} dy$$
 (4.16)

which, when integrated, yields:

$$z_{dbsl} = \frac{\beta}{\beta + r} \left[1 - e^{-(\beta + r)Y^*} \right] + \frac{e^{-\beta Y^*}}{(Y - Y^*)r} \left[e^{-rY^*} - e^{-rY} \right]$$
(4.17)

4.3 User Inputs

Users may enter tax policies and evaluate those policy changes' effects on the cost of capital and effective tax rates. In addition, users may specific changes in the underlying macroe-conomic assumptions. Table 1 summarizes these parameters that the user might adjust to evaluate a tax reform option of interest. We discuss these parameters and how they are computed or entered into the model below.

Parameter Description Source Vary by asset Vary by ind Vary by tax treat Inflation rate CBO/user input No No No Nominal interest rate CBO/user input No No No CBO/user input E_c Required real return No No N/A - only for corp on corporate equity Statutory business entity-User input No No Yes u_j level income tax Maybe Maybe Property tax rate User input Maybe $w_{i,m,j}$ Tax depreciation allowance User input Yes No No $z_i(y)$ Notation? Haircut to Interest Deduction User Input No No Maybe Notation? Allowance for Corporate Equity User Input No No Yes Dividend tax rate on marginal investor User Input No No Yes $\tau_{div,j}$ User Input Interest tax rate on marginal investor No No Yes $\tau_{int,j}$ User Input No No N/A - only for corp Short term capital τ_{scg} gains rate on marginal investor au_{lcg} Long term capital User Input No No N/A - only for corp gains rate on marginal investor Tax on deferred capital User Input No No Yes $\tau_{td,j}$

Table 1: User Defined Parameters

4.3.1 Economic Parameters

income for marginal investor

One may alter the macroeconomic assumptions regarding rates of interest and inflation.³

4.3.2 Tax Policy Parameters

Business Taxation: Users to adjust the statutory marginal tax rates at the entity level, tax depreciation schedules, allowances for deductibility of interest or equity, and property tax rates.

Individual Income Taxation: B-Tax has the ability to allow for changes in individual income tax rates on pass-through business income, interest, dividends, and capital gains. In addition, policies affecting the deductibility of property taxes or mortgage interest affect the after-tax costs of owner-occupied housing. To find the effect of such policy changes on the marginal investor, B-Tax interacts with OSPC's Tax-Calculator. Once the reform policies are specified, the Tax-Calculator computes the marginal tax rates on non-corporate business income, dividend income, interest income, capital gains income, and tax-deferred retirement account income. The rates we apply to the "marginal investor" in the model are then computed as:

• τ_{nc} = weighted average marginal tax rate on ordinary, non-corporate business income (weighted by amount of non-corp business income)

³The default values are the taken from the CBO baseline forecast.

- τ_{div} = weighted average marginal tax rate on dividend income (weighted by amount of dividend income received)
- τ_{int} = weighted average of marginal tax rate on interest income (weighted by amount of interest income received)
- τ_{scg} = weighted average of marginal tax rate on short term capital gains (weighted by amount of short term capital gains received)
- η_{cg} = weighted average of marginal tax rate on long term capital gains (weighted by amount of long term capital gains received)
- τ_{td} = weighted average of marginal tax rate on pension distributions (weighted by the amount of pension distributions)
- τ_h = weighted average marginal tax rate on mortgage interest and property taxes (weighted by amounts of these deductions)

References

Fullerton, Don, "Marginal effective tax rate," Technical Report, Urban Institute 1999.

Ozanne, Larry and Paul Burnham, "Computing Effective Tax Rates on Capital Income," Technical Report, Congressional Budget Office 2006.