

dosampling

April 9, 2022

```
[1]: import import_ipynb
      from sampling import Sampler
      from constants import Constants
      import numpy as np
```

importing Jupyter notebook from sampling.ipynb
importing Jupyter notebook from constants.ipynb

0.1 Don't run cells in this notebook without doing it deliberately. Many files will be created unnecessarily

```
[2]: sample = Sampler()
      constants = Constants()
```

0.2 Sample 1 Hydrogen ions

$N_A = \text{constants.constants}['N_A']$ # Avogadro's number

$V_{STP} = 22.4$ # Volume; in Liters, of 1 mole gas at Standard Temperature and Pressure conditions (STP)

$V_{LPM_reference} = 10$ # Volume flow rate; in Liters per minute taken as reference

$V_{LPS_reference} = V_{LPM_reference} / 60$ # Volume flow rate; in Liters per second taken as reference

$T_{sample_batch} = 10$ # Time; in seconds, taken to get volume from volume flow rate

$V_{sample_batch} = V_{LPS_reference} * T_{batch}$ # Volume; in liters, of a sampling batch taken

$V_{ratio} = V_{sample_batch} / V_{STP}$

$n = N_A * V_{ratio}$ # number of molecules in the gas

$n_{atoms} = 2$ # Number of atoms in a molecule, 2 for hydrogen

$n = n * n_{atoms}$ # The number of particles involved in the sampling

This procedure gives number of particles in the order of 10^{23} which is just too large for simulation. So instead we only use 100 particles for now.

```
[3]: # Constants separated
K = constants.constants['K'][0] # Boltzmann constant
amu = constants.constants['amu'][0] # Atomic mass unit in kg

m_amu = constants.constants['m_H'][0] # The relative atomic mass of hydrogen
↳atom in amu
m_kg = m_amu * amu # The mass of Hydrogen atom in kg
```

```
[4]: #Define needed parameters
n = 100 # Consider 100 particles for now

#Position parameters
r = [-0.5, 0, 0]
# The chamber is considered as a cube of side 1 m, with [-0.5, -0.5, -0.5]
↳being the bottom left corner
# and [0.5, 0.5, 0.5] being the top right corner
# Particles start at the center of the left face.

r_strategy = 'sample_same_given_position'
r_details = 'r=[-0.5,0,0] for 1m x 1m x 1m cube chamber. H atom'
#Velocity parameters
v_median = 800 # Median particle speed considered 800 m/s

T = 10000 #Plasma temperature = 10000 K

v_strategy = 'sample_Maxwellian_velocity_all_random_direction'
v_details = 'v_median=800ms-1 T=10000K. H atom'
```

```
[5]: #Sample positions and velocities and write to file.

positions = sample.sample_same_given_position(r, n)

'''
sample.write_to_csv_file(positions, 'r', r_strategy, n, r_details)
'''

velocities = sample.sample_Maxwellian_velocity_all_random_direction(v_median,
↳K, T, m_kg, n)

'''
sample.write_to_csv_file(velocities, 'v', v_strategy, n, v_details)
'''
```

```
[5]: "\nsample.write_to_csv_file(velocities, 'v', v_strategy, n, v_details)\n"
```

1 Sample 1 attempt 2

$v_{\text{median}} = 800$ gives large velocity components like 2000, 3000 Perhaps $v_{\text{median}} = 0$ should be good

So only velocities file will be regenerated

```
[6]: v_median_2 = 0

v_details_2 = 'v_median=0ms-1 T=10000K. H atom'

velocities_2 = sample.
↳sample_Maxwellian_velocity_all_random_direction(v_median_2, K, T, m_kg, n)

'''
sample.write_to_csv_file(velocities_2, 'v', v_strategy, n, v_details_2)
'''
```

```
[6]: "\nsample.write_to_csv_file(velocities_2, 'v', v_strategy, n, v_details_2)\n"
```

1.0.1 Sample 1 attempt 3

we were using Hydrogen atom, but let's use Hydrogen gas instead and try.

Only velocities will be regenerated

```
[7]: v_details_3 = 'v_median=0ms-1 T=10000K. H2 gas'

velocities_3 = sample.
↳sample_Maxwellian_velocity_all_random_direction(v_median_2, K, T, m_kg * 2,
↳n)

'''
sample.write_to_csv_file(velocities_3, 'v', v_strategy, n, v_details_3)
'''
```

```
[7]: "\nsample.write_to_csv_file(velocities_3, 'v', v_strategy, n, v_details_3)\n"
```

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[ ]:
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2 Sample 2

2.1 2 a position

All particles are 0.5 m away from the center [0,0,0] but in a uniform random direction

```
[8]: positions_p2 = sample.sample_same_given_distance_all_random_direction(d=0.5,
↳n=100)

r_strategy_p2 = 'sample_same_given_distance_all_random_direction'
```

```
r_details_p2 = 'd=0,5m from center [0,0,0] for 1m x 1m x 1m cube chamber'
#sample.write_to_csv_file(positions_p2, 'r', r_strategy_p2, 100, r_details_p2)
```

2.2 2 b velocity

Particle speeds are sampled from parabolic distribution velocity directions are uniformly randomly sampled

```
[9]: R = constants.constants['R'][0]
T_p2 = 10000 # plasma temperature 10000 K
mH_gmol = constants.constants['m_H'][0]
mH_kgmol = mH_gmol * (10**(-3))
sqrt_pi = np.sqrt(np.pi)
# Mean to be used equal to mean speed of Maxwellian distribution
maxwell_mean = (2/sqrt_pi) * np.sqrt( (2 * R * T_p2)/ mH_kgmol)
# Standard deviation to be used such that
# Variance = RMS of Maxwellian - (Mean of Maxwellian)**2
maxwell_std_coeff = np.sqrt(3 - (8/(np.pi**2)))
maxwell_std_speed = maxwell_std_coeff * np.sqrt( (R * T_p2)/ mH_kgmol)
# Found empirically
maxwell_speed_scale = 30049.5113130523
```

```
[10]: ### MAIN part where sampling was done ###
velocities_p2 = sample.sample_parabolic_speed_f1_all_random_direction(n=100,
    ↳loc=maxwell_mean, scale=maxwell_speed_scale)
v_strategy_p2 = 'sample_parabolic_speed_f1_all_random_direction'
v_details_p2 = 'n=100, parameters based on 10000K Maxwellian'
#sample.write_to_csv_file(velocities_p2, 'v', v_strategy_p2, 100, v_details_p2)
```

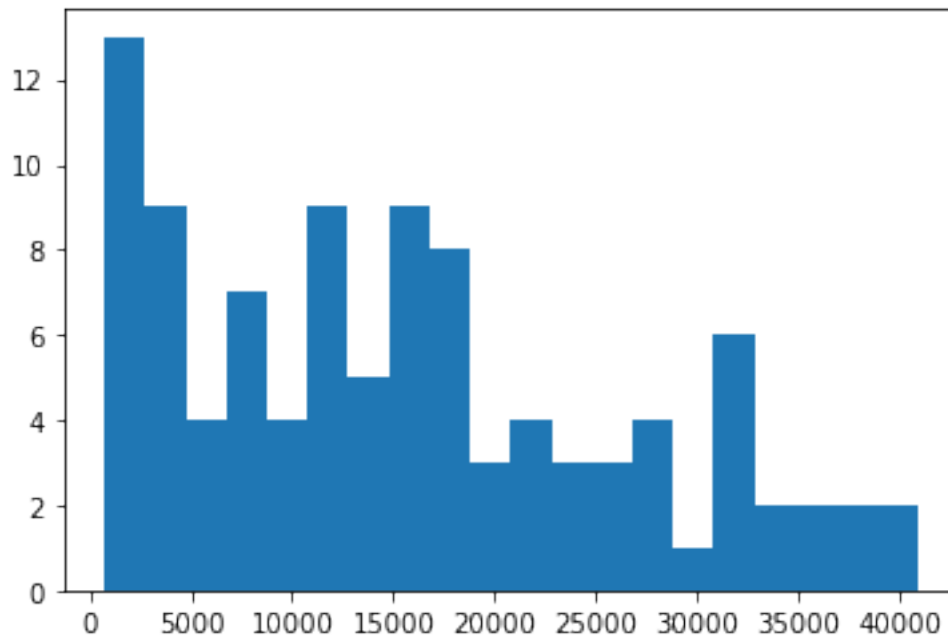
```
[64]: # To plot and see the speed distribution before saving to csv file
import matplotlib.pyplot as plt
speeds = []
def norm(x, y, z):
    return np.sqrt((x*x)+(y*y)+(z*z))
for i in range(len(velocities_p2)):
    speeds.append(norm(velocities_p2[i][0], velocities_p2[i][1],
    ↳velocities_p2[i][2]))
speeds = np.array(speeds)
plt.hist(speeds, 20)
#plt.savefig('parabolic_speeds_sampling', dpi='figure', format='png')
```

```
[64]: (array([13., 9., 4., 7., 4., 9., 5., 9., 8., 3., 4., 3., 3.,
    4., 1., 6., 2., 2., 2., 2.]),
array([ 733.48899315, 2739.42868759, 4745.36838202, 6751.30807646,
    8757.24777089, 10763.18746533, 12769.12715977, 14775.0668542 ,
    16781.00654864, 18786.94624308, 20792.88593751, 22798.82563195,
    24804.76532639, 26810.70502082, 28816.64471526, 30822.58440969,
```

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32828.52410413, 34834.46379857, 36840.403493 , 38846.34318744,
40852.28288188]),
<BarContainer object of 20 artists>)

```



```

[61]: # Writing to the csv file
      # sample.write_to_csv_file(velocities_p2, 'v', v_strategy_p2, 100, v_details_p2)

```

SUCCESS

```

/home/kushik/Kushik/VIT/Eighth semester/MagneticMirror/csvfiles/sampling/100 v
sample_parabolic_speed_f1_all_random_direction n=100, parameters based on 10000K
Maxwellian 06-04-2022 17:44:46:811591

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[41]: # This was done to determine the scale parameter to be passed to sample the
      ↳parabolic velocities
      # This is correct to 10**(-10) which is the highest precision output during the
      ↳process.
      import scipy.stats as stats
      def find_scale(maxwell_mean, maxwell_std_speed):
          required = maxwell_std_speed
          current_scale = 30049.5113130523
          current_std = stats.rdist.std(c=4, loc=maxwell_mean, scale=current_scale)
          i = 0
          while True:
              i+= 1

```

```

diff = required - current_std

if np.abs(diff) < 10**(-11):
    break

'''if np.close(current, required):
    break
'''

if diff > 0:
    current_scale = current_scale + 10**(-11)
    current_std = stats.rdist.std(c=4, loc=maxwell_mean,
↪scale=current_scale)
if diff < 0:
    current_scale = current_scale - 10**(-11)
    current_std = stats.rdist.std(c=4, loc=maxwell_mean,
↪scale=current_scale)

if i%100 == 0:
    print(f'Current_std:{current_std} Current_scale:{current_scale} i:
↪{i}\n')
    return current_scale
#maxwell_speed_scale = find_scale(maxwell_mean=maxwell_mean,
↪maxwell_std_speed=maxwell_std_speed)

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[47]: # We check the value of the standard deviation of this distribution
stats.rdist.std(c=4, loc=maxwell_mean, scale=maxwell_speed_scale)

```

```

[47]: 13438.54999732678

```

```

[48]: # Indeed is equal to the Maxwellian standard deviation
maxwell_std_speed

```

```

[48]: 13438.549997326772

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