

# A Novel Maximum Power Point Tracking Technique for Solar Panels Using a SEPIC or Cuk Converter

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**Abstract**—A novel technique for efficiently extracting the maximum output power from a solar panel under varying meteorological conditions is presented. The methodology is based on connecting a pulse-width-modulated (PWM) dc/dc SEPIC or Cuk converter between a solar panel and a load or battery bus. The converter operates in discontinuous capacitor voltage mode whilst its input current is continuous. By modulating a small-signal sinusoidal perturbation into the duty cycle of the main switch and comparing the maximum variation in the input voltage and the voltage stress of the main switch, the maximum power point (MPP) of the panel can be located. The nominal duty cycle of the main switch in the converter is adjusted to a value, so that the input resistance of the converter is equal to the equivalent output resistance of the solar panel at the MPP. This approach ensures maximum power transfer under all conditions without using microprocessors for calculation. Detailed mathematical derivations of the MPP tracking technique are included. The tracking capability of the proposed technique has been verified experimentally with a 10-W solar panel at different insolation (incident solar radiation) levels and under large-signal insolation level changes.

**Index Terms**—dc-dc power conversion, maximum-power-point-tracking, photovoltaic.

## I. INTRODUCTION

SOLAR panel is the fundamental energy conversion component of photovoltaic (PV) systems [1], [2]. It has been used in many applications [3], such as aerospace industries, electric vehicles, communication equipment, etc. As the solar panels are relatively expensive, much research work has been conducted to improve the utilization of solar energy. Physically, the power supplied by the panels depends on many extrinsic factors, such as insolation (incident solar radiation) levels, temperature, and load condition. Thus, a solar panel is typically rated at an insolation level together with a specified temperature, such as 1000 W/m<sup>2</sup> at 25 °C. Its electrical power output usually increases linearly with the insolation and decreases with the cell/ambient temperature.

In practice, there are three possible approaches for maximizing the solar power extraction in medium- and large-scale PV systems. They are sun tracking, maximum power point

(MPP) tracking or both. For the small-scale systems, the use of MPP tracking only is popular for economical reasons. In the last two decades, various methods including the power-matching scheme [4]–[6], curve-fitting technique [7], [8], perturb-and-observe method [9]–[14], and incremental conductance algorithm [15]–[17] have been proposed for tracking the MPP of solar panels.

The power-matching scheme requires the selected solar panels to have suitable output characteristics [4], [5] or configurations [6] that can be matched with particular loads. However, these techniques only approximate the location of the MPP because they are basically associated with specific insolation and load conditions [17].

The curve-fitting technique requires prior examination of the solar panel characteristics, so that an explicit mathematical function describing the output characteristics can be predetermined. The method proposed in [7] and [8] is based on fitting the operating characteristic of the panel to the loci of the MPP of the PV systems. Although this technique attempts to track the MPP without computing the voltage–current product explicitly for the panel power, the curve-fitting technique cannot predict the characteristics including other complex factors, such as aging, temperature, and a possible breakdown of individual cells [7].

The perturb-and-observe (PAO) method is an iterative approach that perturbs the operation point of the PV system, in order to find the direction of change for maximizing the power [9]–[12]. It is operated by periodically perturbing the panel terminal voltage and comparing the PV output power with that of the previous perturbation cycle. Maximum power control is achieved by forcing the derivative of the power to be equal to zero under power feedback control. This has an advantage of not requiring the solar panel characteristics. However, this approach is unsuitable for applications in rapidly changing atmospheric conditions [17]. The solar panel power is measured by multiplying its voltage and current, either with a microprocessor or with an analog multiplier [10]. In [13] and [14], the tracking technique is based on the fact that the terminal voltage of the solar panels at MPP is approximately at 76% of the open-circuit voltage. Thus, in order to locate the MPP, the panel is disconnected from the load momentarily so that the open-circuit voltage can be sampled and kept as reference for the control loop.

The disadvantage of the PAO method can be improved by comparing the instantaneous panel conductance with the incremental panel conductance [15]–[17]. This method is the most accurate one among the above methods and is usually

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named as the incremental conductance technique (ICT). The input impedance of a switching converter is adjusted to a value that can match the optimum impedance of the connected PV panel. This technique gives a good performance under rapidly changing conditions. The implementation is usually associated with a microcomputer [15] or digital signal processor [17].

Concluding the above discussions, one of the most desirable approaches of implementing a MPP tracker is to use the ICT without requiring sophisticated digital sampling or mathematical manipulations. Moreover, the realization should be of low-cost and high accuracy and control capability. In this paper, a novel technique for efficiently maximizing the output power of a solar panel supplying to a load or battery bus under varying meteorological conditions is presented. The proposed MPP tracking is achieved by connecting a pulse-width-modulated (PWM) dc/dc SEPIC or Cuk converter between a solar panel and a load or battery bus. The converter is operating in discontinuous capacitor voltage (DCV) mode whilst its input current is kept continuous. The nominal duty cycle of the main switch in the converter is adjusted to a certain value, so that the input resistance of the converter is equal to the equivalent output resistance of the solar panel. This ensures the maximum power transfer. By modulating a small-signal sinusoidal perturbation into the duty cycle of the main switch and comparing the maximum variation in the input voltage and the voltage stress of the main switch, the MPP of the panel can be located. The tracking capability of the proposed technique has been verified experimentally with a 10-W solar cell panel at different insolation (incident solar radiation) levels and temperatures and under different large-signal insolation changes.

## II. MODELING OF THE CONVERTER INPUT AT MPP

### A. Derivation of the Required Dynamic Input Characteristics of a Converter at MPP

Fig. 1 shows an equivalent circuit of the solar panel connecting to a converter. The equivalent circuit for solar panels generally consists a current source shunted by a diode and a resistor and with an output series resistor [18], [19]. However, a Thevenin's equivalent circuit is used to represent the solar panel at the MPP in this case. The solar panel is represented by a voltage source  $v_g$  connecting in series with an output resistance  $r_g$ . The input voltage and the equivalent input resistance of the converter are  $v_i$  and  $r_i$ , respectively. As the input power  $P_i$  to the converter is equal to the output power  $P_o$  of the solar panel

$$P_i = P_o = \frac{v_i^2}{r_i}. \quad (1)$$

The rate of change of  $P_i$  with respect to  $v_i$  and  $r_i$  can be shown to be

$$\partial P_i = 2 \frac{v_i}{r_i} \partial v_i - \frac{v_i^2}{r_i^2} \partial r_i. \quad (2)$$

At the MPP, the rate of change of  $P_i$  equals zero. Hence

$$\partial P_i = 0 \Rightarrow \frac{\partial v_i}{\partial r_i} = \frac{V_i}{2R_i} \quad (3)$$

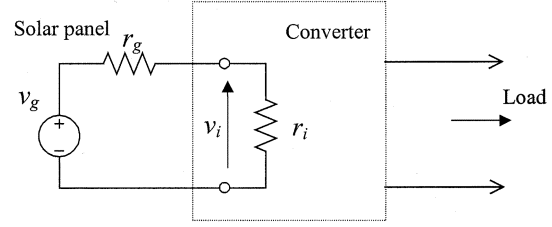


Fig. 1. Equivalent circuit of a solar panel connecting to a converter.

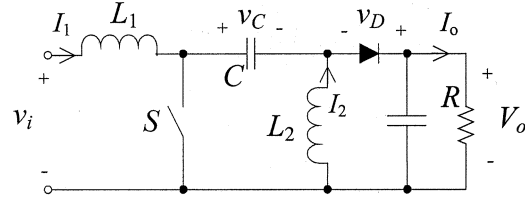


Fig. 2. Circuit diagram of a SEPIC converter.

where  $V_i$  and  $R_i$  are the input voltage and the input resistance at MPP.

The above equation gives the required dynamic input characteristics of the converter at the MPP. The input voltage will have a small-signal variation of  $\delta v_i$  if the input resistance is subject to a small-signal change of  $\delta r_i$ . That is

$$\frac{\delta v_i}{\delta r_i} \approx \frac{\partial v_i}{\partial r_i} = \frac{V_i}{2R_i}. \quad (4)$$

### B. Input Resistance and Voltage Stress of a SEPIC Converter

Fig. 2 shows the circuit diagram of a SEPIC converter. If the converter is operated in DCV mode [20], there are in total three circuit topologies in one switching cycle. The sequence of operation and the waveforms are shown in Fig. 3. If the two inductor currents (i.e.,  $I_1$  and  $I_2$ ) are assumed to be constant, the capacitor voltage  $v_C(t)$  and diode voltage  $v_D(t)$  in the respective three operating intervals can be expressed as

$$v_C(t) = \begin{cases} \frac{I_1(1-d)T_S}{C} - V_o - \frac{I_2}{C}t, & 0 < t < d_1T_S \\ -V_o, & d_1T_S < t < dT_S \\ \frac{I_1}{C}(t - dT_S) - V_o, & dT_S < t < T_S \end{cases} \quad (5a)$$

$$v_D(t) = \begin{cases} V_o + v_C(t), & 0 < t < d_1T_S \\ 0, & d_1T_S < t < T_S. \end{cases} \quad (5b)$$

As  $v_C(d_1T_S) = -V_o$

$$\begin{aligned} \frac{I_1(1-d)T_S}{C} - V_o - \frac{I_2}{C}d_1T_S &= -V_o \\ \Rightarrow d_1 &= \frac{I_1}{I_2}(1-d). \end{aligned} \quad (6)$$

Under the steady-state condition, the average voltage across  $L_2$  is zero. Hence, the  $V_o$  is equal to the average value of  $v_D$ . That is

$$V_o = \frac{1}{T_S} \int_0^{dT_S} v_D(t)dt = \frac{T_S}{2C} I_1(1-d)d_1. \quad (7)$$

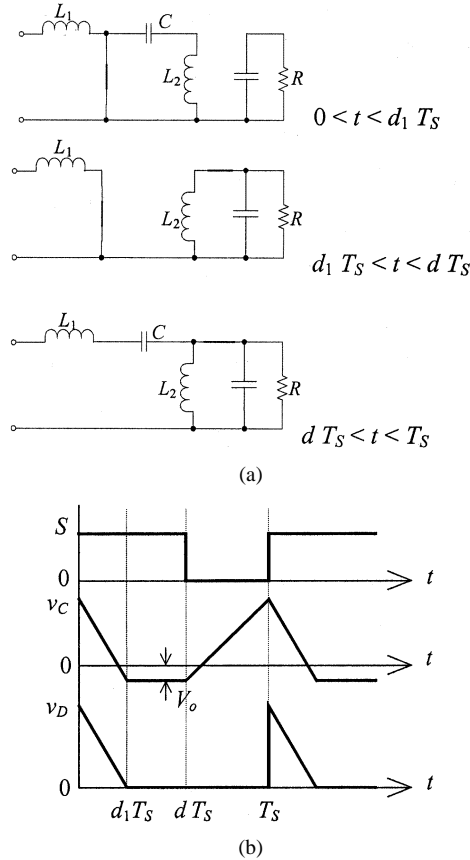


Fig. 3. Principles of operation. (a) Topology sequence. (b) Theoretical waveforms of  $v_C$  and  $v_D$ .

As the average voltage across  $L_1$  is also zero

$$v_i = \frac{1}{T_S} \int_0^{T_S} v_C(t) dt = \frac{T_S}{2C} I_1 (1-d)^2. \quad (8)$$

Hence, the input resistance  $r_i$  of the converter is

$$r_i = \frac{v_i}{I_1} = \frac{(1-d)^2}{2Cf_S} \quad (9)$$

where  $f_S = 1/T_S$  is the switching frequency.

Moreover, the voltage stress across the main switch  $S$   $v_{\text{stress}}$ , equals

$$v_{\text{stress}} = v_C(T_S) + V_o = \frac{I_1}{C} (1-d)T_S = \frac{2}{1-d} v_i. \quad (10)$$

In the proposed technique, (9) and (10) will be used to locate the MPP of a solar panel. As shown in [21], the input resistance and the voltage stress across the main switch of a Cuk converter is same as (9) and (10), respectively. Hence, both SEPIC and Cuk converters exhibit similar  $r_i$  and  $v_{\text{stress}}$ , and thus, they can be used to locate the MPP.

### C. Dynamic Input Resistance of the Converter Under Perturbation

If a small-signal sinusoidal perturbation  $\delta d$  is injected into  $d$

$$d = D + \delta d = D + \hat{d} \sin \omega t \quad (11)$$

where  $\omega = 2\pi f$ , and  $D$  is the nominal duty cycle at the MPP, and  $\hat{d}$  and  $f$  are the amplitude and frequency of the injected perturbation, respectively. In the following derivations, the value of  $f$  is assumed to be much smaller than  $f_S$ .

By substituting (11) into (9), the input resistance can be expressed as

$$r_i = \frac{(1-D)^2}{2f_S C} - \frac{(1-D)}{f_S C} \hat{d} \sin \omega t + \frac{1}{2f_S C} \hat{d}^2 \sin^2 \omega t. \quad (12)$$

Hence,  $r_i$  includes two main components, namely, the static resistance  $R_i$  at the MPP and the dynamic resistance  $\delta r_i$  around the MPP. Each one can be expressed as

$$R_i = \frac{(1-D)^2}{2f_S C} \quad (13)$$

and

$$\delta r_i = -\frac{(1-D)}{f_S C} \hat{d} \sin \omega t + \frac{1}{2f_S C} \hat{d}^2 \sin^2 \omega t. \quad (14)$$

By substituting (14) into (4), the input voltage variation  $\delta v_i$  at the MPP can be expressed as

$$\delta v_i = \delta \bar{v}_i + \delta \tilde{v}_i \quad \text{and} \quad \delta \tilde{v}_i = \delta \tilde{v}_{i,1} + \delta \tilde{v}_{i,2} \quad (15)$$

where  $\delta \bar{v}_i = (V_i/(4(1-D)^2)) \hat{d}^2$ ,  $\delta \tilde{v}_{i,1} = -(V_i/(1-D)) \hat{d} \sin \omega t$ , and  $\delta \tilde{v}_{i,2} = -(V_i/(4(1-D)^2)) \hat{d}^2 \cos 2\omega t$ .

$\delta v_i$  is maximum when

$$\omega t = \frac{(2n+1)}{2} \pi, \quad n = 1, 3, 5, \dots \quad (16)$$

Its maximum value  $\delta v_{i,\text{max}}$  can be shown to be equal to

$$\delta v_{i,\text{max}} = \frac{V_i}{(1-D)} \hat{d} + \frac{V_i}{2(1-D)^2} \hat{d}^2. \quad (17)$$

Considering the ac-component of  $\delta v_i$ , its maximum value  $\delta \tilde{v}_{i,\text{max}}$  can be expressed as

$$\delta \tilde{v}_{i,\text{max}} = \delta \tilde{v}_{i,m1} + \delta \tilde{v}_{i,m2} \quad (18)$$

where  $\delta \tilde{v}_{i,m1} = (V_i/(1-D)) \hat{d}$ , and  $\delta \tilde{v}_{i,m2} = (V_i/(4(1-D)^2)) \hat{d}^2$ .

The ratio between the magnitude of  $\delta \tilde{v}_{i,m1}$  and  $\delta \tilde{v}_{i,m2}$   $\Re$  is

$$\Re = \left| \frac{\delta \tilde{v}_{i,m2}}{\delta \tilde{v}_{i,m1}} \right| = \frac{\hat{d}}{4(1-D)}. \quad (19)$$

$\Re$  is an index showing the spectral quality of the input voltage variation at the frequency of the injected perturbation with respect to the amplitude of the perturbation. The smaller the value of  $\Re$ , the more dominant the component of the injected frequency in  $\delta v_i$  will be.

### D. Voltage Stress of the Main Switch Under Perturbation

The maximum value of  $v_{\text{stress}}$  (i.e.,  $v_{\text{stress,max}}$ ) under a sinusoidal perturbation can be obtained by substituting  $d = D + \delta d$

and  $v_i = V_i + \delta v_i$  into (10). Thus

$$\begin{aligned}
 v_{\text{stress}} &= \frac{2}{(1-D-\delta d)} (V_i + \delta v_i) \\
 &= \frac{2}{(1-D)} \frac{1}{1 - \frac{\delta d}{(1-D)}} (V_i + \delta v_i) \\
 &= \frac{2}{(1-D)} \left[ 1 + \frac{1}{(1-D)} \delta d + \frac{1}{(1-D)^2} \delta d^2 + \dots \right] \\
 &\quad \cdot (V_i + \delta v_i) \\
 &= \frac{2}{(1-D)} V_i + \frac{2\delta d}{(1-D)^2} \left( \frac{1}{1 - \frac{\delta d}{1-D}} \right) \\
 &\quad \cdot (V_i + \delta v_i) + \frac{2}{1-D} \delta v_i \\
 &= V_{\text{stress}} + \delta v_{\text{stress}}
 \end{aligned} \tag{20}$$

where  $V_{\text{stress}} = (2V_i/(1-D))$  and

$$\delta v_{\text{stress}} = \frac{2\delta d}{(1-D)^2} \left( \frac{1}{1 - \frac{\delta d}{1-D}} \right) (V_i + \delta v_i) + \frac{2}{1-D} \delta v_i.$$

The maximum value of  $v_{\text{stress}}$ ,  $v_{\text{stress, max}}$ , can be approximated by substituting  $\delta d = \hat{d}$  and  $\delta v_i = \delta \tilde{v}_{i, \text{max}}$  in (17) into (18). It can be shown that

$$v_{\text{stress, max}} = \frac{2V_i}{(1-D)} [1 + \varepsilon(D)] \tag{21}$$

where

$$\varepsilon(D) = \frac{2\hat{d} \left( 1 - D + \frac{\hat{d}}{4} \right)}{(1-D)(1-D-\hat{d})}.$$

Comparing (18) and (21), it can be shown that

$$\begin{aligned}
 \delta \tilde{v}_{i, \text{max}} &= \beta v_{\text{stress, max}} \\
 \beta &= \frac{\hat{d}}{2} \left[ \frac{(1-D-\hat{d})(1-D+\frac{\hat{d}}{4})}{(1-D)^2 + \hat{d}(1-D+\frac{\hat{d}}{2})} \right]
 \end{aligned} \tag{22}$$

at the MPP. If  $\hat{d} \ll 1-D$ ,  $\beta \cong \hat{d}/2$ . Thus,  $\delta \tilde{v}_{i, \text{max}}$  and  $v_{\text{stress, max}}$  form a relatively constant ratio of  $\beta$  at the MPP.

The control mechanism for locating the MPP is illustrated in Fig. 4. First, the error amplifier compares the maximum input ripple voltage (i.e.,  $\delta \tilde{v}_{i, \text{max}}$ ) and the attenuated switch voltage stress (i.e.,  $\beta' v_{\text{stress, max}}$ ) and generates an error signal. Theoretically,  $\beta'$  should be equal to  $\beta$  in (22). However, as  $\beta$  is dependent on  $D$ , a constant value is used to represent it for the sake of simplicity in the implementation. Its value is equal to  $r_2/(r_1 + r_2)$  so that

$$\beta' = \frac{r_2}{r_1 + r_2} = \frac{1}{D_{\text{max}} - D_{\text{min}}} \int_{D_{\text{min}}}^{D_{\text{max}}} \beta(D) dD \tag{23}$$

where  $D_{\text{min}}$  and  $D_{\text{max}}$  are the minimum and maximum duty cycle of the main switch, respectively.

$D_{\text{max}}$  is determined by the minimum input resistance  $R_{i, \text{min}}$  of the converter, which is also the minimum equivalent output resistance of the solar panel. By using (9)

$$D_{\text{max}} = 1 - \sqrt{2R_{i, \text{min}} C f_S}. \tag{24}$$

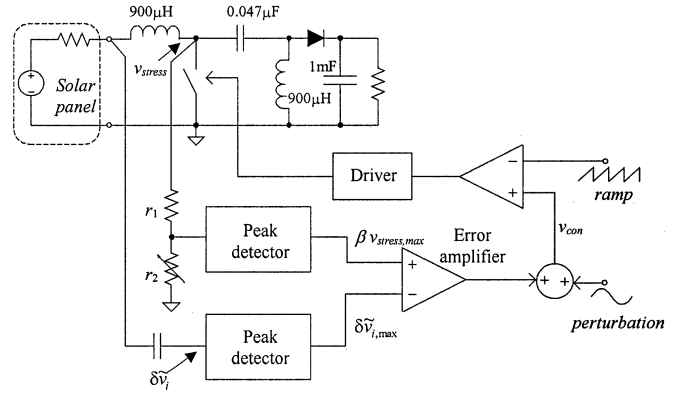


Fig. 4. Block diagram of the proposed MPP tracking method.

For the converter operating in DCV mode, we must ensure that  $d_1 \leq d$ . The output current  $I_o$  can be expressed as

$$\begin{aligned}
 I_o &= \frac{V_o}{R} = (1-d)I_1 + (1-d_1)I_2 \\
 \Rightarrow I_2 &= \frac{1}{1-d_1} \left[ \frac{V_o}{R} - (1-d)I_1 \right].
 \end{aligned} \tag{25}$$

$d_1$  is determined by substituting (6) and (7) into (25), and thus

$$D_{\text{min}} = \sqrt{2RCf_S}. \tag{26}$$

Second, the error signal is superimposed with a small-signal sinusoidal perturbation. Third, the combined signal  $v_{\text{con}}$  is compared to a ramp function to generate a PWM gate signal to the main switch.

The tracking action can be illustrated by considering the values of  $\delta \tilde{v}_{i, \text{max}}$  and  $v_{\text{stress, max}}$  when  $d$  does not equal  $D$ . Based on Fig. 1 and using (9), it can be shown that

$$\begin{aligned}
 v_i &= \frac{r_i}{r_i + r_g} v_g \\
 \Rightarrow \delta v_i &= -\frac{2r_i r_g}{(r_i + r_g)^2} \frac{v_g}{(1-d)} \delta d.
 \end{aligned} \tag{27}$$

Thus

$$\delta \tilde{v}_{i, \text{max}} = \frac{2\alpha}{(1+\alpha)^2} \frac{v_g}{(1-d)} \hat{d} \tag{28}$$

where  $\alpha = r_i/r_g = [(1-d)/(1-D)]^2$ .

By substituting (27) and (28) into (20),  $v_{\text{stress, max}}$  is equal to

$$v_{\text{stress, max}} = \frac{2\alpha [(1+\alpha)(1-d) + 2\hat{d}]}{(1-d)(1-d-\hat{d})(1+\alpha)^2} v_g. \tag{29}$$

Referring to (22), if  $\hat{d} \ll 1-d$ ,  $\beta' \cong \hat{d}/2$ . It can be shown that

$$\begin{aligned}
 \Phi &= \frac{\beta' v_{\text{stress, max}}}{\delta \tilde{v}_{i, \text{max}}} \cong \frac{1}{2} \left[ \frac{(1+\alpha)(1-d) + 2\hat{d}}{1-d-\hat{d}} \right] \\
 &\cong \frac{1}{2} (1+\alpha) = \frac{1}{2} \left[ 1 + \left( \frac{1-d}{1-D} \right)^2 \right].
 \end{aligned} \tag{30}$$

When  $r_i$  equals  $r_g$  (i.e.,  $\alpha = 1$ ),  $\Phi$  becomes unity. This is the condition when the converter is at the MPP. If  $d$  is smaller than  $D$ ,  $r_i$  will be larger than  $r_g$  (i.e.,  $\alpha > 1$ ), and  $\Phi$  becomes larger than unity. The error amplifier will then generate a signal so as

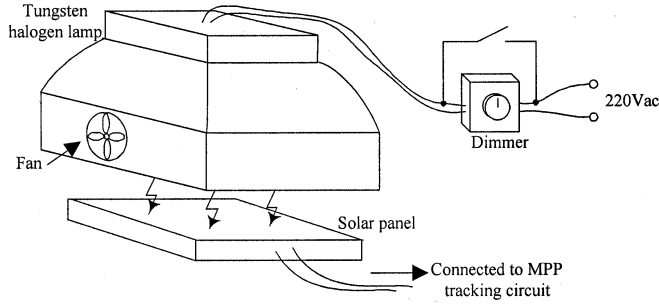


Fig. 5. Experimental setup of the solar panel for testing the proposed MPP tracking technique.

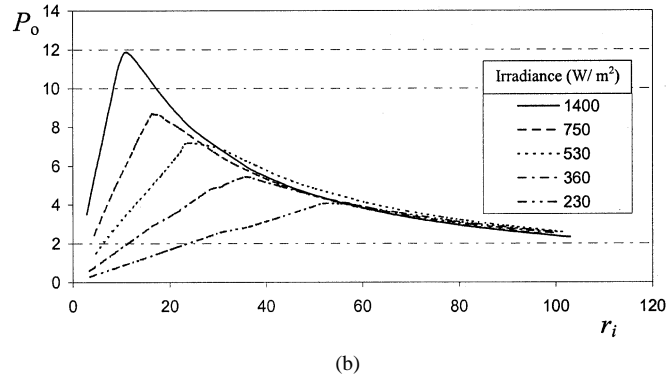
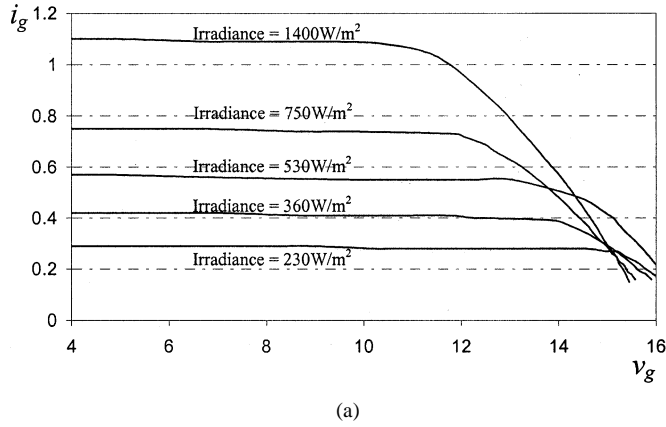


Fig. 6. Solar panel characteristics at different  $P_{lamp}$ . (a)  $i_g$  versus  $v_g$ . (b)  $P_o$  versus  $r_i$ .

to increase the duty cycle. Conversely, if  $d$  is larger than  $D$ ,  $r_i$  will be smaller than  $r_g$  (i.e.,  $\alpha < 1$ ).  $\Phi$  becomes less than unity. The error amplifier will then generate a signal so as to decrease the duty cycle. The above regulatory actions cause the feedback network to adjust the duty cycle, in order to make  $\Phi = 1$  or  $r_i = r_g$ .

### III. EXPERIMENTAL VERIFICATIONS

A control experiment has been performed using a solar panel Siemens SM-10 with a rated output power of 10 W. The setup is shown in Fig. 5 and the component values of the SEPIC converter are shown in Fig. 4. The output resistance  $R$  equals 10  $\Omega$ . The switching frequency is set at 80 kHz, and the injected sinusoidal perturbation frequency is 500 Hz. The radiation level illuminated on the solar panel is adjusted by controlling

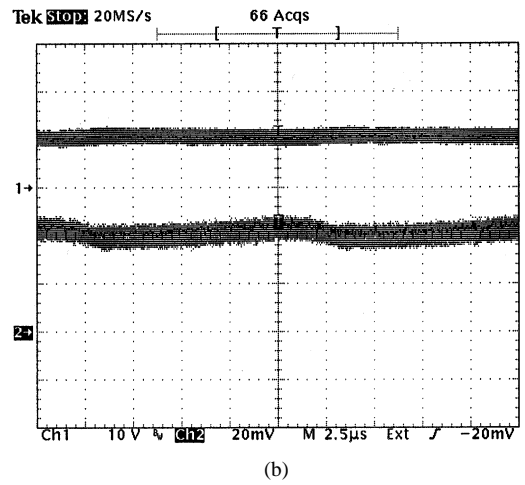
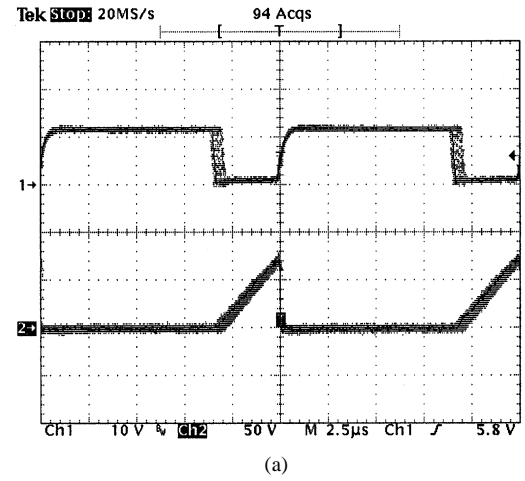


Fig. 7. Detailed experimental waveforms of the SEPIC converter. (a) Ch1: gate signal, 10 V/div; Ch2: switch voltage stress, 50 V/div. (b) Ch1: input voltage, 10 V/div; Ch2: input current, 0.5 A/div.

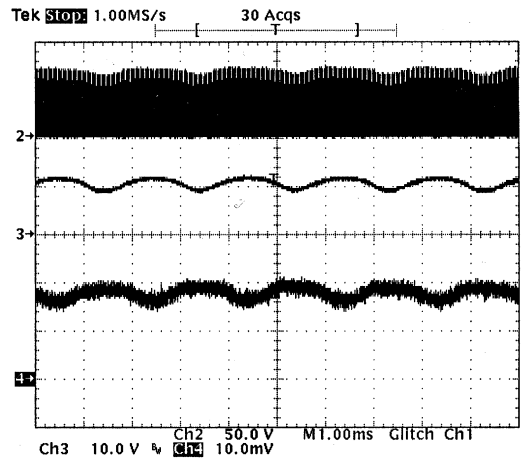


Fig. 8. Macroscopic view of the experimental waveforms of the SEPIC converter. Ch2: switch voltage stress, 50 V/div; Ch3: input voltage, 10 V/div; Ch4: input current, 0.5 A/div.

the power of a 900 W halogen lamp using a light dimmer. The bypass switch is used to give the maximum brightness from the lamp for studying the transient response. The surface temperature of the panel is maintained at about 40 °C. The measured  $v_g - i_g$  characteristics and the output power versus

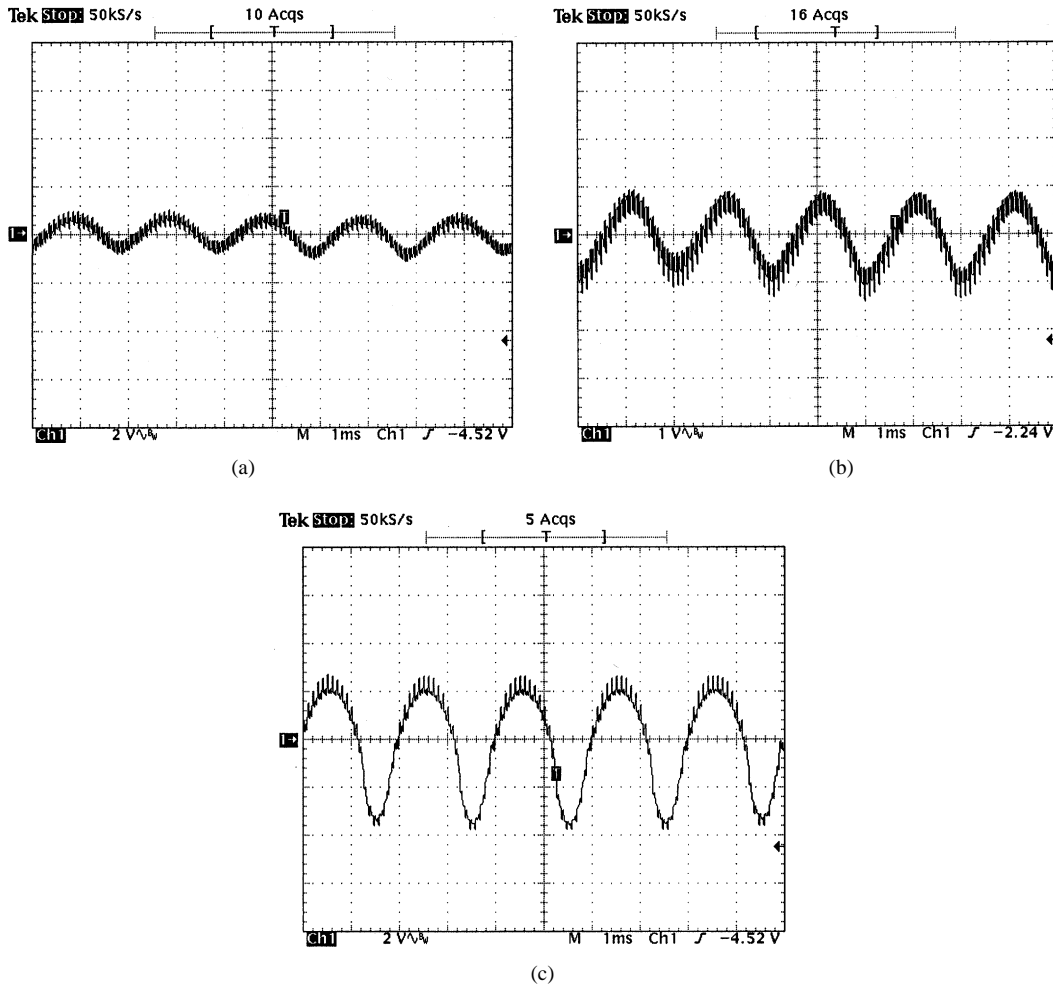


Fig. 9. Experimental waveforms of  $\delta \bar{v}_i$  with respect to different value of  $\mathcal{R}$ . (a)  $\mathcal{R} = 0.02$ . (b)  $\mathcal{R} = 0.05$ . (c)  $\mathcal{R} = 0.1$ .

the terminal resistance of the solar panel at different insolation levels are shown in Fig. 6(a) and (b), respectively. Under a given insolation level, it can be seen that the panel output power will be at its maximum under a specific value of the terminal resistance. When the irradiance is  $1400 \text{ W/m}^2$ , the required terminal resistance is  $14 \Omega$ , in order to extract maximum power from the solar panel. Thus, by applying (24) and (26),  $D_{\min}$  and  $D_{\max}$  equal 0.274 and 0.675, respectively. Based on (9), the variation of the input resistance is between 14 and  $70 \Omega$ , which is well within the required tracking range of the input resistance shown in Fig. 6(b).

Detailed experimental waveforms of the gate signal, the switch voltage stress, the converter input terminal voltage, and the input inductor current in one switching cycle at the maximum lamp power are shown in Fig. 7. Macroscopic views of the switch voltage stress, input voltage, and input current are shown in Fig. 8. It can be seen that a low-frequency variation of 500 Hz is superimposed on all waveforms. They are all in close agreement with the theoretical ones. In addition, the input current is continuous. Thus, the proposed MPP tracker is better than the one using classical buck-type converter [1], which takes pulsating input current. Moreover, it is unnecessary to interrupt the system, in order to test the open-circuit terminal voltage of the solar panel as in [13] and [14].

Fig. 9 shows the ac-component of the converter input terminal voltage with  $\mathcal{R}$  equal to 0.02, 0.05, and 0.1, respectively. As  $\mathcal{R}$  increases, the ac-component will be distorted because the second-order harmonics become dominant in (15).

In order to observe the feedback action of the proposed approach under a large-signal variation in the radiation level from 360 to  $1400 \text{ W/m}^2$ . The transient waveform of the feedback signal is shown in Fig. 10. The settling time is about 0.4 s. Based on the results in Fig. 6(b), a comparison of the maximum extractable power from the solar panel and the measured output power with the proposed control scheme under different insolation levels is shown in Fig. 11. It can be seen that the proposed control technique can track the output power of the panel with an error of less than 0.2 W. A major reason for the discrepancy is due to the variation of  $\beta$  with respect to the duty cycle shown in (23), which will directly affect the tracking accuracy.

#### IV. CONCLUSION

A novel technique using a SEPIC or Cuk converter to efficiently track the MPP of a solar panel has been presented. The technique is simple and elegant and does not require complicated mathematical computation, hardware implementation,

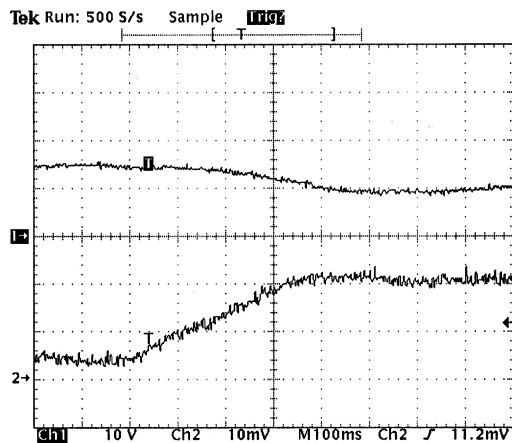


Fig. 10. Transient waveforms of the SEPIC converter when  $P_{lamp}$  is subject to a change from 500 to 900 W. Ch1: input voltage, 10 V/div. Ch2: input current, 0.5 A/div.

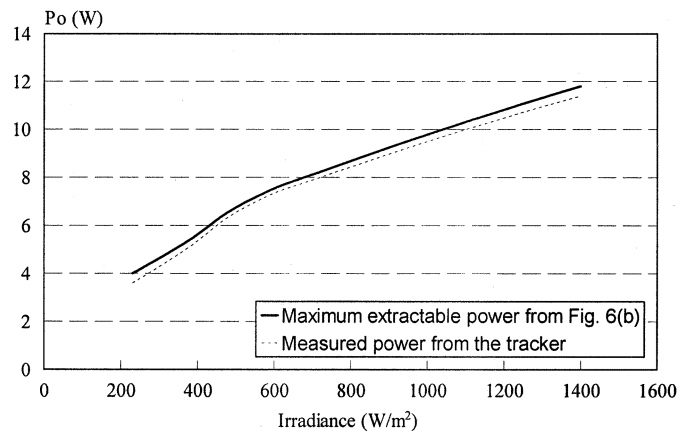


Fig. 11. Comparison of maximum solar panel output power using the proposed method and the maximum extractable value in Fig. 6(b) under different insolation.

microprocessor, or digital signal processor. The tracking capability of the proposed technique has been verified experimentally with a 10-W solar panel at different radiation levels. Compared to many existing methods, the proposed technique is unnecessary to

- 1) perform digital sampling of the converter parameters;
- 2) perform sophisticated mathematical computations of the panel output power;
- 3) approximate the panel output characteristics.

Hence, it can be used under a wide range of meteorological conditions. We have applied for a U.S. patent for this technique [22].

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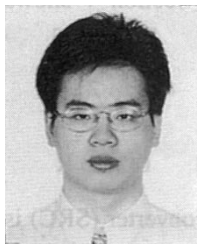
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