

## Portfolio Optimization with R/Rmetrics

Diethelm Würtz Yohan Chalabi, Andrew Ellis, Dominik Locher

ETH Zurich, Rmetrics Association, Theta Fundmanagement

Thanks to William Chen, Alexios Ghalanos, Francisco Gochez

RinFinance Workshop Chicago, April 2009

### The Problem ...



### Portfolio Optimization Problem

... return, risk, performance ratio

For a given set of financial assets let us find the composition

- 1) which minimizes the risk for a given return (reward),
- 2) which maximizes the return for a given risk,
- 3) which optimizes a reward/risk performance ratio,
- 4) which finds the global minimum risk,

subject to certain constraints and preferences.



### How to quantify Risk?



#### *Stone* 1973

$$R_{S}[Y_{0}, k, A](f) = \left(\int_{-\infty}^{A} |y - Y_{0}|^{k} f(y) dy\right)^{1/k}$$

$$R_{SD}(f) = R_S[\mu_v, 2, \infty](f)$$

$$R_{SD}(f) = R_S[\mu_v, 2, \infty](f)$$
  $R_{SSD}(f) = R_S[\mu_v, 2, 0](f)$ 

$$R_{SVM}(f) = R_S[\mu_V, 2, 0]^2(f)$$
  $R_{\alpha-t}(f) = R_S[t, \alpha, t]^{\alpha}(f)$ 

$$R_{\alpha-t}(f) = R_S[t, \alpha, t]^{\alpha}(f)$$

y are the financial returns, f() their multivariate distribution A,  $Y_0$ , and k parameters

#### Pederson and Satchell 1998

$$R[A, b, \alpha, \theta, W(\cdot)] = \left[ \int_{-\infty}^{A} |y - b|^{\alpha} W[F(y)] f(y) dy \right]^{\theta}$$

for some bounded function W()

(BP1) (Nonnegativity):  $R[\tilde{v}] > 0$ .

(BP2) (Homogeneity):  $R[\lambda \tilde{y}] = |\lambda| R[\tilde{y}]$  for  $\lambda > 0$ .

(BP3) (Subadditivity):  $R[\tilde{v_1} + \tilde{v_2}] < R[\tilde{v_1}] + R[\tilde{v_2}]$ .

(BP4) (Shift-invariance):  $R[\tilde{y} + \lambda] \leq R[\tilde{y}]$  for all  $\lambda$ .

### Artzner, Delbaen, Eber, Heath 1999

(ADEH 3) (translation invariance) R(X + c) = R(X) - c for all c

(ADEH 4) (monotonicity)  $X \le Y \implies R(Y) \le R(X)$ . ... this makes a coherent risk measure



### Axiomatic Risk Measures



- (a) Stone's Class for k > 1 and  $Y_0 = \mu_y$  and  $A = \mu_y$  or  $A = \infty$ 
  - Standard deviation
  - Mean absolute deviation
  - Fishburn's  $\alpha t$  measures for  $t = \mu_y$  raised to power  $\frac{1}{k}$
  - *Semistandard deviation* (3)
  - The first Kijima-Ohnishi measure
  - Generalized lower partial moment
- (b) *The range*
- (c) The piecewise linear measures
  - The Gini coefficient
  - The L-moments for r + s < 2
- (d) Kijima and Ohsniki's second measure

Pederson and Satchell 1998

... note

Covariance Risk Measure: (Standard deviation)<sup>2</sup>

CVaR Measure:  $k = 1, A = VaR, Y_0 = 0$ 

new Developments: Spectral Risk Measures



### Mean - Variance Portfolios



#### Markowitz 1952, QP1:

#### Minimize Risk for a given Return:

$$\min \quad w^{\top} \hat{\Sigma} w$$

$$s.t.$$

$$w^{\top} \hat{\mu} = \overline{r}$$

$$w^{\top} 1 = 1$$

$$Aw < b$$

#### QP2:

#### Maximize Return for a given Risk:

$$s.t.$$
  $\begin{aligned} \max_{w} & w^{\top} \hat{\mu} \\ w^{\top} 1 &= 1 \\ Aw &\leq b \\ w^{\top} \hat{\Sigma} w &\leq \sigma \\ w^{\top} B w &\leq c \end{aligned}$ 

QP1 Solution:

"Quadratic Programming Solvers" Goldfarb and Idnani, 1982

QP2 Solution:

"Second Order Cone Programming Solver" Nesterov and Nemirovski, 1994



### Mean – QLPM Portfolios



#### Nawrocki, 1992:

#### **Quadratic Lower Partial Moments:**

#### $LPM = E[\{\max(0, \tau - y)\}^a]$

τ Benchmark

0 < a < 1 Risk seeking behavior

a = 1 Risk neutrality

a > 1 Risk aversion

$$min_{w} \quad w^{\top}Lw$$
  $s.t.$   $Aw \leq b$ 

Co-Lower Partial Moments

$$CLPM_{ij} = \frac{1}{k} \sum_{t=1}^{k} [MAX\{0, (\tau_t - x_{it})\}]^{a-1} (\tau_t - x_{jt}), \text{ for } a > 1$$

$$CLPM_{ij} = \frac{1}{k} \sum_{t=1}^{k} I_{\{MAX[0.(\tau_T - x_{it})]\}} \cdot (\tau_t - x_{jt}), \text{ for } a = 1$$

$$L = \begin{pmatrix} CLPM_{11} & \cdots & CLPM_{1n} \\ \vdots & \ddots & \vdots \\ CLPM_{n1} & \cdots & CLPM_{nn} \end{pmatrix}$$

Mean – QLPM Solution: For a > 1 formally equivalent to QP1



### Mean - CVaR Poertfolios



#### Rockafeller and Uryasev 1992:

#### CVAR:

$$e_s = \max \left[ 0, VaR - \sum_{i=1}^n w_i r_{i,s} \right]$$

$$CVaR = VaR - \left(\frac{1}{m} \sum_{s=1}^{m} e_s\right) / \alpha$$

Note if the assets are elliptically distributed, we will get the same set of weights as for the Mean-Variance Markowitz Portfolio!

$$\max_{w_i, e_s, VaR} VaR - \left(\frac{1}{m} \sum_{s=1}^{m} e_s\right) / \alpha$$

$$\sum\nolimits_{i=1}^n w_i \mu_i \geq \overline{\mu}$$

$$e_s \ge VaR - \sum_{i=1} w_i r_{i,s}$$

$$e_s \ge 0$$

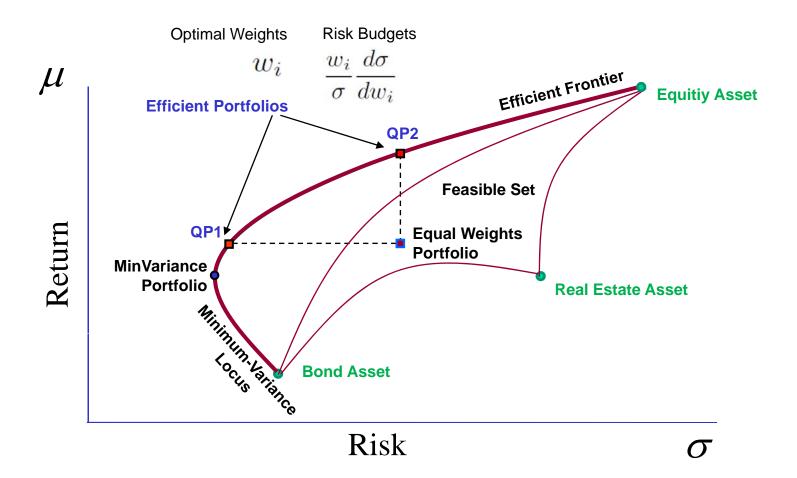
$$w_i \ge 0$$

. . .

Mean - CVaR Solution: Linear Programming Problem

... note Conditional Drawdown at Risk Portfolios can be solved in the same way

### Risk vs. Return



Chicago, April 2009 www.rmetrics.org Page 8



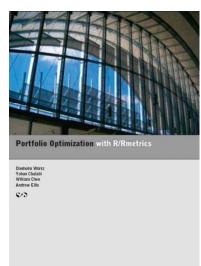
### fPortfolio Models

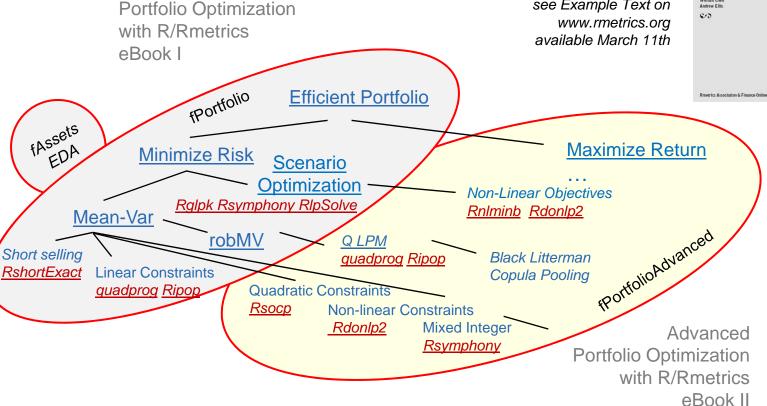


#### fPortfolio Zoo: **Rmetrics Software**

**Topics** Managing Data Sets of Assets Exploratory Data Analysis of Assets Portfolio Framework Mean-Variance Portfolios Mean-CVaR Portfolios Portfolio Backtesting

> 462 p 88 CHF see Example Text on www.rmetrics.org







### Rmetrics Packages



# Chronological Objects in R/Rmetrics eBook, available in July

timeDate\*

timeSeries\*

1

datafeed\*3

- CRAN Repository
- 2 r-forge Repository
- 3 Rmetrics Repository
- \* Rmetrics Packages and/or Interfaces





```
fPortfolioAdvanced*3
fPortfolioSolver*2
Ripop*3
Rnlminb*3
RlpSolve*2
RlpSolveAPI*2
Rsocp*2
Rdonlp22
... commercial solvers3
BLCOP12
```



### Portfolio Structure.



#### **Portfolio Model**

#### **Portfolio Functions**

#### **Portfolio Data**

#### **Portfolio Specification**

#### **Portfolio Constraints**

#### **Default Portfolio:**

```
Constrained MV Portfolio with LongOnly constraints
```

```
portfolioFrontier()
  efficientPortfolio()
  minriskPortfolio()
  maxratioPortfolio()
  feasiblePortfolio()
```

#### portfolioData()

timeSeries

#### portfolioSpec()

```
setType() = "MV"
setEstimator() = "covEstimator"
setOptimize() = "minRisk"
setSolver() = "solveRquadprog"
...
```

#### portfolioConstraints()

```
"LongOnly"
```

#### CVaR Example:

```
Mean-CVaR Portfolio with alternative constraints
```

```
portfolioFrontier()
  efficientPortfolio()
  minriskPortfolio()
  maxratioPortfolio()
  feasiblePortfolio()
```

#### portfolioData()

timeSeries

#### portfolioSpec()

```
setType() = "CVaR"
setAlpha() = 0.05
setOptimize() = "minRisk"
setSolver ()= "solveRsymphony"
...
```

#### portfolioConstraints()

"LongOnly", "Short", "Partial", minW, maxW, minsumW, maxSumW, eqsumW, minsumB, maxSumB, eqsumB, listFun, minFun, maxFun, ...



### Explorative Data Analysis

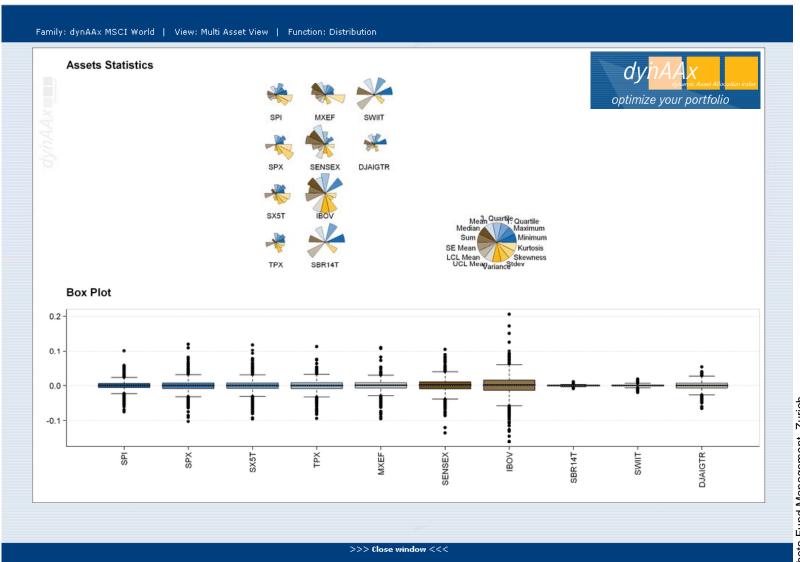




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### Asset Selection



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### Optimizing MV Portfolios ...



Load Data Set, Specification and Constraints
Pictet Swiss Pension Fund Benchmark
LPP2005

Compute the efficient frontier

Output:

The portfolio weights

The covariance risk budgets

The target returns and target risks

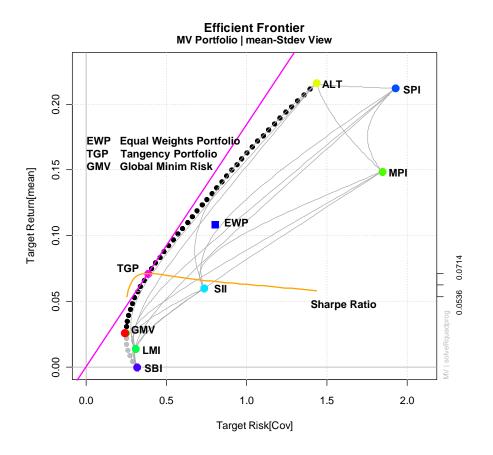
```
# LPP Portfolio Example:
  Data = LPP2005.RET[, 1:6]
  Spec = portfolioSpec()
> Cons = "LongOnly"
# Portfolio Frontier:
> portfolioFrontier(Data, Spec, Cons)
Title:
 MV Portfolio Frontier:
                   covEstimator
 Estimator:
 Solver:
                   solveRquadprog
                   minRisk
 Optimize:
                   LongOnly
 Constraints:
 Portfolio Points: 5 of 50
Portfolio Weights:
           SPI
      SBI
                  SII
  1.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
13 0.0327 0.0000 0.1458 0.6594 0.0000 0.1621 0.0000 0.0000 0.0000
25 0.0000 0.0081 0.2492 0.3528 0.0000 0.3899 0.0000 0.0000 0.0000
37 0.0000 0.0197 0.3516 0.0120 0.0000 0.6168 0.0000 0.0000 0.0000
50 0.0000 0.0000 0.0000 0.0000 1.0000 0.0000 0.0000 0.0000
Covariance Risk Budgets:
      SBI
              SPI
                      SII
                              LMI
                                      MPI
                                              ALT
                                                    LPP25
                                                           LPP40
                                                                   LPP60
   1.0000
           0.0000
                   0.0000
                           0.0000
                                   0.0000
                                          0.0000
                                                  0.0000
                                                          0.0000
                                                                  0.0000
   0.0116
           0.0000
                   0.1586
                           0.3456
                                                  0.0000
                                   0.0000
                                           0.4841
                                                          0.0000
                                                                  0.0000
   0.0000
           0.0176
                   0.1225 -0.0083
                                   0.0000
                                                  0.0000
                                                          0.0000
                                                                  0.0000
                                           0.8683
   0.0000
           0.0274
                   0.0954 -0.0008
                                   0.0000
                                           0.8780
                                                  0.0000
                                                          0.0000
                                                                  0.0000
   0.0000
           0.0000
                   0.0000
                          0.0000
                                   0.0000
                                          1.0000
                                                  0.0000
                                                          0.0000
                                                                  0.0000
Target Return and Risks:
                   Cov Sigma
                                CVaR
                                        VaR
     mean
  0.0000 0.0000 0.1261 0.1261 0.2758 0.2177
13 0.0210 0.0210 0.1198 0.1198 0.2329 0.1708
25 0.0420 0.0420 0.2381 0.2381 0.5135 0.3348
37 0.0630 0.0630 0.3845 0.3845 0.8577 0.5714
50 0.0858 0.0858 0.5684 0.5684 1.3343 0.8978
```

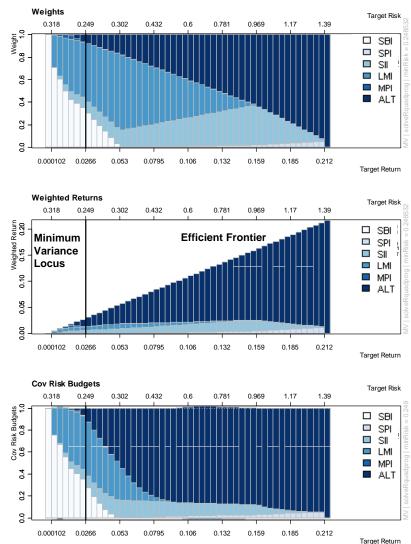


### Plotting Frontiers and Weights .....



#### LPP 2005 Benchmark Portfolio



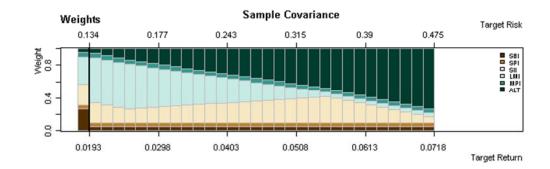




## Adding Box/Group Constraints ...



```
# Example:
Cons = c(
  "minW[1:nAssets] = 0.05",
  "maxsumW[c('SBI','LMI'] = 0.6")
# Mean-Variance:
frontier = portfolioFrontier(Data,Spec,Cons)
# Weights Plot:
weightsPlot(frontier)
```



### Reducing Estimation Errors ...



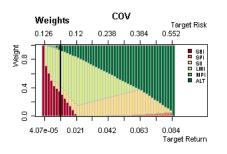
#### Functions:

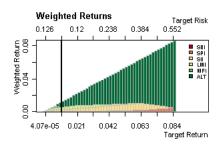
covEstimator
kendallEstimator
spearmanEstimator
mcdEstimator
mveEstimator
covMcdEstimator
covOGKEstimator
shrinkEstimator
baggedEstimator

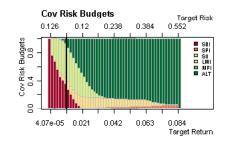
```
# MV Sample Estimator:
covFrontier = portfolioFrontier(Data, Spec)

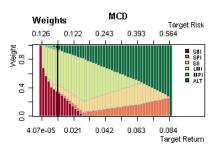
# MV MCD Estimator:
setEstimator(Spec) <- "covMcdEstimator"
mcdFrontier <- portfolioFrontier(Data, Spec)

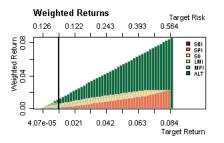
# Weights Plot:
weightsPlot(covFrontier)
weightsPlot(mcdFrontier)</pre>
```

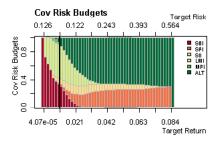


































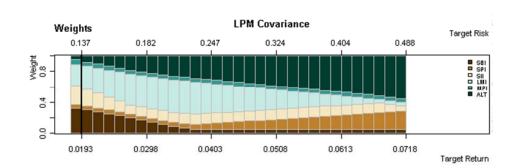
### Q Lower Partial Moments



```
# Example:
Cons = c(
   "minW[1:nAssets] = 0.05",
   "maxsumW[c('SBI','LMI'] = 0.60")

# Quadratic Lower Partial Moments:
setEstimator(Spec) <- "lpmEstimator"
Spec@model$param$a <- 1.25
Spec@model$param$tau <- "colMeans"
frontier <- portfolioFrontier(Data,Spec,Cons)

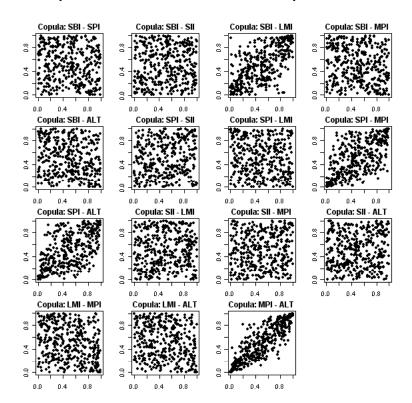
# Weights Plot:
weightsPlot(frontier)</pre>
```



### Copulae Tail Risks.



#### Copulae Lower Tail Risk Dependence Budgets



SBI CH Bonds SPI CH Stocks SII CH Immo LMI World Bonds MPI World Stocks ALT World AltInvest

$$\lambda_{lower} = \lim_{u \to 0} \left[ \Pr\left( Y \le F_Y^{-1}(u) \mid X \le F_X^{-1}(u) \right) \right]$$
$$= \lim_{u \to 0} \left[ \frac{C(u, u)}{u} \right]$$

$$\min \ w^{\top} \hat{\Sigma} \ w$$

$$s. \ t.$$

$$w^{\top} \hat{\mu} = \overline{r}$$

$$w^{\top} 1 = 1$$

$$\mathcal{L}_{i}^{lower} \leq \frac{w_{i}}{\lambda} \frac{d\lambda}{dw_{i}} \leq \mathcal{L}_{i}^{upper}$$
...

... Quadratic Constraints use Rsocp (not yet fully implemented)



### Handling Nonlinear Constraints ....

```
# Specification:
spec <- portfolioSpec()</pre>
setTargetReturn(spec) <- 4*mean(data) # 17.2%</pre>
setObjective(spec) = c("Objective", "Return", "Risk")
Return <- function(weights)</pre>
   (getMu(Data) %*% weights)
Risk <- function(weights)</pre>
   (sqrt(weights %*% getSigma(Data) %*% weights))
Objective <- function(weights) Risk(weights)</pre>
setSolver(spec) <- "solveRdonlp2"</pre>
# 130/30 Extension Constraints:
lowerExtension <- function(w) sum(w[w<01)</pre>
upperExtension <- function(w) sum(w[w>0])
cons <- c(
   "minW[1:nAssets] = rep(-0.30, times = nAssets)",
   "maxW[1:nAssets] = rep( 1.30, times = nAssets)",
   "minsumW[1:nAssets] = -0.30",
   "maxsumW[1:nAssets] = 1.30",
   "listF = list(lowerExtension, upperExtension),
   "minF = c(-0.30, 0.00)",
   "maxF = c(0.00, 1.30)")
# Portfolio:
efficientPortfolio(data, spec, cons)
```

```
Title:
 MV Efficient Portfolio
 Estimator:
               covEstimator
 Solver:
               solveRdonlp2
 Optimize:
               minRisk
 Constraints:
               minW maxW minsumW maxsumW
Portfolio Weights:
   SBI
          SPI
                 SII
                       LMI
                              MPI
                                     ALT
-0.293 0.001 -0.000 -0.006 0.000 1.243
Covariance Risk Budgets:
   SBT
          SPT
                 STT
                       T.M.T
                              MPT
                                     AT.T
0.0121 0.0009 0.0000 0.0003 0.0003 0.9864
Target Return and Risks:
  mean
                 Cov Sigma
                             CVaR
                                     VaR
0.1067 0.1067 0.7157 0.7157 1.6843 1.1471
```

Other non-linear Constraints: Value at Risk, Tracking Error, Drawdowns, ...



### Mixed Integer Programming ...

#### **Buy-In Threshold Constraints:**

These constraints define the minimum level at which an asset can be purchased. Its eliminates the problem of unrealistically small trades.

#### **Cardinality Constraints:**

These constraints restrict the number of stocks allowed in the portfolio

#### **Roundlot Constraints:**

Roundlots are used to define the basic unit of investment. Investors are allowed only to make transactions in multiples of the roundlots.

```
• • •
```

```
setSolver(spec) <- "solveRsymphony"
cons <- ...</pre>
```

is currently under implementation in Package fPortfolioAdvanced.



### Black - Litterman



#### **BLCOP**

#### **BLCOP**

is a contributed Package written by Francisco Gochez for Black-Litterman and Copula Opinion Pooling in Portfolio Optimization.

#### Black-Litterman

Fisher Black and Robert Litterman's 1992 goal wasto create a systematic method of specifying and then incorporating analyst/portfolio manager views into the estimation of market parameters for portfolio optimization.

#### Copula Opinion Pooling

is an alternative way with several advantages compared with Black-Litterman, Attilio Meucci 2005.

```
• • •
```

```
setType(spec) <- "BLCOP"
setViews(spec) <- ...</pre>
```

an interface is currently under implementation in Package fPortfolioAdvanced.



### Rolling Portfolio Backtests



#### *fPortfolioBacktest*

Portfolio Model

Example: Rolling Tangency CVaR Portfolio with box/group constraints

Specification the Backtest Settings

Run the Backtests

Smooth the Weights

Analyze the Performance

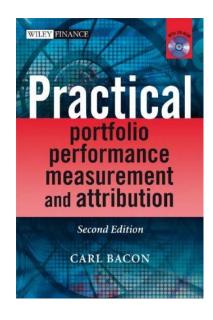
```
backtestSpec <-
portfolioBacktest(
 windows,
  strategy,
  smoother, ...)
rollingBacktest <-
portfolioBacktesting(
   formula,
   data, spec, constraints,
   backtest = backtestSpec, ...)
portfolioSmoothing(
   object = rollingBacktest,
   backtest = backtestSpec, ...)
portfolioPerformance(...)
```



### Rolling Performance Analysis ...



#### fPortfolioPerformance



Implements more than 100 traditional portfolio risk and performance measures from Carl Bacon's book, plus some more, e.g. robust risk measures, extreme value measures, copulae measures, ...

Preliminary version (without documentation) is available on demand.



### GCC Country Rotation



# MSCI GCC Gulf Cooperation Council Countries Indices

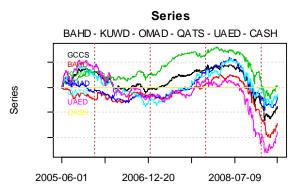
#### **Rolling Windows:**

Horizon 12m Shift 1m

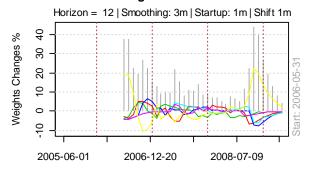
#### Portfolio Strategy:

MV Tangency Portfolio
Dynamic Horizon < 12M
Optimal Shrinkage Estimator
best of λ – 0 ... 1
Partial Cash Position
Max 30% Box Constraints

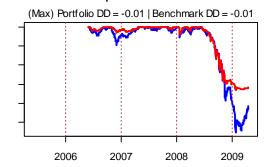
### Weights Smoothing:



#### Weights Rebalance

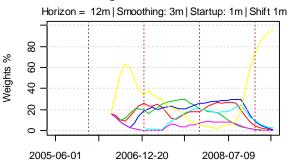


#### Drawdowns | Portfolio vs Benchmark

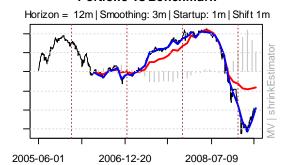


**Drawdowns** 

#### Weights Recommendation



#### Portfolio vs Benchmark



Cumulated



### Backtesting Results ...





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## Backtesting Results





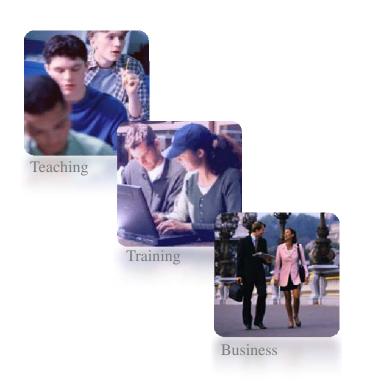
Theta Fund Management, Zurich

### Rmetrics



### open source software for computational finance and financial engineering





Thank you wuertz@phys.ethz.ch

### Rmetrics



### Rmetrics

### open source software for computational finance and financial engineering





### About Rmetrics ...





#### **Rmetrics**

is a collection of R packages for computational finance and financial engineering. It is based on the R language and the R run-time environment.



#### **Rmetrics**

is designed

as an Open Source Environment – you can look at any piece of the code as a Rapid Model Prototyping System – do in one day where others need one week as a Teaching Tool for "Computational Finance and Financial Engineering", but also a Code Archive for business use – copy and paste for free what you need



#### **Rmetrics**

tries to cover all major aspects of computational finance and financial engineering
Time and Date Management of Financial Time Series
Pricing and Valuation of Financial Instruments and Derivatives
Volatilty Modeling and Forecasting including GARCH Processes
Risk Management including Extreme Value Theory and Copulae
Asset Management and Portfolio Optimization together with Performance Analysis

...



### Time Line ...



1997	Starting with a	a Collection of	<b>SPlus Functions</b>

1999 Moving to R

2001 Creating Rmetrics Packages

2002 Adding to CRAN Packages

2003 Introducing R-sig-Finance / Private Repository – Martin Mächler

2004 Providing Debian Packages – Dirk Eddelbüttel

2007 Organizing the1st Rmetrics User and Developer Workshop

2008 Founding the Rmetrics Association / Offering Student Internships

2008 2<sup>nd</sup> Rmetrics Developer Workshop

2008 Joining R-forge / Rmetrics Repository

2009 3<sup>rd</sup> Rmetrics User and Developer Workshop

2009 First Rmetrics eBook "Portfolio Optimization with R/Rmetrics"



### Rmetrics Users Worldwide .





#### People use it in Education

Chicago Business School, University of Chicago University of Economics, Vienna Swiss Federal Administration, Berne Institute for Advanced Studies, Vienna Swiss Economic Institute, KOF ETH Zurich Swiss Banking Institute, University of Zurich

#### and in Business ...

Bank Clariden, Zurich
Bank of America, Chicago
Credit Suisse, Madrid,
European Central Bank, Frankfurt
Government Investment Corp,
Singapore
Lippers – Reuters, Dallas

. .



### R/Rmetrics Links





Download R Run-Time Environment and Rmetrics Packages: www.r-project.org



Get most recent updates from the Rmetrics Repository: <a href="https://r-forge.r-project.org">https://r-forge.r-project.org</a>



Find help from the Special Interest Group of R inFinance: https://stat.ethz.ch/mailman/listinfo/rmetrics-core https://stat.ethz.ch/mailman/listinfo/r-sig-finance



Visit the home of Rmetrics Association for Financial Computing:

www.rmetrics.org

### Rmetrics Association ...





The "Rmetrics Association" is a not-for-profit organization working in the public interest. It was founded May, 2008 as an association under Swiss law and has its seat in Zurich.

Rmetrics was born 1997 in the econphysics group of Dr. Diethelm Würtz at the Institute of Theoretical Physics. When Rmetrics was introduced it served as a teaching environment in computational finance and financial engineering.

Diethelm Würtz is Senior Scientist and Private Lecturer at the Physics Department and at the Curricuilum for Computational Science at the Swiss Federal Institute of Technology in Zurich.

#### The Rmetrics Association ...

- supports the Rmetrics project and other innovations in financial computing,
- ensures the continued development of the Rmetrics software packages,
- provides a reference point for individuals, institutions or commercial enterprises, that want to support or interact with the Rmetrics development community,
- encourages students to participate in internships,
- publishes eBooks covering user and programming guides,
- offers traineeships, and organizes meetings and workshops.



Swiss Federal Institute of Technology Zurich

## Rmetrics Activities ...

#### Open Source Software ...



· Install all Rmetrics Packages from CRAN More information at wiki metrics org ...

Download Rmetrics Packages from CRAN
Major Rinetrics packages and many contributed R packages related to
finance and econometrics can be downloaded from the CRAN server.

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- Download the R Environment from CRAN

Download Packages from the Portfolio Project
 Here you can download all packages used in the fimetres Portfolio Project. The versions of the packages offered in the download area are exactly these which we use.

#### Documentation, eBooks, Wiki, ...





Documentation

Rmetrics eBooks



#### Conferences, Workshops, Lectures, Seminars ...





Conferences Workshop Lectures Seminars ...

Meielisalp Workshop 2009

"Computational Physics and Econophysics" Lecture given by Diethelm Wurtz at ETH Zurich.

Go to the Course Catalogue ...



#### Meielisalp User and Developer Workshop





Meielisalp Workshop 2009

• The Workshop Focuses on ...

\*The Program Consists of ...

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. The Call for Papers Invites

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all Riffenters users and developers to submit abstracts preserting innovations or excelling applications of R and Celementers, financial and invited and applications of Celementers, financial and invited and applications of Celementers, and Celementers, and Celementers, and Celementers, and Celementers, and Time Bisales Data - Richous Statistics.





### Rmetrics Support ..









#### Donations ...

The non-profit Rmetrics
Association supports the open
source Rmetrics Software in the
public interest. Rmetrics has
expenses and it is hoped that
businesses that use it and make
money through it will contribute
back to help make Rmetrics the
best open source software in
computational finance and
financial engineering.



https://www.rmetrics.org