

MEE4099 Capstone Project Review 1 Report

Project Title:

Magnetic Mirror Effect in Magnetron Plasma: Modeling of Plasma Parameters

Project ID: 21BTECH10051

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1 Introduction

One of the team members- 18BME2104 Kaushal studied the class MEE4005 Surface Engineering taught by Professor Sitaram Dash- our internal guide during the Fall Semester 2021. Many interesting plasma based surface engineering techniques were studied during the class, one such technique being Magnetron Sputtering. This inspired the study of plasma in this project.

1.1 Plasma

One comes across many definitions of plasma including: Fourth state of matter, Ionized gas, etc. However, it is best to describe plasma with some characteristic parameters, when one attempts to describe a plasma quantitatively. Some quantities that help define a plasma are:

1. Number density, n

Number density of a plasma describes the number of particles per unit volume. Plasma contains charged particles or ionized species. However, a plasma might at the same time also contain neutral atoms and molecules but also particles of different species- charged and neutral. If multiple species are contained in a plasma system, number densities of each species could be used to describe the system. For example, a plasma may contain electrons, charged ions and neutral atoms and molecules. Mass density ρ is defined as $\rho := mn$ and is often used alongside number density, where m is the mass of the species.

2. Ionization, α

Defined as $\alpha := \frac{n_{charged}}{n_{charged} + n_{neutral}}$, the ionization of a plasma describes the fraction of charged particles, with $\alpha = 1$ meaning that all the particles are charged and $\alpha = 0$ meaning that all the particles are neutral.

3. Temperature, T

The temperature of a plasma describes the average kinetic energy of the particles in the plasma. When a gas is ionized to form a plasma, the ionization α can depend on the temperature of the plasma.

4. Mean free path, λ_{mfp}

The gas-like behavior of a plasma is characterized by mean free path of particles much larger than the scale of the plasma. The mean free path is influenced by the temperature of the plasma. The mean free path and the thermal velocity of the particles as described by the temperature, are related by the timescale of collisions as $\lambda := v_{th}\tau$ where τ is the timescale of collisions.

5. Debye Length, λ_D

In a plasma, electrostatic Coulomb interactions between charged particles compete with random thermal speed of the particles described by the temperature of the plasma. The Debye sphere is an imaginary sphere around a charged particle, where oppositely charged particles are attracted and in doing so screen the charge of the central particle to the outer plasma so that the electrostatic influence of a particle is limited to the Debye sphere surrounding it. This is why plasma's are often said to be Quasi-neutral as charge screening leads to a neutral behavior electrostatically on a scale much larger than the Debye length. The Debye length is defined as the radius of the Debye sphere.

6. Plasma beta parameter, β

The beta parameter defined as $\beta := \frac{8\pi nT}{B^2}$ describes the ratio of the thermal and magnetic energies of the plasma, as particles in random thermal motions compete with the Lorentz force.

Many other parameters describe a plasma including several electrodynamic quantities.

1.2 Laboratory Plasma

Laboratory plasmas are often characterized by some properties like:

- High ionization fraction
- Sub atmospheric pressure required to sustain ionization
- Temperature range : 1000 - 30000 K

Many surface engineering processes use plasmas to obtain high performance coatings. Some processes that use plasma are:

1. Plasma Immersion Ion Implantation
2. Plasma Enhanced Chemical Vapor Deposition
3. Magnetron Sputtering (PVD)
4. Air Plasma Spray (Spray technique)
5. Plasma Transferred Arc (Hardfacing technique)

1.3 Physical Vapor Deposition

Physical Vapor Deposition(PVD) is a family of surface engineering techniques where thin film coatings are grown on the surface of a specimen, in a vacuum chamber. Particles from a vapor move around on the surface of the specimen as random walkers and eventually get trapped in strained pockets producing nucleation site for the growth of a film. Most PVD techniques fall under either of the two categories:

1. Evaporation techniques

Evaporation techniques involve heating the material to a high temperature when it forms vapor and the particles in the vapor are coated on the substrate. It is for that reason that evaporation techniques are called hot techniques. Semiconductors like Si/Ge, insulators like oxides and metals like Tungsten are often coated on substrates using evaporation techniques.

2. Sputtering techniques

Sputtering techniques on the other hand are known as cold techniques. Sputtering techniques use a high energy beam to remove material from a target and the removed material is coated on the required substrate.

1.4 Magnetron Sputtering

Magnetron sputtering is a sputtering technique where the sputtered ions form a magnetically confined plasma. The plasma, controlled by magnetic fields, transports the ions to the surface of the substrate forming the coating.

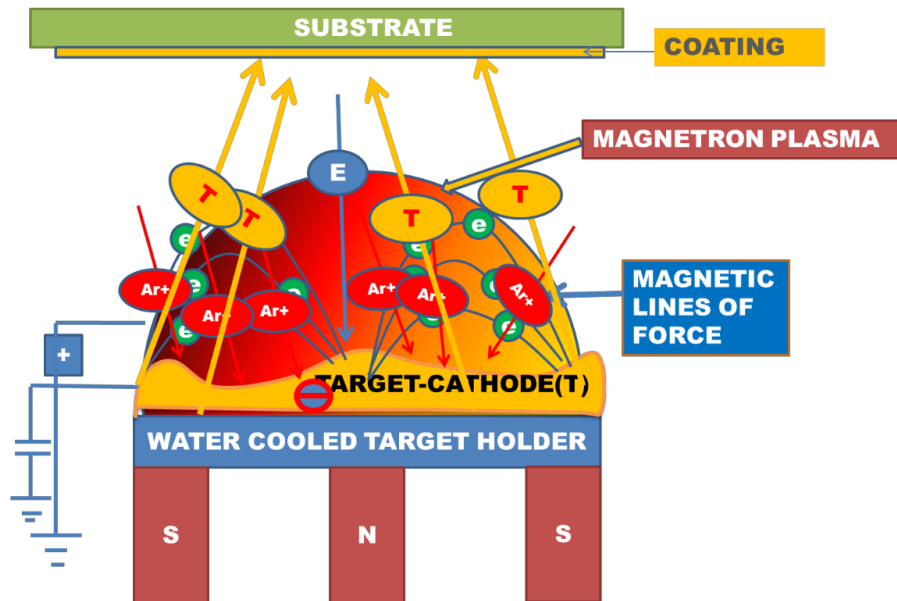


Figure 1: Magnetron Sputtering system. credit: [1]

1.5 Magnetic Mirror

The magnetic mirror effect can first be illustrated with a single particle. For the simple case, it is assumed that there is no electric field acting on the particle, the magnetic field is cylindrically symmetric and the gradient of the magnetic field is only along the axial direction of the cylinder, the z direction. The magnetic moment

$$\mu = \frac{mv_{\perp}^2}{2B_z}$$

of the particle is an adiabatic invariant of the particle motion and hence is approximately conserved for a magnetic field whose z component B_z does not vary too much. The kinetic energy

$$KE = \frac{1}{2}mv^2$$

of the particle is also approximately conserved. Writing $v_{\perp} = v \sin \theta$,

$$\frac{\mu}{KE} = \frac{\sin^2 \theta}{B_z}$$

is also a conserved quantity. This means that as B increases (within a small range), $\sin^2 \theta$ increases as well and so does $|\sin \theta|$ which means that $|v_{\perp}|$ increases and since v is conserved, v_{\parallel} decreases to zero. When $v_{\parallel} = 0$, the particle is no longer moving in the z direction, but is moving with velocity v in the plane perpendicular to z direction. The v_{\parallel} then increases in the opposite direction as the particle moves towards decreasing B because of the Lorentz force. Such a particle is seen as being reflected due to the configuration of the magnetic field and hence such a configuration of the magnetic field is called a magnetic mirror. Particles whose v_{\parallel} does not decrease to 0 while the value of B is decreasing, escape from the magnetic mirror configuration.

A magnetic mirror configuration is important in a magnetic plasma trap chamber such as that used in Magnetron sputtering. Particles in a plasma have different speeds depending on the initial distribution which is based on parameters like the plasma temperature. The speeds of particles change depending on the electric and magnetic fields. Based on the magnetic mirror effect, one can determine which particle (having certain velocities) can escape the magnetic trap and which of those are reflected. The less the particles escape the magnetic trap, the more of the flux is used in forming coatings and less of the ionized gas is wasted. This is very useful in understanding the required gas supply and rate of deposition.

2 Literature Review

A large part of the literature review for the project consisted of studying basic plasma physics in order to understand how we could formulate the project and proceed ahead.

2.1 Plasma as a system

Various models are used to describe Plasma as a system. Some of the common approaches are:

1. Single particle description

This model is used to describe the motion of a charged particle under the influence of electric and magnetic fields. The particle's motion is described by the Lorentz force

$$\frac{d\mathbf{v}}{dt} = \frac{q}{m} (\mathbf{E} + \mathbf{v} \times \mathbf{B}) \quad (1)$$

Describing many particles evolving under the influence of Lorentz force, it is easy to describe a plasma assuming that the mean free path of the particles is much larger than the dimensions of the chamber; meaning that particles hardly ever collide. This is to say that in the simplest case, under this model particles evolve under the influence of electric and magnetic fields but the particles do not produce any electric and magnetic fields of their own or affect the external applied fields and hence also do not interact with other particles.

2. Kinetic theory

The kinetic theory describes the plasma as collection of particles whose state (position and velocity) is treated as a random variable with a density function

$f(x, y, z, v_x, v_y, v_z, t)$ which describes the number of particles at position (x, y, z) at time t with velocities between v_x and $v_x + dv_x$, v_y and $v_y + dv_y$, v_z and $v_z + dv_z$ in directions x , y and z respectively. For a simpler notation $f(x, y, z, v_x, v_y, v_z, t)$ is denoted as $f(\mathbf{r}, \mathbf{v}, t)$. The expression

$$\int_{all} dv_x \int_{all} dv_y \int_{all} dv_z f(\mathbf{r}, \mathbf{v}, t)$$

gives the number of particles at position \mathbf{r} , at time t . For a simple choice of notation, it is often written as

$$\int_{all} d^3v f(\mathbf{r}, \mathbf{v}, t) \quad \text{or} \quad \int_{all} d\mathbf{v} f(\mathbf{r}, \mathbf{v}, t)$$

A density function is said to be normalized if

$$\int_{all} d\mathbf{v} f(\mathbf{r}, \mathbf{v}, t) = 1$$

Such a density function is also denoted with a hat as $\hat{f}(\mathbf{r}, \mathbf{v}, t)$.

The average velocity \bar{v} for a density function $\hat{f}(\mathbf{r}, \mathbf{v}, t)$ is calculated as

$$\int_{all} d\mathbf{v} \mathbf{v} f(\mathbf{r}, \mathbf{v}, t)$$

Various other features of the distribution are: the Root Mean Square velocity v_{rms} , the average absolute velocity $|\bar{v}|$, the average velocity in z direction \bar{v}_z , etc.

The evolution of the particles is described as the changing of the density function. Boltzmann equation is often used to describe this dynamics:

$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \nabla f + \frac{\mathbf{F}}{m} \cdot \partial_{\mathbf{v}} f = \left(\frac{\partial f}{\partial t} \right)_c$$

3. Fluid model

The fluid model describes the plasma in terms of macroscopic variables like Pressure, Temperature, average velocity, density, flux; like ordinary fluid dynamics. The governing Partial Differential Equations are obtained by taking moments of the Boltzmann equation, or a special case of the Boltzmann equation called the Vlasov equation. Such a procedure gives rise to:

The continuity equation:

$$\frac{\partial \varrho}{\partial t} + \nabla \cdot (\varrho \mathbf{v}) = 0$$

and the Cauchy momentum equation:

$$\varrho \left(\frac{\partial}{\partial t} + \mathbf{v} \cdot \nabla \right) \mathbf{v} = \mathbf{J} \times \mathbf{B} - \nabla p$$

Higher moments yield other equations for quantities like the entropy. The fluid equations average over the velocity distribution of the particles to obtain the macroscopic variables like Pressure and Temperature, as discussed earlier- by taking moments of the Kinetic equations like the Boltzmann equation or the Vlasov equation.

4. Magnetohydrodynamics

Magnetohydrodynamics(MHD) is an extension of the fluid model of describing a plasma. In a first approximation, the magnetic and electric fields acting on the fluid and the currents generated are now solved using Faraday's law:

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

and the Ampere's law:

$$\mu_0 \mathbf{J} = \nabla \times \mathbf{B}$$

The full set of Maxwell's equations can also be coupled with the fluid. MHD description of a plasma also describes dynamic waves such as Alfvén waves and magnetosonic waves. MHD theory can also be used to describe interaction of the plasma with electromagnetic waves, for example those from a LASER source relevant to LASER plasma processes in surface engineering. Ideal MHD studies plasma as a fluid of single species, however, multi-species plasma can also be studied.

5. The model used in the project

In the context of plasma processes like Magnetron Sputtering where particles have a considerably large mean free path, we have decided not to use the fluid model and the MHD descriptions of a plasma. In such processes, it is almost always the case that the strength of the electric and magnetic fields applied by the apparatus is far more stronger than the electric and magnetic fields generated by charged particles in a plasma. This approximation allows us to avoid solving Maxwell's equations and use only the Lorentz force. The model used in the project is mostly similar to the single particle model, where in a collection of particles, each particle evolves under the influence of the electric and magnetic fields set up by the apparatus; governed by the Lorentz force. However, we incorporate a little bit of the Kinetic theory in that we are interested in different initial velocity distributions for particles in the plasma and how the velocity distribution changes over time; as it is important to understand the velocity distribution to characterize the reflection and loss of particles in a magnetic-mirror like trap that may be setup in the plasma chamber.

3 Gaps in Literature

It would take a number of courses on plasma physics to fully understand the current research methods in plasma physics. In the interest of time, we have studied some simple setups; so that we can setup well functioning plasma configuration during the course of the project and study some aspects that we are interested in. The forefront of research in plasma physics concerns complicated devices like Magnetic Confinement Fusion, or Quantum Optic systems. Most research in surface engineering focuses on the properties of coatings obtained and parameters of plasma used; in processes that use plasma. In our project, we would like to set up a simple plasma simulation that can help us study smaller devices like the one available in the School of Mechanical Engineering; where we can control a small flux of particles by tuning the electric and magnetic fields. This section describes, how we construct a simple easy to use, plasma simulation system; which is yet to be functional.

3.1 Particle in Cell Methods

Particle in a cell methods are used to simulate the kinetic theory of plasma. Most

3.2 Boris Algorithm

4 Problem Definition

4.1 Particle Sampling

Maxwell Boltzmann distribution
Parabolic density functions

4.2 Particle Evolution

Lorentz force and Boris Algorithm.

4.3 Fields

5 Objectives

The objectives of the project are:

1. **Single Particle Method**

To simulate charged particles that evolve under the influence of electric and magnetic fields; as governed by the Lorentz force.

2. **Field Configurations**

To simulate a few different configurations of electric and magnetic fields- some describing apparatus like coils; some describing analytic expressions for fields and to study the different evolution of particles.

3. **Kinetic Theory**

To study different initial velocity distributions and how the velocity distribution of particles changes as the particles evolve. Parameters like the Plasma temperature are to be studied under this topic.

4. **Analysis**

To analyze different batches or collections of particles, subjected to different field configurations.

6 Methodology

6.1 Single particle and evolution

6.2 Defining the fields

6.3 Particle initialization

6.4 Running different batches

7 Work carried out so far

7.1 Algorithm Outline

8 Work to be done

9 Gant Chart(Work Plan)

10 Milestones in the project phase

References

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