```
In [1]:
          import matplotlib.pyplot as plt
          plt.style.use('seaborn')
In [2]:
         import pandas as pd
         PRIMARY = 'Category Name'
         SECONDARY = 'Order Region'
         df = pd.read_csv(
              'DataCoSupplyChainDataset.csv',
              usecols = [PRIMARY, SECONDARY],
              encoding = 'unicode_escape'
          ).apply(lambda col: col.str.strip())
         df.head()
            Category Name Order Region
Out[2]:
         0 Sporting Goods Southeast Asia
         Sporting Goods
                              South Asia
         2 Sporting Goods
                              South Asia
            Sporting Goods
                                Oceania
            Sporting Goods
                                Oceania
```

Check & remove null + duplicate values

```
In [3]:
         df.isnull().sum().sort_values(ascending=False)
        Category Name
Out[3]:
        Order Region
        dtype: int64
In [4]:
         df.drop_duplicates(inplace=True)
        <class 'pandas.core.frame.DataFrame'>
        Int64Index: 691 entries, 0 to 162002
        Data columns (total 2 columns):
         # Column
                        Non-Null Count Dtype
            Category Name 691 non-null
                                           object
         1 Order Region 691 non-null
                                           object
        dtypes: object(2)
        memory usage: 16.2+ KB
```

Convert DataFrame to Graphs

```
primary_col, secondary_col = df[PRIMARY], df[SECONDARY]
print(f'Number of {PRIMARY}:', primary_col.nunique())
print(f'Number of {SECONDARY}:', secondary_col.nunique())
print('Number of edges:', len(df))

Number of Category Name: 50
Number of Order Region: 23
Number of edges: 691
```

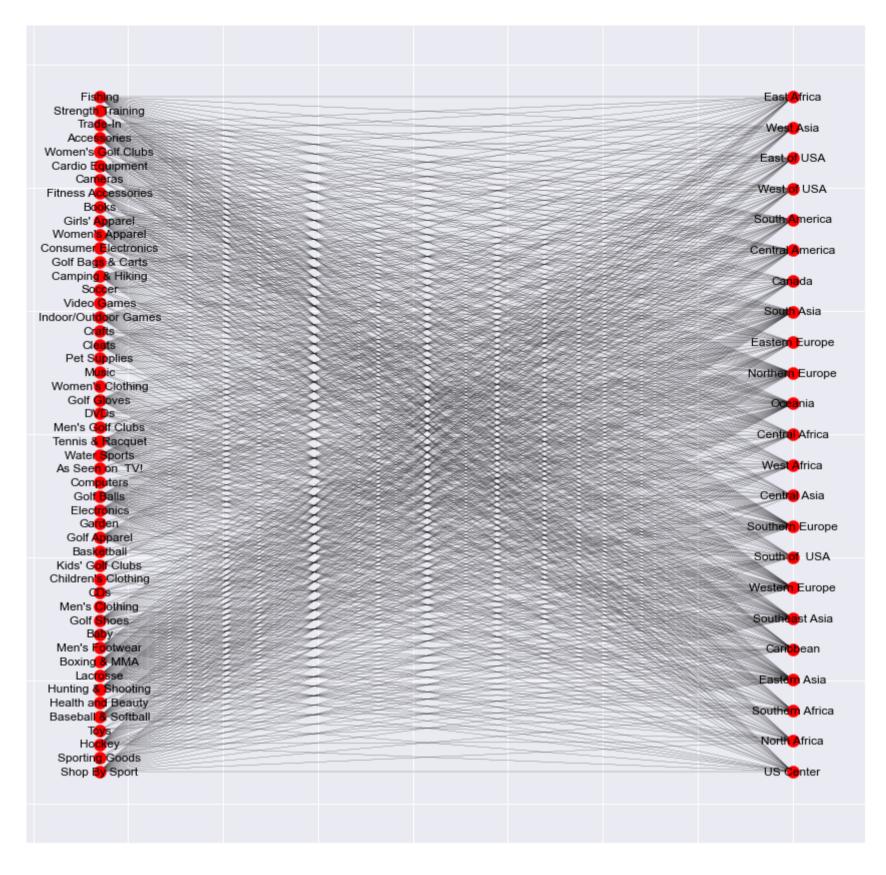
1. Bipartite Graph

```
import networkx as nx
from networkx.algorithms import bipartite

B = nx.Graph()
for index, row in df.iterrows():
        B.add_edge(row[PRIMARY], row[SECONDARY], weight=1)

B.add_nodes_from(primary_col, bipartite=0)
B.add_nodes_from(secondary_col, bipartite=1)

In [7]:
import matplotlib.pyplot as plt
plt.figure(figsize=(15, 15))
pos = nx.drawing.layout.bipartite_layout(B, primary_col)
nx.draw_networkx(B, pos=pos, node_size=150, width=0.2, node_color='red')
```

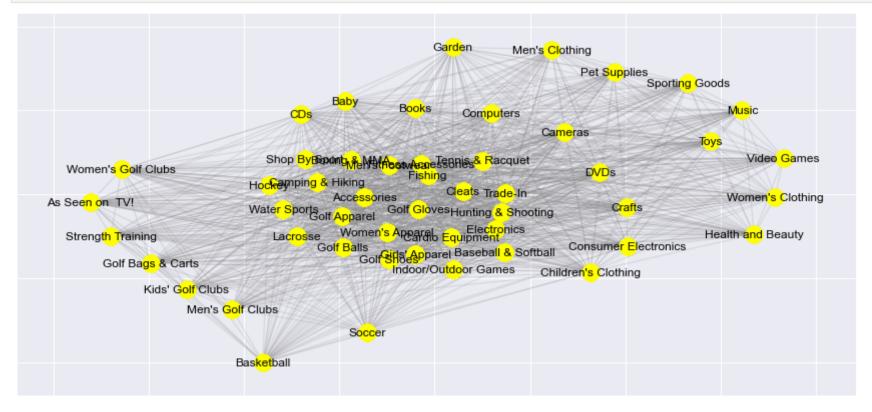


2. Weighted Projected Graph

```
In [8]: G = bipartite.weighted_projected_graph(B, primary_col)
    node_labels = dict(zip(primary_col, primary_col))

In [9]: plt.figure(figsize=(15, 7))
    pos = nx.spring_layout(G)

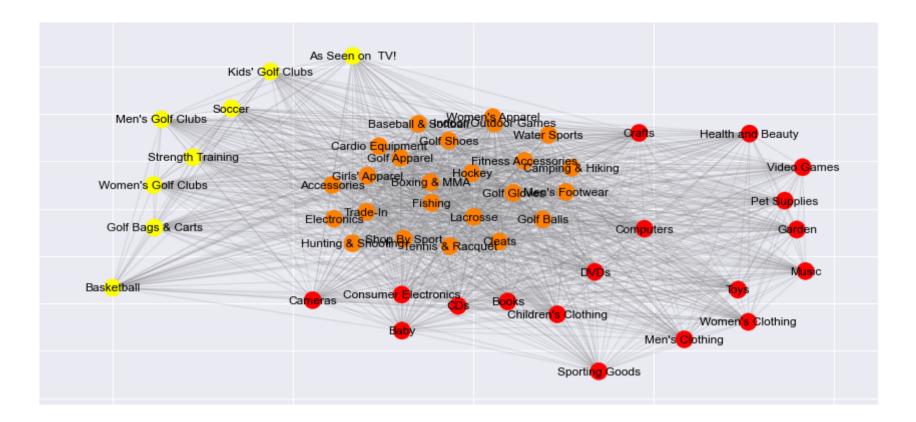
    nx.draw_networkx_nodes(G, pos, nodelist=primary_col, node_color='yellow')
    nx.draw_networkx_edges(G, pos, edge_color='grey', alpha=0.2)
    nx.draw_networkx_labels(G, pos, labels=node_labels)
    plt.show()
```



Community Detection

```
In [10]:
          df_groupby_category = df_groupby([SECONDARY])[PRIMARY]_apply(lambda x: sorted(set(x)))
          df_groupby_category = df_groupby_category.reset_index()
          # print(df_groupby_category.iloc[14][1])
          df_groupby_category.head()
Out[10]:
              Order Region
                                                     Category Name
         0
                            [Accessories, Baseball & Softball, Boxing & MM...
                   Canada
                 Caribbean
         1
                              [Accessories, As Seen on TV!, Baseball & Soft...
              Central Africa
                            [Accessories, Baseball & Softball, Boxing & MM...
          2
          3 Central America
                              [Accessories, As Seen on TV!, Baseball & Soft...
                Central Asia [Accessories, Boxing & MMA, Camping & Hiking, ...
In [11]:
          def get_cluster_common_values(cluster):
               commons = []
               for index, row in df_groupby_category.iterrows():
                   if set(cluster).issubset(row[PRIMARY]):
                       commons.append(row[SECONDARY])
               return commons
In [12]:
          def print_communities(node_groups):
               print('Number of communities:', len(node_groups))
               for index, cluster in enumerate(node_groups):
                   common_values = get_cluster_common_values(cluster)
                   print(f'\nCluster {index}:')
                   print(f"- {len(cluster)} Nodes: {', '.join(cluster)}")
                   print(f"- {len(common_values)} Common values: {', '.join(common_values)}")
In [13]:
          import matplotlib.cm as cm
          def plot_communities(nodes, labels):
               cmap = cm.get_cmap('autumn', max(labels) + 1)
               pos = nx.spring_layout(G)
               plt.figure(figsize=(15, 7))
               nx.draw_networkx_nodes(G, pos, nodes, cmap=cmap, node_color=labels)
               nx.draw_networkx_edges(G, pos, edge_color='grey', alpha=0.2)
               nx.draw_networkx_labels(G, pos)
               plt.show()
         1. Louvain Algorithm
In [14]:
          import community.community_louvain as community_louvain
          partition = community_louvain.best_partition(G)
          louvain_node_groups = [[] for _ in set(partition.values())]
          for node, cluster in sorted(partition.items()):
               louvain_node_groups[cluster].append(node)
In [15]:
          print_communities(louvain_node_groups)
          plot_communities(partition.keys(), list(partition.values()))
         Number of communities: 3
         Cluster 0:
          - 18 Nodes: Baby, Books, CDs, Cameras, Children's Clothing, Computers, Consumer Electronics, Crafts, DVDs, Garden, Health and Beau
          ty, Men's Clothing, Music, Pet Supplies, Sporting Goods, Toys, Video Games, Women's Clothing
          - 3 Common values: Oceania, South Asia, Southeast Asia
         Cluster 1:
          - 24 Nodes: Accessories, Baseball & Softball, Boxing & MMA, Camping & Hiking, Cardio Equipment, Cleats, Electronics, Fishing, Fitn
         ess Accessories, Girls' Apparel, Golf Apparel, Golf Balls, Golf Gloves, Golf Shoes, Hockey, Hunting & Shooting, Indoor/Outdoor Gam
         es, Lacrosse, Men's Footwear, Shop By Sport, Tennis & Racquet, Trade-In, Water Sports, Women's Apparel
          - 22 Common values: Canada, Caribbean, Central Africa, Central America, East Africa, East of USA, Eastern Asia, Eastern Europe, No
          rth Africa, Northern Europe, Oceania, South America, South Asia, South of USA, Southeast Asia, Southern Africa, Southern Europe,
         US Center, West Africa, West Asia, West of USA, Western Europe
         Cluster 2:
         - 8 Nodes: As Seen on TV!, Basketball, Golf Bags & Carts, Kids' Golf Clubs, Men's Golf Clubs, Soccer, Strength Training, Women's
         Golf Clubs
```

- 3 Common values: Northern Europe, Southern Europe, Western Europe



2. K-Means Algorithm

```
In [16]:
          from sklearn.cluster import KMeans
          from scipy.spatial.distance import cdist
          adj_matrix = nx.to_numpy_array(G)
          adj_matrix
         array([[ 0., 4., 4., ..., 4., 4., 4.],
                [ 4., 0., 23., ..., 4., 23., 23.],
                [ 4., 23., 0., ..., 4., 23., 23.],
                [4., 4., 4., ..., 0., 4., 4.],
                [ 4., 23., 23., ..., 4., 0., 23.],
                [ 4., 23., 23., ..., 4., 23., 0.]])
In [17]:
          import numpy as np
          distortions = []
          K = range(1, 8)
          for k in K:
              kmean_model = KMeans(n_clusters=k)
              kmean_model.fit(adj_matrix)
              dist = sum(np.min(cdist(adj_matrix, kmean_model.cluster_centers_, 'euclidean'), axis=1))
              distortions.append(dist / adj_matrix.shape[0])
In [18]:
          plt.figure(figsize=(10, 5))
          plt.plot(K, distortions, 'bs-')
          plt.xlabel('k')
          plt.ylabel('Distortion')
          plt.title('The Elbow Method showing the optimal k')
          plt.show()
                                      The Elbow Method showing the optimal k
           45
           40
           35
```

```
stortion
80
    20
    15
```

```
In [19]:
          kmeans = KMeans(n_clusters=2)
          kmeans.fit(adj_matrix)
          kmeans_node_groups = [[] for _ in range(kmeans.n_clusters)]
          for node, cluster in zip(G.nodes(), kmeans.labels_):
              kmeans node groups[cluster].append(node)
```

In [20]: print_communities(kmeans_node_groups)

```
plot_communities(G.nodes(), kmeans.labels_)
```

Number of communities: 2

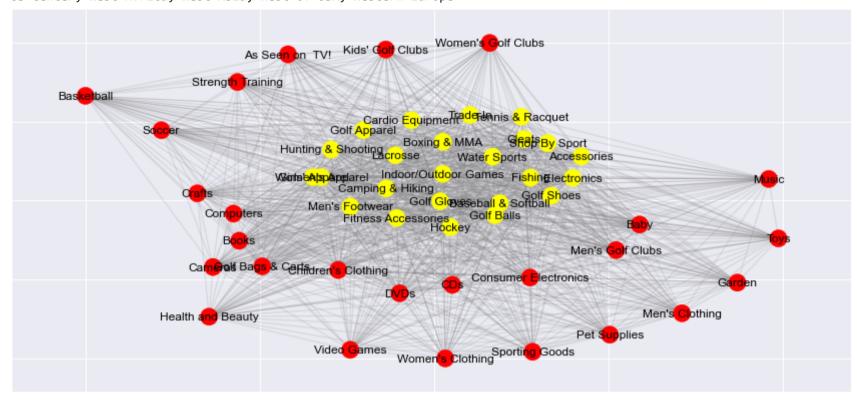
Cluster 0:

- 26 Nodes: Sporting Goods, Kids' Golf Clubs, Consumer Electronics, Cameras, Computers, Basketball, Soccer, Women's Clothing, Crafts, Men's Clothing, As Seen on TV!, Strength Training, Children's Clothing, Baby, Books, DVDs, CDs, Garden, Pet Supplies, Health and Beauty, Music, Video Games, Golf Bags & Carts, Women's Golf Clubs, Men's Golf Clubs, Toys

- 0 Common values:

Cluster 1:

- 24 Nodes: Cleats, Shop By Sport, Women's Apparel, Electronics, Boxing & MMA, Cardio Equipment, Trade-In, Hunting & Shooting, Bas eball & Softball, Men's Footwear, Camping & Hiking, Girls' Apparel, Accessories, Tennis & Racquet, Fitness Accessories, Golf Ball s, Lacrosse, Fishing, Hockey, Golf Gloves, Golf Shoes, Golf Apparel, Water Sports, Indoor/Outdoor Games
- 22 Common values: Canada, Caribbean, Central Africa, Central America, East Africa, East of USA, Eastern Asia, Eastern Europe, No rth Africa, Northern Europe, Oceania, South America, South Asia, South of USA, Southeast Asia, Southern Africa, Southern Europe, US Center, West Africa, West Asia, West of USA, Western Europe



3. Gaussian Mixture Model

```
from sklearn.mixture import GaussianMixture
    n_clusters = 3
    gmm = GaussianMixture(n_components=n_clusters)
    gmm.fit(adj_matrix)

labels = gmm.predict(adj_matrix)
    gmm_node_groups = [[] for _ in range(n_clusters)]
    for node, cluster in zip(G.nodes(), labels):
        gmm_node_groups[cluster].append(node)
```

In [33]:

print_communities(gmm_node_groups)
plot_communities(G.nodes(), labels)

Number of communities: 3

Cluster 0:

- 18 Nodes: Sporting Goods, Consumer Electronics, Cameras, Computers, Women's Clothing, Crafts, Men's Clothing, Children's Clothing, Baby, Books, DVDs, CDs, Garden, Pet Supplies, Health and Beauty, Music, Video Games, Toys

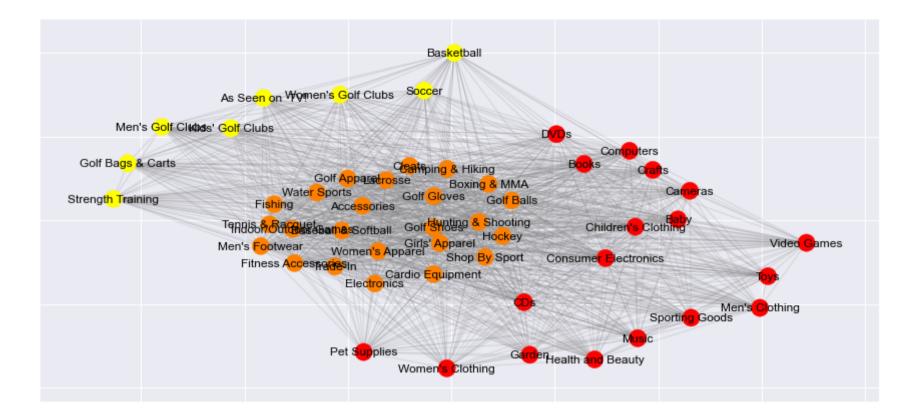
- 3 Common values: Oceania, South Asia, Southeast Asia

Cluster 1:

- 24 Nodes: Cleats, Shop By Sport, Women's Apparel, Electronics, Boxing & MMA, Cardio Equipment, Trade-In, Hunting & Shooting, Bas eball & Softball, Men's Footwear, Camping & Hiking, Girls' Apparel, Accessories, Tennis & Racquet, Fitness Accessories, Golf Ball s, Lacrosse, Fishing, Hockey, Golf Gloves, Golf Shoes, Golf Apparel, Water Sports, Indoor/Outdoor Games
- 22 Common values: Canada, Caribbean, Central Africa, Central America, East Africa, East of USA, Eastern Asia, Eastern Europe, No rth Africa, Northern Europe, Oceania, South America, South Asia, South of USA, Southeast Asia, Southern Africa, Southern Europe, US Center, West Africa, West Asia, West of USA, Western Europe

Cluster 2:

- 8 Nodes: Kids' Golf Clubs, Basketball, Soccer, As Seen on TV!, Strength Training, Golf Bags & Carts, Women's Golf Clubs, Men's Golf Clubs
- 3 Common values: Northern Europe, Southern Europe, Western Europe



Network Centrality

```
In [34]:
          def print_centrality(centrality, name):
              result = pd.DataFrame(centrality.items(), columns=['Category Name', name])
              result.sort_values(name, ascending=False, inplace=True)
              print(result.to_records(index=False).tolist())
              return result
In [35]:
          def plot_centrality(centrality):
              plt.figure(figsize=(15, 7))
              node_color = [centrality[i] for i in centrality.keys()]
              cmap = plt.cm.ScalarMappable(
                  cmap = 'Wistia',
                  norm = plt.Normalize(vmin=min(node_color), vmax=max(node_color))
              cmap.set_array([])
              plt.colorbar(cmap)
              pos = nx.spring_layout(G)
              nx.draw_networkx_nodes(G, pos, node_color=node_color, cmap='Wistia')
              nx.draw_networkx_edges(G, pos, edge_color='grey', alpha=0.2)
              plt.show()
```

Degree Centrality

```
In [36]: degree = dict(nx.degree(G))
plot_centrality(degree, 'Degree Centrality').head()

49
48
47
46
45
44
43
42
```

[('Indoor/Outdoor Games', 49), ('Golf Balls', 49), ('Golf Shoes', 49), ('Crafts', 49), ('Golf Gloves', 49), ('Tennis & Racquet', 4 9), ('Fitness Accessories', 49), ('Cleats', 49), ("Children's Clothing", 49), ('Golf Apparel', 49), ('Lacrosse', 49), ('Baby', 4 9), ('Fishing', 49), ('Books', 49), ('DVDs', 49), ('CDs', 49), ('Accessories', 49), ("Girls' Apparel", 49), ('Hockey', 49), ('Shop By Sport', 49), ('Computers', 49), ('Cameras', 49), ('Consumer Electronics', 49), ('Camping & Hiking', 49), ("Men's Footwear", 4 9), ('Baseball & Softball', 49), ('Hunting & Shooting', 49), ('Water Sports', 49), ('Trade-In', 49), ('Cardio Equipment', 49), ('Boxing & MMA', 49), ('Electronics', 49), ("Women's Apparel", 49), ('Music', 41), ('Health and Beauty', 41), ('Toys', 41), ('Video G

ames', 41), ('Sporting Goods', 41), ('Pet Supplies', 41), ('Garden', 41), ("Men's Clothing", 41), ("Women's Clothing", 41), ('Stre ngth Training', 40), ('Golf Bags & Carts', 40), ('Soccer', 40), ("Women's Golf Clubs", 40), ("Men's Golf Clubs", 40), ('Basketbal l', 40), ("Kids' Golf Clubs", 40), ('As Seen on TV!', 40)]

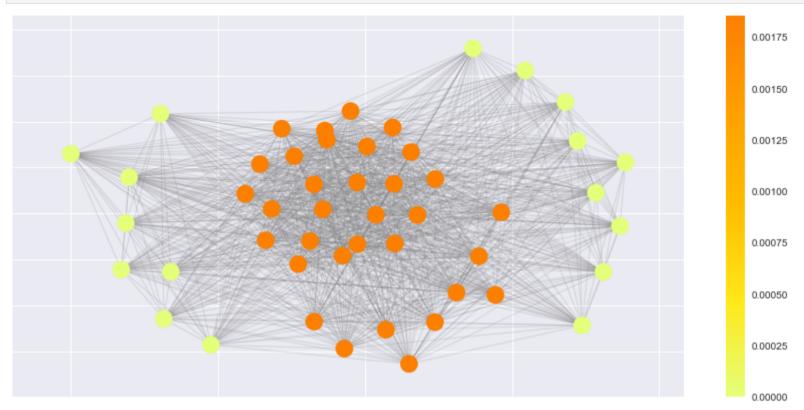
Out[36]:

	Category Name	Degree Centrality
49	Indoor/Outdoor Games	49
26	Golf Balls	49
43	Golf Shoes	49
21	Crafts	49
41	Golf Gloves	49

Betweenness Centrality

In [37]:

```
betweenness = nx.betweenness_centrality(G)
plot_centrality(betweenness)
print_centrality(betweenness, 'Betweenness Centrality').head()
```



[('Indoor/Outdoor Games', 0.0018552875695732828), ("Girls' Apparel", 0.0018552875695732828), ('Golf Apparel', 0.0018552875695732828), ('Tennis & Racquet', 0.0018552875695732828), ('Fitness Accessories', 0.0018552875695732828), ('Cleats', 0.0018552875695732828), ('Golf Balls', 0.0018552875695732828), ('Golf Shoes', 0.0018552875695732828), ("Children's Clothing", 0.0018552875695732828), ('Lacrosse', 0.0018552875695732828), ('Baby', 0.0018552875695732828), ('Fishing', 0.0018552875695732828), ('Books', 0.0018552875695732828), ('DVDs', 0.0018552875695732828), ('CDs', 0.0018552875695732828), ('Hockey', 0.0018552875695732828), ('Golf Gloves', 0.0018552875695732828), ('Colf Gloves', 0.0018552875695732828), ('Colf Gloves', 0.0018552875695732828), ('Computers', 0.0018552875695732828), ('Shop By Sport', 0.0018552875695732828), ('Women's Apparel', 0.0018552875695732828), ('Computers', 0.0018552875695732828), ('Cameras', 0.0018552875695732828), ('Consumer Electronics', 0.0018552875695732828), ('Camping & Hiking', 0.0018552875695732828), ("Men's Footwear", 0.0018552875695732828), ('Baseball & Softball', 0.0018552875695732828), ('Boxing & MMA', 0.0018552875695732828), ('Trade-In', 0.0018552875695732828), ('Cardio Equipment', 0.0018552875695732828), ('Boxing & MMA', 0.0018552875695732828), ('Golf Bags & Carts', 0.0), ('Music', 0.0), ('Women's Golf Clubs'', 0.0), ('Toys', 0.0), ('Men's Golf Clubs'', 0.0), ('Yet Supplies', 0.0), ('Garden', 0.0), ('Strength Training', 0.0), ('Sporting Goods', 0.0), ('Health and Beauty', 0.0), ('Basketball', 0.0), ('Kids' Golf Clubs'', 0.0), ('As Seen on TV!', 0.0)]

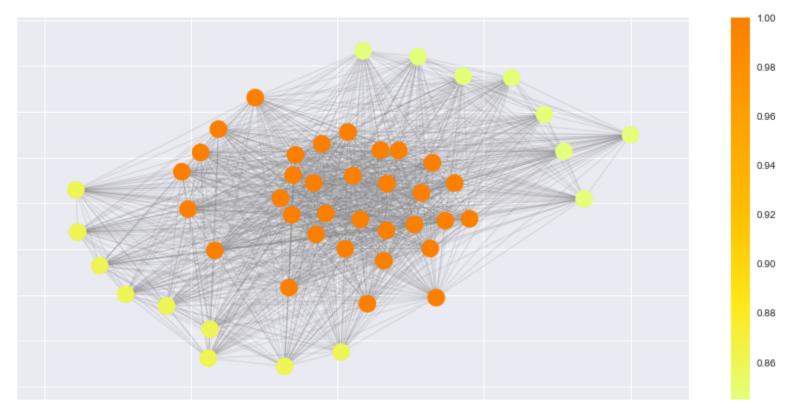
Out[37]:

	Category Name	Betweenness Centrality	
49	Indoor/Outdoor Games	0.001855	
18	Girls' Apparel	0.001855	
44	Golf Apparel	0.001855	
23	Tennis & Racquet	0.001855	
24	Fitness Accessories	0.001855	

Closeness Centrality

```
In [38]:
```

```
closeness = nx.closeness_centrality(G)
plot_centrality(closeness)
print_centrality(closeness, 'Closeness Centrality').head()
```



[('Indoor/Outdoor Games', 1.0), ('Golf Balls', 1.0), ('Golf Shoes', 1.0), ('Crafts', 1.0), ('Golf Gloves', 1.0), ('Tennis & Racque t', 1.0), ('Fitness Accessories', 1.0), ('Cleats', 1.0), ("Children's Clothing", 1.0), ('Golf Apparel', 1.0), ('Lacrosse', 1.0), ('Baby', 1.0), ('Fishing', 1.0), ('Books', 1.0), ('DVDs', 1.0), ('CDs', 1.0), ('Accessories', 1.0), ("Girls' Apparel", 1.0), ('Hockey', 1.0), ('Shop By Sport', 1.0), ('Computers', 1.0), ('Cameras', 1.0), ('Consumer Electronics', 1.0), ('Camping & Hiking', 1.0), ("Men's Footwear", 1.0), ('Baseball & Softball', 1.0), ('Hunting & Shooting', 1.0), ('Water Sports', 1.0), ('Trade-In', 1.0), ('Cardio Equipment', 1.0), ('Boxing & MMA', 1.0), ('Electronics', 1.0), ("Women's Apparel", 1.0), ('Music', 0.8596491228070176), ('Health and Beauty', 0.8596491228070176), ('Toys', 0.8596491228070176), ('Video Games', 0.8596491228070176), ('Sporting Goods', 0.8596491228070176), ('Pet Supplies', 0.8596491228070176), ('Garden', 0.8596491228070176), ("Men's Clothing", 0.8596491228070176), ('Strength Training', 0.8448275862068966), ('Golf Bags & Carts', 0.8448275862068966), ('Soccer', 0.8448275862068966), ("Women's Golf Clubs", 0.8448275862068966), ("Men's Golf Clubs", 0.8448275862068966)]

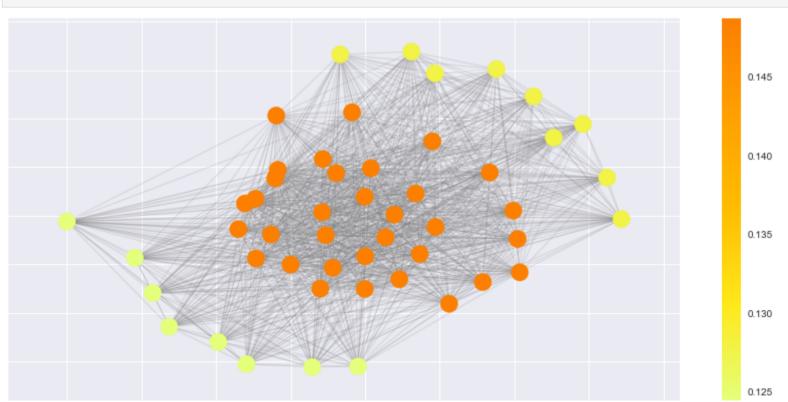
Out[38]:		Category Name	Closeness Centrality
	49	Indoor/Outdoor Games	1.0
	26	Golf Balls	1.0
	43	Golf Shoes	1.0
	21	Crafts	1.0

41

Eigenvector Centrality

Golf Gloves

eigenvector = nx.eigenvector_centrality(G)
plot_centrality(eigenvector)
print_centrality(eigenvector, 'Eigenvector Centrality').head()



[('Indoor/Outdoor Games', 0.14867064721396608), ("Children's Clothing", 0.14867064721396608), ('Crafts', 0.14867064721396608), ('Golf Gloves', 0.14867064721396608), ('Tennis & Racquet', 0.14867064721396608), ('Fitness Accessories', 0.14867064721396608), ('Cleats', 0.14867064721396608), ('Golf Balls', 0.14867064721396608), ('Lacrosse', 0.14867064721396608), ('Girls' Apparel", 0.14867064721396608), ('Baby', 0.14867064721396608), ('Fishing', 0.14867064721396608), ('Books', 0.14867064721396608), ('DVDs', 0.14867064721396608), ('CDs', 0.14867064721396608), ('Hockey', 0.14867064721396608), ('Golf Shoes', 0.14867064721396608), ('Accessories', 0.14867064721396608), ('Golf Apparel', 0.14867064721396608), ('Water Sports', 0.14867064721396608), ('Shop By Sport', 0.14867064721396608), ("Women's Apparel", 0.14867064721396608), ('Electronics', 0.14867064721396608), ('Boxing & MMA', 0.14867064721396608), ('Cardio Equipment', 0.14867064721396608), ('Trade-In', 0.14867064721396608), ('Hunting & Shooting', 0.14867064721396608), ('Baseball & Softball', 0.14867064721396608), ('Men's Footwear", 0.14867064721396608), ('Camping & Hiking', 0.14867064721396608), ('Consumer Electronics', 0.14867064721396608), ('Garden', 0.12767929833125463), ('Toys', 0.12767929833125463), ('Pet Supplies', 0.12767929833125463), ('Health and Beauty', 0.12767929833125463), ('Sporting Goods', 0.1276792983312546), ("Men's Clothing", 0.127679298

3312546), ("Women's Clothing", 0.1276792983312546), ('Strength Training', 0.12444087284685672), ('Golf Bags & Carts', 0.12444087284685672), ('Soccer', 0.12444087284685672), ("Women's Golf Clubs", 0.12444087284685672), ("Men's Golf Clubs", 0.12444087284685672), ('Basketball', 0.12444087284685672), ("Kids' Golf Clubs", 0.12444087284685672), ('As Seen on TV!', 0.12444087284685672)]

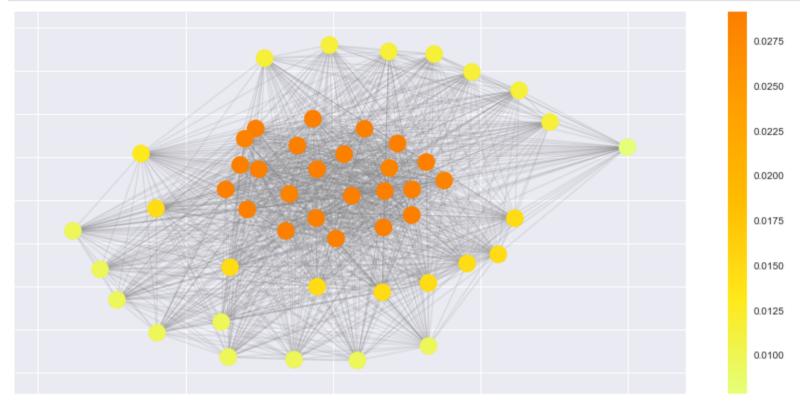
Out[39]: Category Name Eigenvector Centrality

49	Indoor/Outdoor Games	0.148671
28	Children's Clothing	0.148671
21	Crafts	0.148671
41	Golf Gloves	0.148671
23	Tennis & Racquet	0.148671

PageRank

In [40]:

pagerank = nx.pagerank(G)
plot_centrality(pagerank)
print_centrality(pagerank, 'PageRank').head()



[('Indoor/Outdoor Games', 0.02910004330793566), ("Men's Footwear", 0.02910004330793566), ('Fishing', 0.02910004330793566), ('Lacro sse', 0.02910004330793566), ('Golf Balls', 0.02910004330793566), ('Cleats', 0.02910004330793566), ('Tennis & Racquet', 0.029100043 30793566), ('Golf Apparel', 0.02910004330793566), ('Accessories', 0.02910004330793566), ('Camping & Hiking', 0.02910004330793566), ("Girls' Apparel", 0.02910004330793566), ('Cardio Equipment', 0.02910004330793566), ('Water Sports', 0.02910004330793566), ('Shop By Sport', 0.02910004330793566), ("Women's Apparel", 0.02910004330793566), ('Electronics', 0.02910004330793566), ('Boxing & MMA', 0.02910004330793566), ('Hunting & Shooting', 0.02910004330793566), ('Trade-In', 0.02910004330793566), ('Golf Gloves', 0.0291000433 0793566), ('Hockey', 0.028393028110741375), ('Golf Shoes', 0.028393028110741375), ('Fitness Accessories', 0.028393028110741375), ('Baseball & Softball', 0.028393028110741375), ('Crafts', 0.01460032971973412), ('Computers', 0.01460032971973412), ("Children's C lothing", 0.01460032971973412), ('Baby', 0.01460032971973412), ('Consumer Electronics', 0.01460032971973412), ('Books', 0.01460032 971973412), ('DVDs', 0.01460032971973412), ('CDs', 0.01460032971973412), ('Cameras', 0.012939485390217484), ("Women's Golf Clubs", 0.01134315515704318), ("Men's Golf Clubs", 0.01134315515704318), ('Golf Bags & Carts', 0.01134315515704318), ('As Seen on TV!', 0.01134315515704318), ('Strength Training', 0.01134315515704318), ('Soccer', 0.01134315515704318), ("Kids' Golf Clubs", 0.01134315 515704318), ('Pet Supplies', 0.009718050588254678), ('Health and Beauty', 0.009718050588254678), ('Music', 0.009718050588254678), ('Video Games', 0.009718050588254678), ('Garden', 0.009718050588254678), ("Men's Clothing", 0.009718050588254678), ("Women's Cloth ing", 0.009718050588254678), ('Toys', 0.009718050588254678), ('Sporting Goods', 0.009718050588254678), ('Basketball', 0.0078203568 56636094)]

Out[40]:

	Category Name	PageRank
49	Indoor/Outdoor Games	0.0291
11	Men's Footwear	0.0291
31	Fishing	0.0291
29	Lacrosse	0.0291
26	Golf Balls	0.0291