

```
In [1]: import matplotlib.pyplot as plt
plt.style.use('seaborn')
```

```
In [2]: import pandas as pd
PRIMARY = 'Category Name'
SECONDARY = 'Order Region'

df = pd.read_csv(
    'DataCoSupplyChainDataset.csv',
    usecols = [PRIMARY, SECONDARY],
    encoding = 'unicode_escape'
).apply(lambda col: col.str.strip())
df.head()
```

```
Out[2]:
```

	Category Name	Order Region
0	Sporting Goods	Southeast Asia
1	Sporting Goods	South Asia
2	Sporting Goods	South Asia
3	Sporting Goods	Oceania
4	Sporting Goods	Oceania

Check & remove null + duplicate values

```
In [3]: df.isnull().sum().sort_values(ascending=False)
```

```
Out[3]: Category Name    0
Order Region    0
dtype: int64
```

```
In [4]: df.drop_duplicates(inplace=True)
df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 691 entries, 0 to 162002
Data columns (total 2 columns):
#   Column          Non-Null Count  Dtype
---  ---
0   Category Name    691 non-null    object
1   Order Region     691 non-null    object
dtypes: object(2)
memory usage: 16.2+ KB
```

Convert DataFrame to Graphs

```
In [5]: primary_col, secondary_col = df[PRIMARY], df[SECONDARY]
print(f'Number of {PRIMARY}:', primary_col.nunique())
print(f'Number of {SECONDARY}:', secondary_col.nunique())
print('Number of edges:', len(df))
```

```
Number of Category Name: 50
Number of Order Region: 23
Number of edges: 691
```

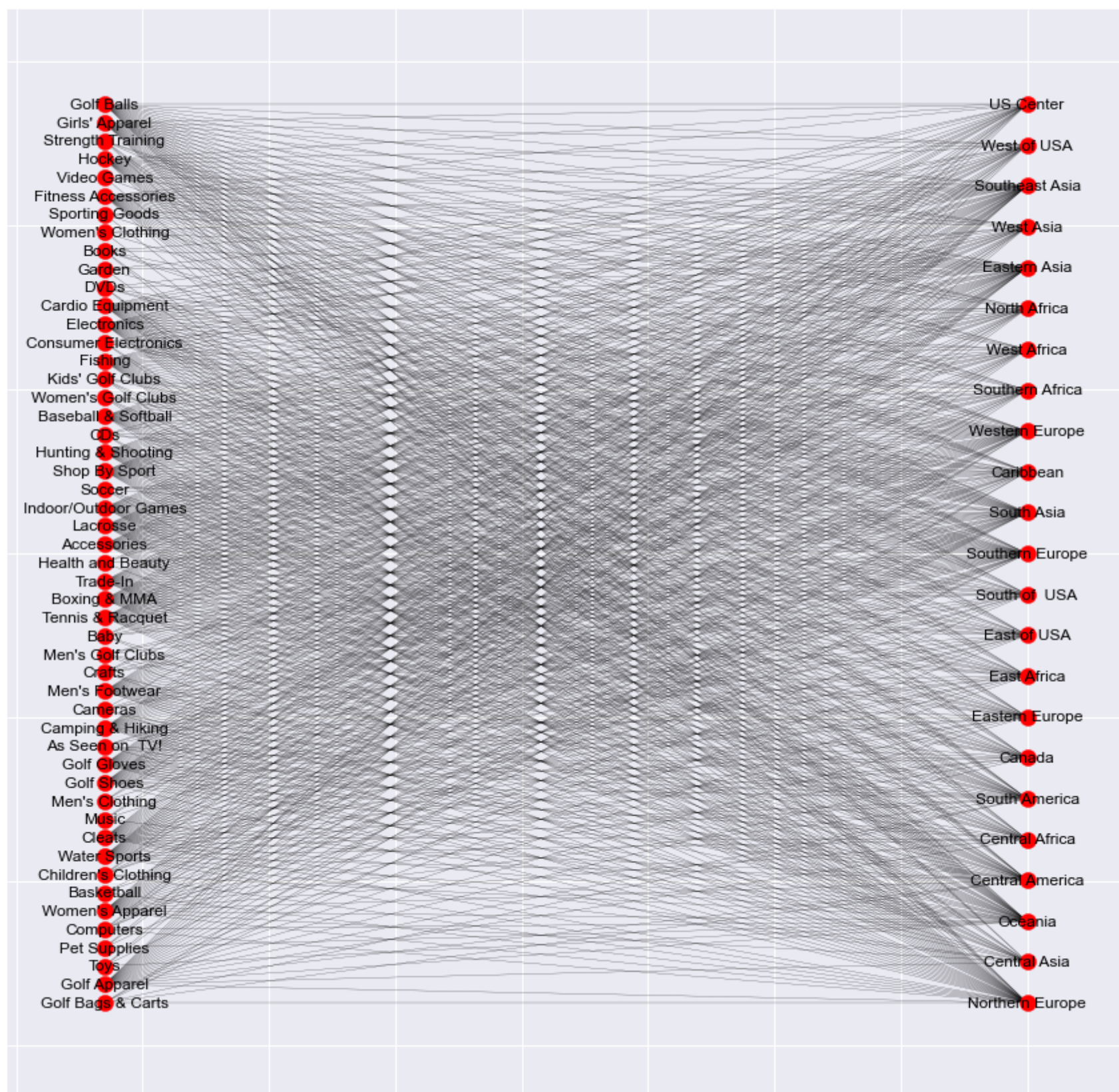
1. Bipartite Graph

```
In [6]: import networkx as nx
from networkx.algorithms import bipartite

B = nx.Graph()
for index, row in df.iterrows():
    B.add_edge(row[PRIMARY], row[SECONDARY], weight=1)

B.add_nodes_from(primary_col, bipartite=0)
B.add_nodes_from(secondary_col, bipartite=1)
```

```
In [7]: import matplotlib.pyplot as plt
plt.figure(figsize=(15, 15))
pos = nx.drawing.layout.bipartite_layout(B, primary_col)
nx.draw_networkx(B, pos=pos, node_size=150, width=0.2, node_color='red')
```

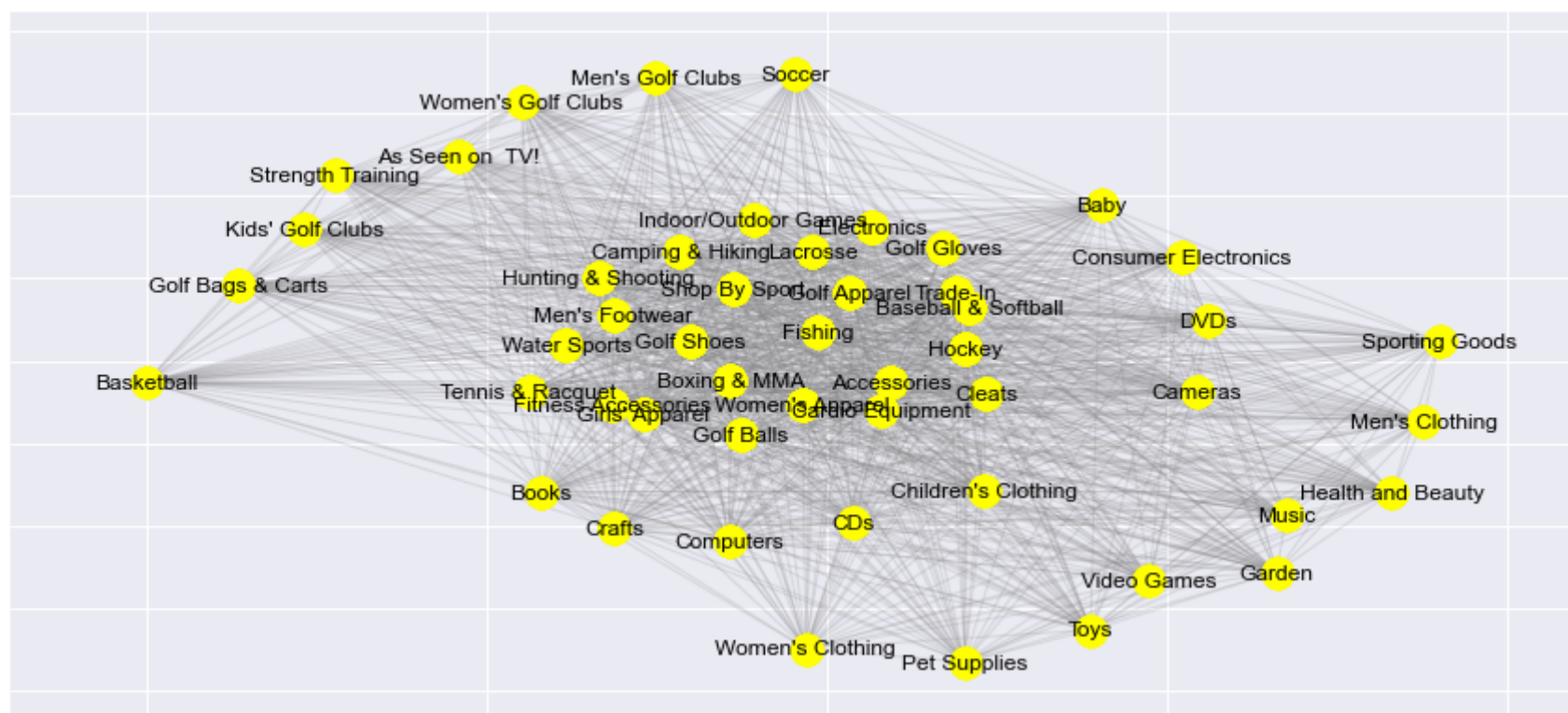



2. Weighted Projected Graph

```
In [8]: G = bipartite.weighted_projected_graph(B, primary_col)
node_labels = dict(zip(primary_col, primary_col))
```

```
In [9]: plt.figure(figsize=(15, 7))
pos = nx.spring_layout(G)

nx.draw_networkx_nodes(G, pos, nodelist=primary_col, node_color='yellow')
nx.draw_networkx_edges(G, pos, edge_color='grey', alpha=0.2)
nx.draw_networkx_labels(G, pos, labels=node_labels)
plt.show()
```



Community Detection

```
In [10]: df_groupby_category = df.groupby([SECONDARY])[PRIMARY].apply(lambda x: sorted(set(x)))
df_groupby_category = df_groupby_category.reset_index()
# print(df_groupby_category.iloc[14][1])
df_groupby_category.head()
```

```
Out[10]:
```

	Order	Region	Category Name
0		Canada	[Accessories, Baseball & Softball, Boxing & MM...
1		Caribbean	[Accessories, As Seen on TV!, Baseball & Soft...
2		Central Africa	[Accessories, Baseball & Softball, Boxing & MM...
3		Central America	[Accessories, As Seen on TV!, Baseball & Soft...
4		Central Asia	[Accessories, Boxing & MMA, Camping & Hiking, ...

```
In [11]: def get_cluster_common_values(cluster):
commons = []
for index, row in df_groupby_category.iterrows():
    if set(cluster).issubset(row[PRIMARY]):
        commons.append(row[SECONDARY])
return commons
```

```
In [12]: def print_communities(node_groups):
print('Number of communities:', len(node_groups))
for index, cluster in enumerate(node_groups):
    cluster = sorted(cluster)
    common_values = sorted(get_cluster_common_values(cluster))

    print(f'\nCluster {index}:')
    print(f"- {len(cluster)} Nodes: {'', '.join(cluster)}")
    print(f"- {len(common_values)} Common values: {'', '.join(common_values)}")
```

```
In [13]: import matplotlib.cm as cm
def plot_communities(nodes, labels):
    cmap = cm.get_cmap('autumn', max(labels) + 1)
    pos = nx.spring_layout(G)

    plt.figure(figsize=(15, 7))
    nx.draw_networkx_nodes(G, pos, nodes, cmap=cmap, node_color=labels)
    nx.draw_networkx_edges(G, pos, edge_color='grey', alpha=0.2)
    nx.draw_networkx_labels(G, pos)
    plt.show()
```

1. Louvain Algorithm

```
In [14]: import community.community_louvain as community_louvain
partition = community_louvain.best_partition(G)
louvain_node_groups = [[] for _ in set(partition.values())]

for node, cluster in sorted(partition.items()):
    louvain_node_groups[cluster].append(node)
```

```
In [15]: print_communities(louvain_node_groups)
plot_communities(partition.keys(), list(partition.values()))
```

Number of communities: 3

Cluster 0:

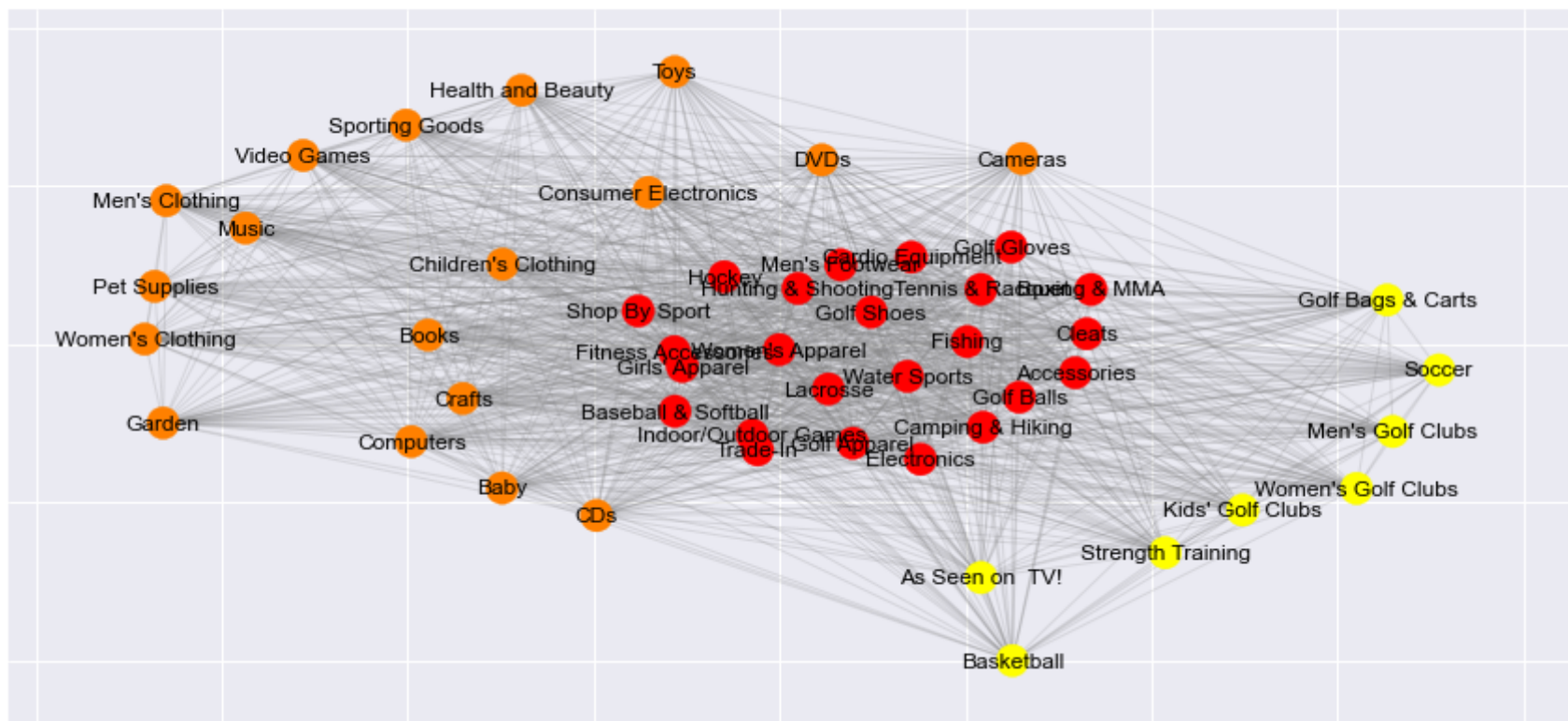
- 24 Nodes: Accessories, Baseball & Softball, Boxing & MMA, Camping & Hiking, Cardio Equipment, Cleats, Electronics, Fishing, Fitness Accessories, Girls' Apparel, Golf Apparel, Golf Balls, Golf Gloves, Golf Shoes, Hockey, Hunting & Shooting, Indoor/Outdoor Games, Lacrosse, Men's Footwear, Shop By Sport, Tennis & Racquet, Trade-In, Water Sports, Women's Apparel
- 22 Common values: Canada, Caribbean, Central Africa, Central America, East Africa, East of USA, Eastern Asia, Eastern Europe, North Africa, Northern Europe, Oceania, South America, South Asia, South of USA, Southeast Asia, Southern Africa, Southern Europe, US Center, West Africa, West Asia, West of USA, Western Europe

Cluster 1:

- 18 Nodes: Baby, Books, CDs, Cameras, Children's Clothing, Computers, Consumer Electronics, Crafts, DVDs, Garden, Health and Beauty, Men's Clothing, Music, Pet Supplies, Sporting Goods, Toys, Video Games, Women's Clothing
- 3 Common values: Oceania, South Asia, Southeast Asia

Cluster 2:

- 8 Nodes: As Seen on TV!, Basketball, Golf Bags & Carts, Kids' Golf Clubs, Men's Golf Clubs, Soccer, Strength Training, Women's Golf Clubs
- 3 Common values: Northern Europe, Southern Europe, Western Europe



2. K-Means Algorithm

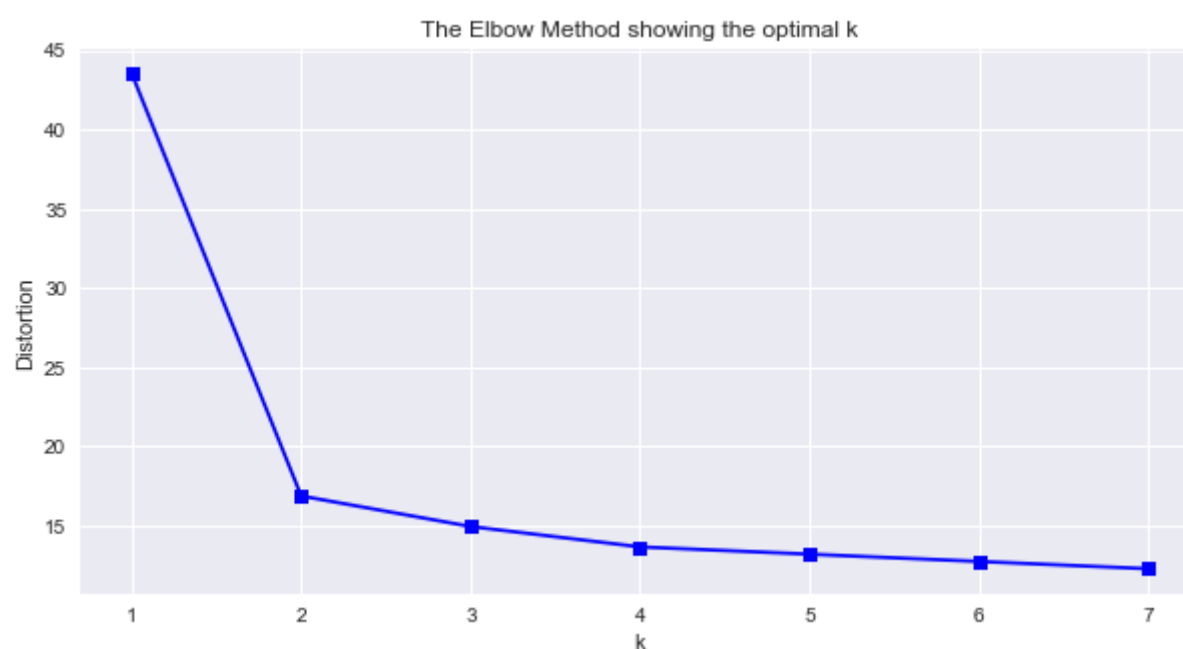
```
In [16]: from sklearn.cluster import KMeans
from scipy.spatial.distance import cdist
adj_matrix = nx.to_numpy_array(G)
adj_matrix
```

```
Out[16]: array([[ 0.,  4.,  4., ...,  4.,  4.,  4.],
        [ 4.,  0., 23., ...,  4., 23., 23.],
        [ 4., 23.,  0., ...,  4., 23., 23.],
        ...,
        [ 4.,  4.,  4., ...,  0.,  4.,  4.],
        [ 4., 23., 23., ...,  4.,  0., 23.],
        [ 4., 23., 23., ...,  4., 23.,  0.]])
```

```
In [17]: import numpy as np
distortions = []
K = range(1, 8)

for k in K:
    kmean_model = KMeans(n_clusters=k)
    kmean_model.fit(adj_matrix)
    dist = sum(np.min(cdist(adj_matrix, kmean_model.cluster_centers_, 'euclidean'), axis=1))
    distortions.append(dist / adj_matrix.shape[0])
```

```
In [18]: plt.figure(figsize=(10, 5))
plt.plot(K, distortions, 'bs-')
plt.xlabel('k')
plt.ylabel('Distortion')
plt.title('The Elbow Method showing the optimal k')
plt.show()
```



```
In [19]: kmeans = KMeans(n_clusters=2)
kmeans.fit(adj_matrix)

kmeans_node_groups = [[] for _ in range(kmeans.n_clusters)]
for node, cluster in zip(G.nodes(), kmeans.labels_):
    kmeans_node_groups[cluster].append(node)
```

```
In [20]: print_communities(kmeans_node_groups)
```

```
plot_communities(G.nodes(), kmeans.labels_)
```

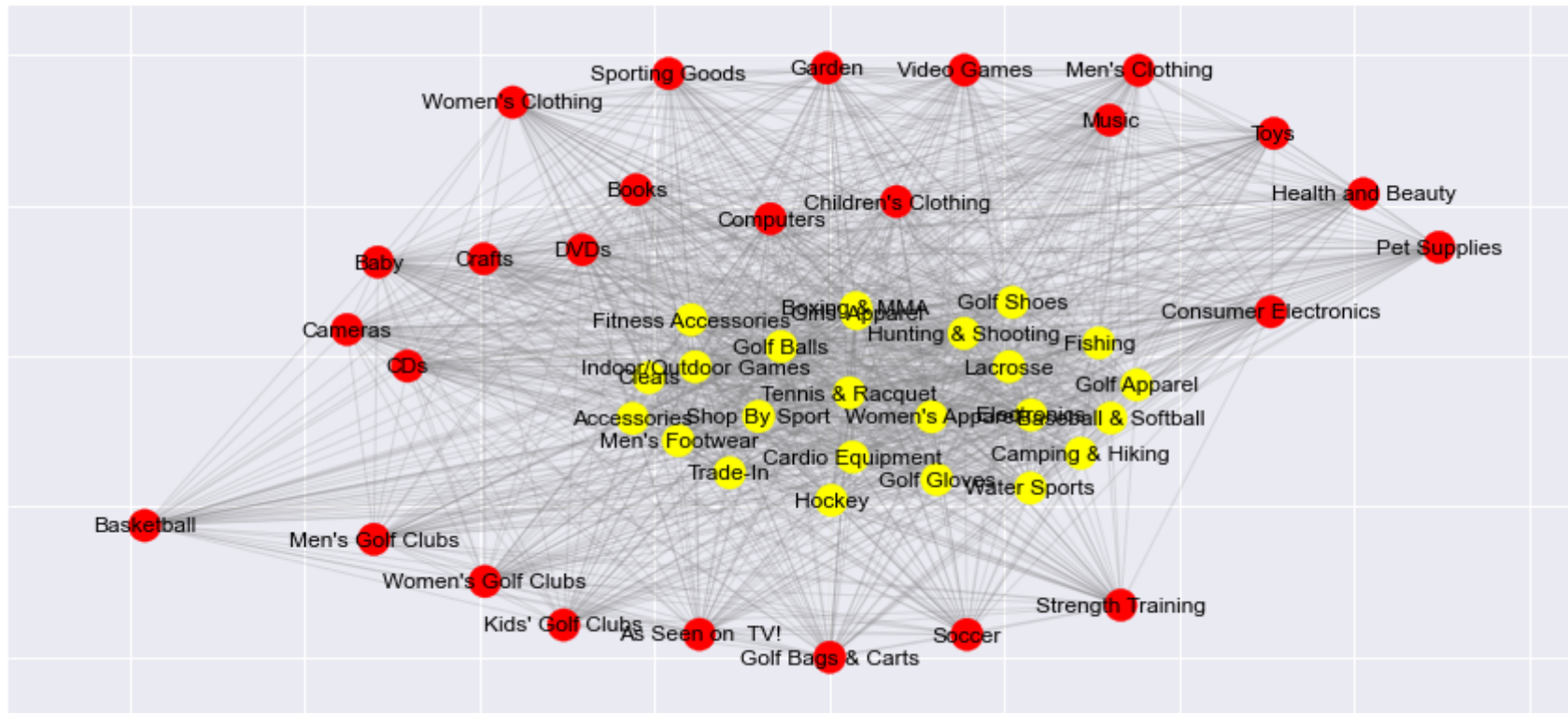
Number of communities: 2

Cluster 0:

- 26 Nodes: As Seen on TV!, Baby, Basketball, Books, CDs, Cameras, Children's Clothing, Computers, Consumer Electronics, Crafts, DVDs, Garden, Golf Bags & Carts, Health and Beauty, Kids' Golf Clubs, Men's Clothing, Men's Golf Clubs, Music, Pet Supplies, Soccer, Sporting Goods, Strength Training, Toys, Video Games, Women's Clothing, Women's Golf Clubs
- 0 Common values:

Cluster 1:

- 24 Nodes: Accessories, Baseball & Softball, Boxing & MMA, Camping & Hiking, Cardio Equipment, Cleats, Electronics, Fishing, Fitness Accessories, Girls' Apparel, Golf Apparel, Golf Balls, Golf Gloves, Golf Shoes, Hockey, Hunting & Shooting, Indoor/Outdoor Games, Lacrosse, Men's Footwear, Shop By Sport, Tennis & Racquet, Trade-In, Water Sports, Women's Apparel
- 22 Common values: Canada, Caribbean, Central Africa, Central America, East Africa, East of USA, Eastern Asia, Eastern Europe, North Africa, Northern Europe, Oceania, South America, South Asia, South of USA, Southeast Asia, Southern Africa, Southern Europe, US Center, West Africa, West Asia, West of USA, Western Europe



3. Gaussian Mixture Model

```
In [42]: from sklearn.mixture import GaussianMixture
n_clusters = 3
gmm = GaussianMixture(n_components=n_clusters)
gmm.fit(adj_matrix)

labels = gmm.predict(adj_matrix)
gmm_node_groups = [[] for _ in range(n_clusters)]
for node, cluster in zip(G.nodes(), labels):
    gmm_node_groups[cluster].append(node)
```

```
In [43]: print_communities(gmm_node_groups)
plot_communities(G.nodes(), labels)
```

Number of communities: 3

Cluster 0:

- 24 Nodes: Accessories, Baseball & Softball, Boxing & MMA, Camping & Hiking, Cardio Equipment, Cleats, Electronics, Fishing, Fitness Accessories, Girls' Apparel, Golf Apparel, Golf Balls, Golf Gloves, Golf Shoes, Hockey, Hunting & Shooting, Indoor/Outdoor Games, Lacrosse, Men's Footwear, Shop By Sport, Tennis & Racquet, Trade-In, Water Sports, Women's Apparel
- 22 Common values: Canada, Caribbean, Central Africa, Central America, East Africa, East of USA, Eastern Asia, Eastern Europe, North Africa, Northern Europe, Oceania, South America, South Asia, South of USA, Southeast Asia, Southern Africa, Southern Europe, US Center, West Africa, West Asia, West of USA, Western Europe

Cluster 1:

- 18 Nodes: Baby, Books, CDs, Cameras, Children's Clothing, Computers, Consumer Electronics, Crafts, DVDs, Garden, Health and Beauty, Men's Clothing, Music, Pet Supplies, Sporting Goods, Toys, Video Games, Women's Clothing
- 3 Common values: Oceania, South Asia, Southeast Asia

Cluster 2:

- 8 Nodes: As Seen on TV!, Basketball, Golf Bags & Carts, Kids' Golf Clubs, Men's Golf Clubs, Soccer, Strength Training, Women's Golf Clubs
- 3 Common values: Northern Europe, Southern Europe, Western Europe

ames', 41), ('Sporting Goods', 41), ('Pet Supplies', 41), ('Garden', 41), ('Men's Clothing', 41), ('Women's Clothing', 41), ('Strength Training', 40), ('Golf Bags & Carts', 40), ('Soccer', 40), ('Women's Golf Clubs', 40), ('Men's Golf Clubs', 40), ('Basketball', 40), ('Kids' Golf Clubs', 40), ('As Seen on TV!', 40)]

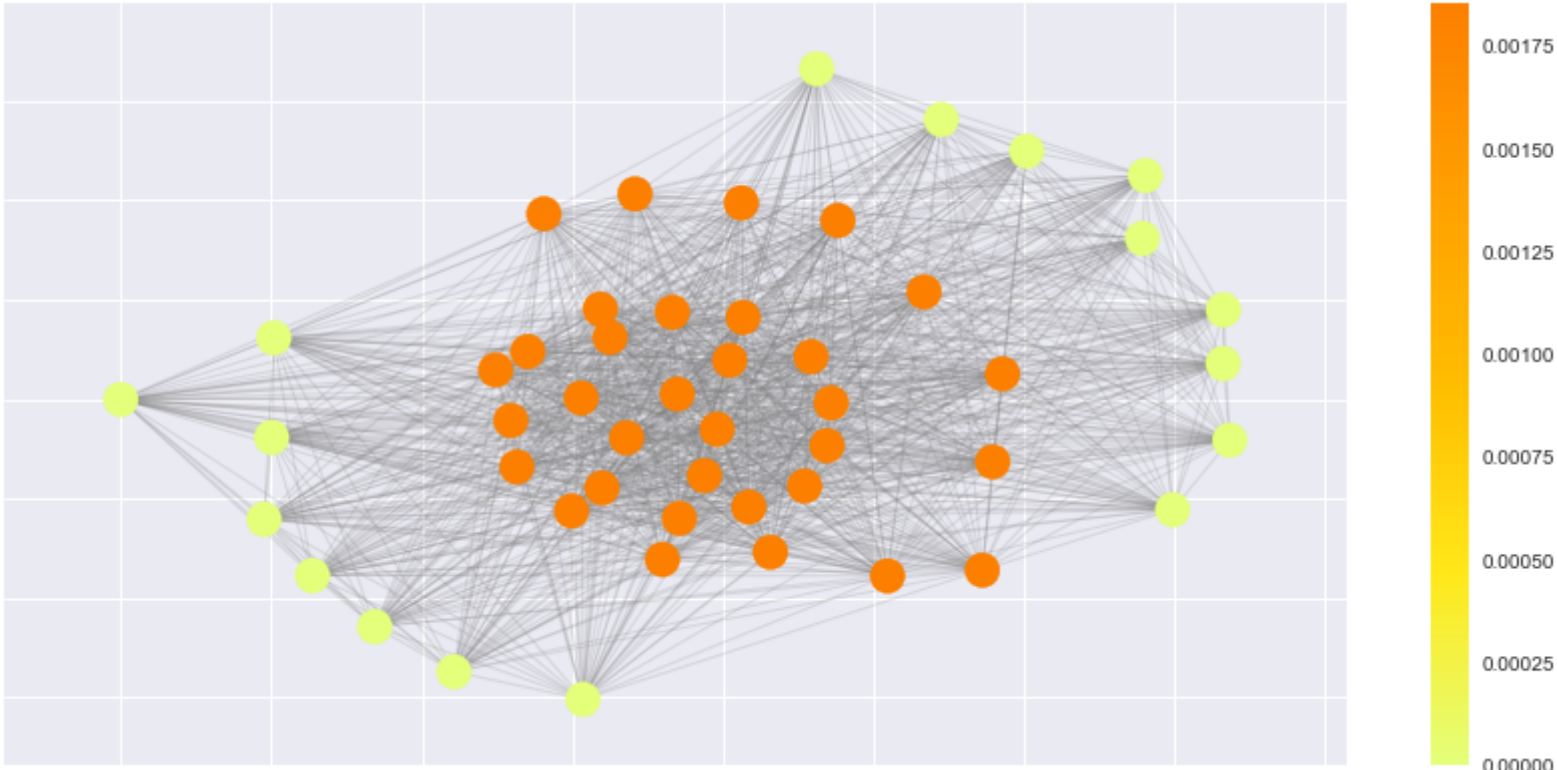
Out[46]:

	Category Name	Degree Centrality
49	Indoor/Outdoor Games	49
26	Golf Balls	49
43	Golf Shoes	49
21	Crafts	49
41	Golf Gloves	49

Betweenness Centrality

In [47]:

```
betweenness = nx.betweenness centrality(G)
plot_centrality(betweenness)
print_centrality(betweenness, 'Betweenness Centrality').head()
```



[('Indoor/Outdoor Games', 0.0018552875695732828), ('Girls' Apparel', 0.0018552875695732828), ('Golf Apparel', 0.0018552875695732828), ('Tennis & Racquet', 0.0018552875695732828), ('Fitness Accessories', 0.0018552875695732828), ('Cleats', 0.0018552875695732828), ('Golf Balls', 0.0018552875695732828), ('Golf Shoes', 0.0018552875695732828), ('Children's Clothing', 0.0018552875695732828), ('Lacrosse', 0.0018552875695732828), ('Baby', 0.0018552875695732828), ('Fishing', 0.0018552875695732828), ('Books', 0.0018552875695732828), ('DVDs', 0.0018552875695732828), ('CDs', 0.0018552875695732828), ('Hockey', 0.0018552875695732828), ('Golf Gloves', 0.0018552875695732828), ('Crafts', 0.0018552875695732828), ('Accessories', 0.0018552875695732828), ('Hunting & Shooting', 0.0018552875695732828), ('Electronics', 0.0018552875695732828), ('Shop By Sport', 0.0018552875695732828), ('Women's Apparel', 0.0018552875695732828), ('Computers', 0.0018552875695732828), ('Cameras', 0.0018552875695732828), ('Consumer Electronics', 0.0018552875695732828), ('Camping & Hiking', 0.0018552875695732828), ('Men's Footwear', 0.0018552875695732828), ('Baseball & Softball', 0.0018552875695732828), ('Water Sports', 0.0018552875695732828), ('Trade-In', 0.0018552875695732828), ('Cardio Equipment', 0.0018552875695732828), ('Boxing & MMA', 0.0018552875695732828), ('Golf Bags & Carts', 0.0), ('Music', 0.0), ('Women's Golf Clubs', 0.0), ('Toys', 0.0), ('Men's Golf Clubs', 0.0), ('Video Games', 0.0), ('Sporting Goods', 0.0), ('Health and Beauty', 0.0), ('Pet Supplies', 0.0), ('Garden', 0.0), ('Strength Training', 0.0), ('Men's Clothing', 0.0), ('Women's Clothing', 0.0), ('Soccer', 0.0), ('Basketball', 0.0), ('Kids' Golf Clubs', 0.0), ('As Seen on TV!', 0.0)]

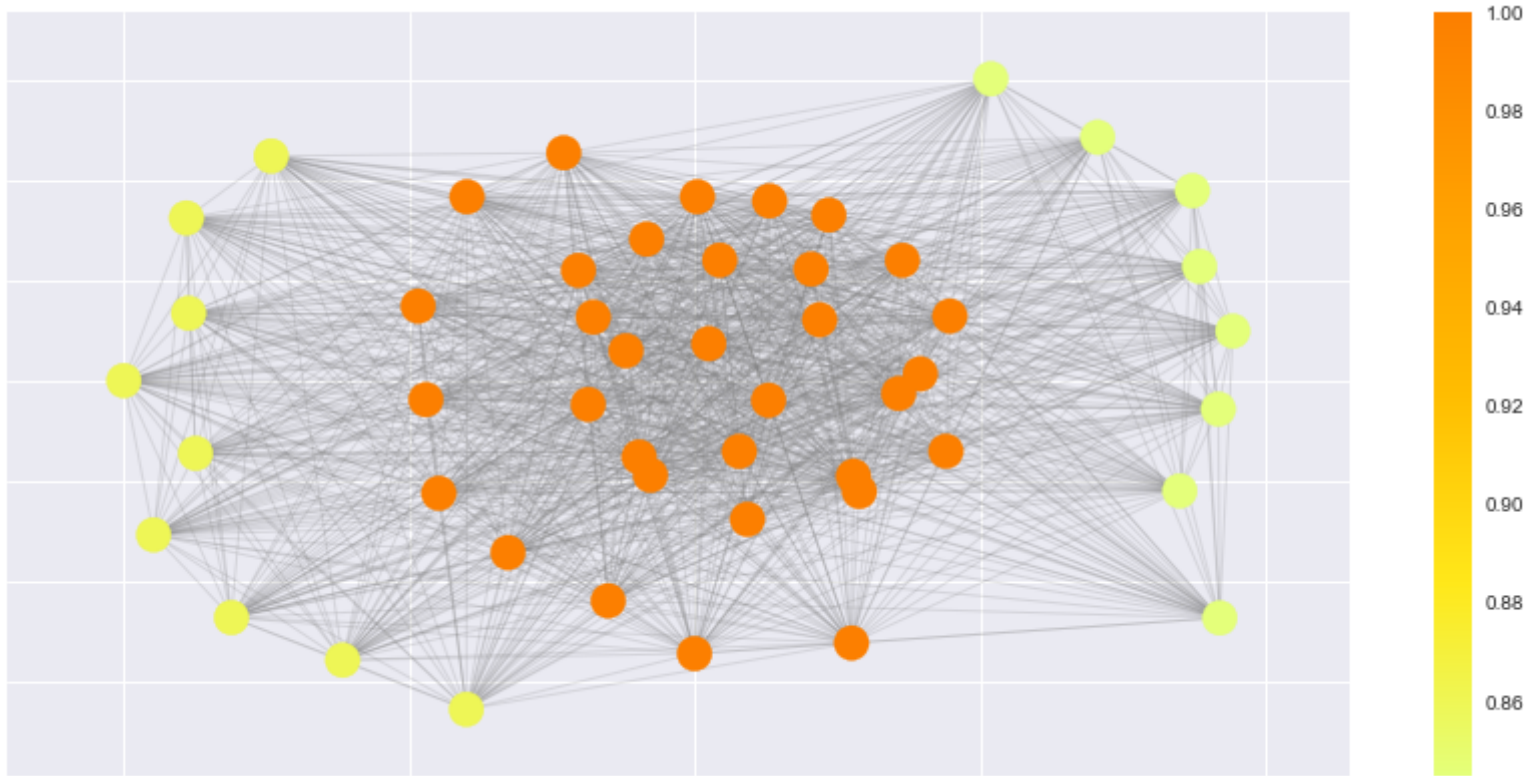
Out[47]:

	Category Name	Betweenness Centrality
49	Indoor/Outdoor Games	0.001855
18	Girls' Apparel	0.001855
44	Golf Apparel	0.001855
23	Tennis & Racquet	0.001855
24	Fitness Accessories	0.001855

Closeness Centrality

In [48]:

```
closeness = nx.closeness centrality(G)
plot_centrality(closeness)
print_centrality(closeness, 'Closeness Centrality').head()
```

```
[('Indoor/Outdoor Games', 1.0), ('Golf Balls', 1.0), ('Golf Shoes', 1.0), ('Crafts', 1.0), ('Golf Gloves', 1.0), ('Tennis & Racquet', 1.0), ('Fitness Accessories', 1.0), ('Cleats', 1.0), ("Children's Clothing", 1.0), ('Golf Apparel', 1.0), ('Lacrosse', 1.0), ('Baby', 1.0), ('Fishing', 1.0), ('Books', 1.0), ('DVDs', 1.0), ('CDs', 1.0), ('Accessories', 1.0), ("Girls' Apparel", 1.0), ('Hockey', 1.0), ('Shop By Sport', 1.0), ('Computers', 1.0), ('Cameras', 1.0), ('Consumer Electronics', 1.0), ('Camping & Hiking', 1.0), ("Men's Footwear", 1.0), ('Baseball & Softball', 1.0), ('Hunting & Shooting', 1.0), ('Water Sports', 1.0), ('Trade-In', 1.0), ('Cardio Equipment', 1.0), ('Boxing & MMA', 1.0), ('Electronics', 1.0), ("Women's Apparel", 1.0), ('Music', 0.8596491228070176), ('Health and Beauty', 0.8596491228070176), ('Toys', 0.8596491228070176), ('Video Games', 0.8596491228070176), ('Sporting Goods', 0.8596491228070176), ('Pet Supplies', 0.8596491228070176), ('Garden', 0.8596491228070176), ("Men's Clothing", 0.8596491228070176), ("Women's Clothing", 0.8596491228070176), ('Strength Training', 0.8448275862068966), ('Golf Bags & Carts', 0.8448275862068966), ('Soccer', 0.8448275862068966), ("Women's Golf Clubs", 0.8448275862068966), ("Men's Golf Clubs", 0.8448275862068966), ('Basketball', 0.8448275862068966), ("Kids' Golf Clubs", 0.8448275862068966), ('As Seen on TV!', 0.8448275862068966)]
```

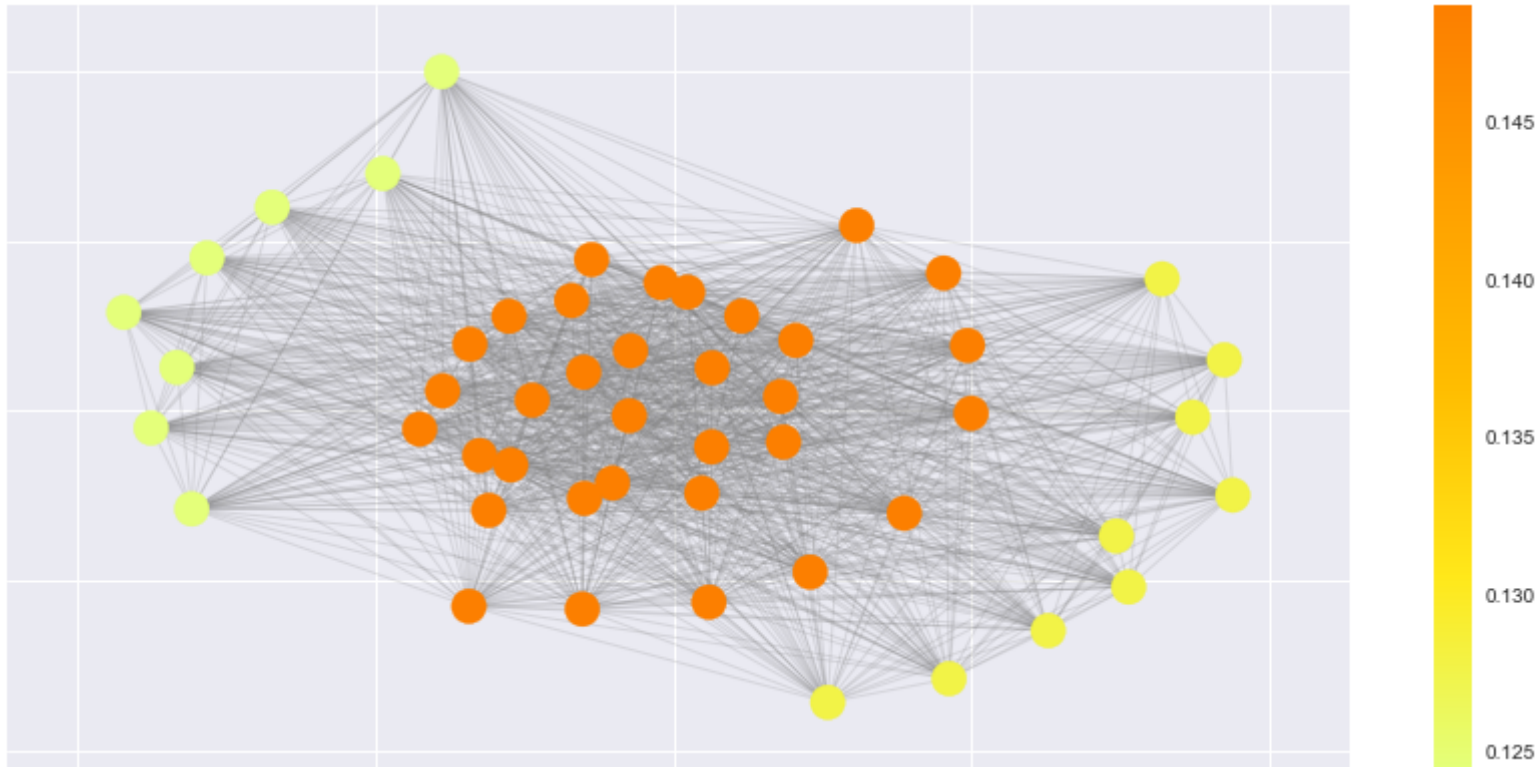
Out[48]:

	Category Name	Closeness Centrality
49	Indoor/Outdoor Games	1.0
26	Golf Balls	1.0
43	Golf Shoes	1.0
21	Crafts	1.0
41	Golf Gloves	1.0

Eigenvector Centrality

In [49]:

```
eigenvector = nx.eigenvector_centrality(G)
plot_centrality(eigenvector)
print_centrality(eigenvector, 'Eigenvector Centrality').head()
```



```
[('Indoor/Outdoor Games', 0.14867064721396608), ("Children's Clothing", 0.14867064721396608), ('Crafts', 0.14867064721396608), ('Golf Gloves', 0.14867064721396608), ('Tennis & Racquet', 0.14867064721396608), ('Fitness Accessories', 0.14867064721396608), ('Cleats', 0.14867064721396608), ('Golf Balls', 0.14867064721396608), ('Lacrosse', 0.14867064721396608), ("Girls' Apparel", 0.14867064721396608), ('Baby', 0.14867064721396608), ('Fishing', 0.14867064721396608), ('Books', 0.14867064721396608), ('DVDs', 0.14867064721396608), ('CDs', 0.14867064721396608), ('Hockey', 0.14867064721396608), ('Golf Shoes', 0.14867064721396608), ('Accessories', 0.14867064721396608), ('Golf Apparel', 0.14867064721396608), ('Water Sports', 0.14867064721396608), ('Shop By Sport', 0.14867064721396608), ("Women's Apparel", 0.14867064721396608), ('Electronics', 0.14867064721396608), ('Boxing & MMA', 0.14867064721396608), ('Cardio Equipment', 0.14867064721396608), ('Trade-In', 0.14867064721396608), ('Hunting & Shooting', 0.14867064721396608), ('Baseball & Softball', 0.14867064721396608), ("Men's Footwear", 0.14867064721396608), ('Camping & Hiking', 0.14867064721396608), ('Consumer Electronics', 0.14867064721396608), ('Cameras', 0.14867064721396608), ('Computers', 0.14867064721396608), ('Video Games', 0.12767929833125463), ('Music', 0.12767929833125463), ('Garden', 0.12767929833125463), ('Toys', 0.12767929833125463), ('Pet Supplies', 0.12767929833125463), ('Health and Beauty', 0.12767929833125463), ('Sporting Goods', 0.1276792983312546), ("Men's Clothing", 0.12767929833125463), ("Women's Golf Clubs", 0.12767929833125463), ("Men's Golf Clubs", 0.12767929833125463), ('Basketball', 0.12767929833125463), ("Kids' Golf Clubs", 0.12767929833125463), ('As Seen on TV!', 0.12767929833125463)]
```


3312546), ("Women's Clothing", 0.1276792983312546), ('Strength Training', 0.12444087284685672), ('Golf Bags & Carts', 0.12444087284685672), ('Soccer', 0.12444087284685672), ("Women's Golf Clubs", 0.12444087284685672), ("Men's Golf Clubs", 0.12444087284685672), ('Basketball', 0.12444087284685672), ("Kids' Golf Clubs", 0.12444087284685672), ('As Seen on TV!', 0.12444087284685672)]

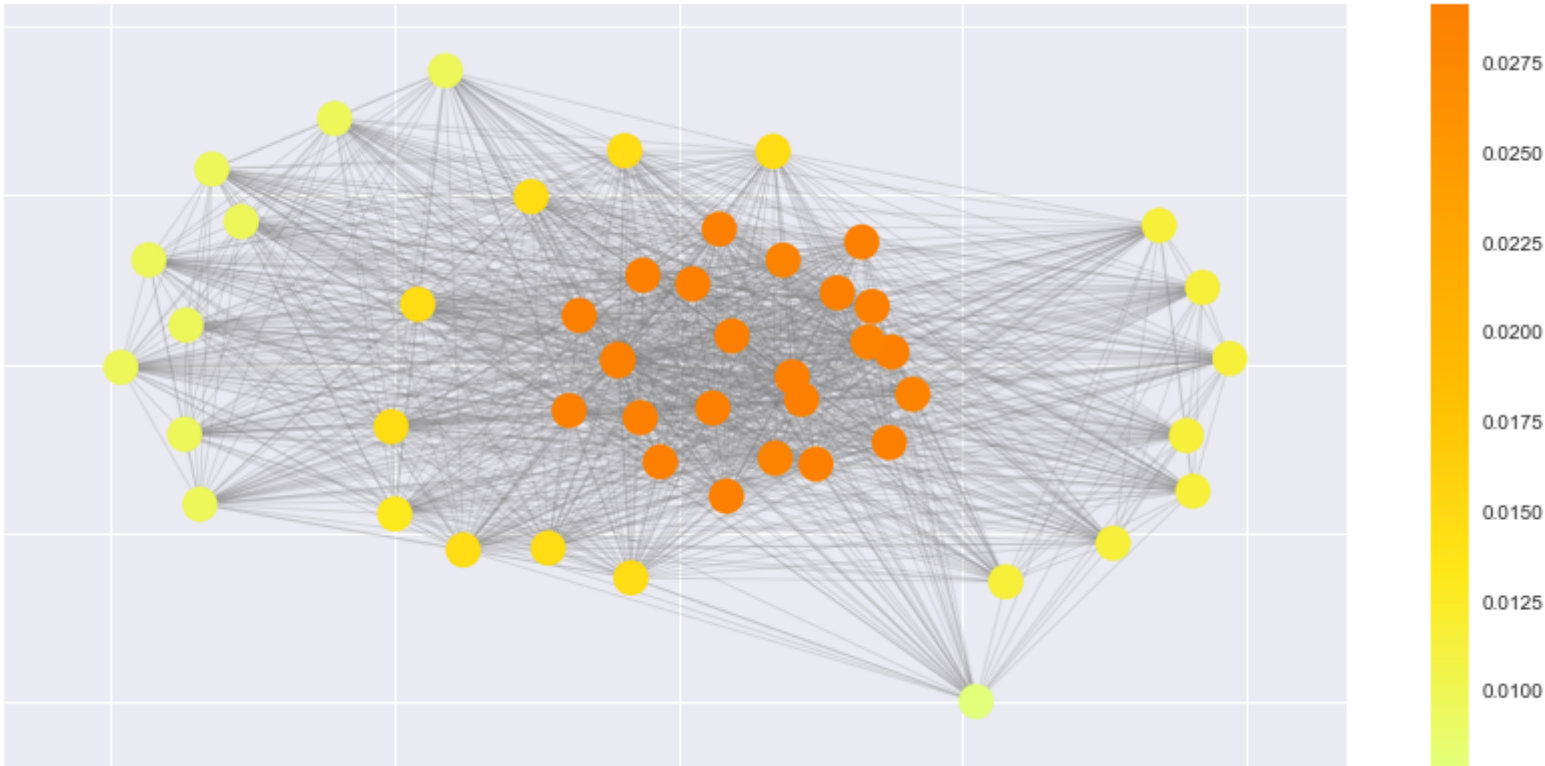
Out[49]:

	Category Name	Eigenvector Centrality
49	Indoor/Outdoor Games	0.148671
28	Children's Clothing	0.148671
21	Crafts	0.148671
41	Golf Gloves	0.148671
23	Tennis & Racquet	0.148671

PageRank

In [50]:

```
pagerank = nx.pagerank(G)
plot_centrality(pagerank)
print_centrality(pagerank, 'PageRank').head()
```



[('Indoor/Outdoor Games', 0.02910004330793566), ("Men's Footwear", 0.02910004330793566), ('Fishing', 0.02910004330793566), ('Lacrosse', 0.02910004330793566), ('Golf Balls', 0.02910004330793566), ('Cleats', 0.02910004330793566), ('Tennis & Racquet', 0.02910004330793566), ('Golf Apparel', 0.02910004330793566), ('Accessories', 0.02910004330793566), ('Camping & Hiking', 0.02910004330793566), ("Girls' Apparel", 0.02910004330793566), ('Cardio Equipment', 0.02910004330793566), ('Water Sports', 0.02910004330793566), ('Shop By Sport', 0.02910004330793566), ("Women's Apparel", 0.02910004330793566), ('Electronics', 0.02910004330793566), ('Boxing & MMA', 0.02910004330793566), ('Hunting & Shooting', 0.02910004330793566), ('Trade-In', 0.02910004330793566), ('Golf Gloves', 0.02910004330793566), ('Hockey', 0.028393028110741375), ('Golf Shoes', 0.028393028110741375), ('Fitness Accessories', 0.028393028110741375), ('Baseball & Softball', 0.028393028110741375), ('Crafts', 0.01460032971973412), ('Computers', 0.01460032971973412), ("Children's Clothing", 0.01460032971973412), ('Baby', 0.01460032971973412), ('Consumer Electronics', 0.01460032971973412), ('Books', 0.01460032971973412), ('DVDs', 0.01460032971973412), ('CDs', 0.01460032971973412), ('Cameras', 0.012939485390217484), ("Women's Golf Clubs", 0.01134315515704318), ("Men's Golf Clubs", 0.01134315515704318), ('Golf Bags & Carts', 0.01134315515704318), ('As Seen on TV!', 0.01134315515704318), ('Strength Training', 0.01134315515704318), ('Soccer', 0.01134315515704318), ("Kids' Golf Clubs", 0.01134315515704318), ('Pet Supplies', 0.009718050588254678), ('Health and Beauty', 0.009718050588254678), ('Music', 0.009718050588254678), ('Video Games', 0.009718050588254678), ('Garden', 0.009718050588254678), ("Men's Clothing", 0.009718050588254678), ("Women's Clothing", 0.009718050588254678), ('Toys', 0.009718050588254678), ('Sporting Goods', 0.009718050588254678), ('Basketball', 0.007820356856636094)]

Out[50]:

	Category Name	PageRank
49	Indoor/Outdoor Games	0.0291
11	Men's Footwear	0.0291
31	Fishing	0.0291
29	Lacrosse	0.0291
26	Golf Balls	0.0291

In []: