

Problems for midterm

Chapter 1.

1. (Birthday)

Chapter 2.

1. **(Poisson + Conditioning)** In your pocket there is a random number N of coins, where N has the Poisson distribution with parameter λ . You toss each coin once, with heads showing with probability p each time. Show that the total number of heads has the Poisson distribution with parameter λp .

Chapter 3.

1. (Birthday)
2. **(Expectation and variance of matchings)** Let S_n denotes the number of matchings of a random permutation of n cards. Compute $\mathbb{E}(S_n)$ and $\text{Var}(S_n)$.
- 3.