

Assignment-3

Let us consider sample dataset have one input (x_i) & one output (y_i) and no. of samples. Develop a sample regression model using stochastic gradient descent optimiser.

Sample (i)	x_i	y_i	manual calc.
1	0.2	3.4	2 iterations
2	0.4	3.8	2 samples.
3	0.6	4.2	
4	0.8	4.6	

Steps

1. $x, y, m=1, c=-1, \eta=0.1, epochs=2, ns=2$
2. $iter=1$
3. $sample=1$
4.
$$\frac{\partial E}{\partial m} = -(3.4 - 1(0.2) - (-1)) \cdot 0.2 = -0.84$$

$$\frac{\partial E}{\partial c} = -(3.4 - 1(0.2) - (-1)) = -4.2$$
5.
$$\Delta m = -\eta \frac{\partial E}{\partial m} = -0.1(-0.84) = 0.084$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = -0.1(-4.2) = 0.42$$
6.
$$m = m + \Delta m = 1 + 0.084 = 1.084$$

$$c = c + \Delta c = -1 + 0.42 = -0.58$$
7.
$$sample = sample + 1 = 1 + 1 = 2$$
8.
$$if (sample > ns) \quad 2 > 2 \quad (\text{false})$$

 next step
 else
 step-4

$$4. \quad \frac{\partial E}{\partial m} = -(3.8 - 1.084(0.4) + 0.58) 0.4$$

$$= -1.5785$$

$$\frac{\partial E}{\partial c} = -(3.8 - 1.084(0.4) + 0.58)$$

$$= -3.9464$$

$$5. \quad \Delta m = -(0.1)(-1.5785) = 0.1578$$

$$\Delta c = -(0.1)(-3.9464) = 0.3946$$

$$6. \quad m = m + \Delta m = 1.084 + 0.1578 = 1.2418$$

$$c = c + \Delta c = -0.58 + 0.3946 = -0.1854$$

$$7. \quad \text{sample} = \text{sample} + 1 = 2 + 1 = 3$$

$$8. \quad \text{if (sample} > n_s) \quad 3 > 2 \text{ (true)}$$

next step
else
step-4
next step

$$9. \quad \text{iter} = \text{iter} + 1 = 1 + 1 = 2$$

$$10. \quad \text{if (iter} > \text{epochs}) \quad 2 > 2$$

next step
else
step-3
false
step-3

$$S-3. \quad \text{sample} = 1$$

$$4. \quad \frac{\partial E}{\partial m} = -(3.4 - 1.2(0.2) + 0.18) 0.2$$

$$= -0.668$$

$$\frac{\partial E}{\partial c} = -(3.4 - 1.2(0.2) + 0.18)$$

$$= -3.34$$

$$5. \Delta m = -(0.1) (-0.668) = 0.0668$$

$$\Delta c = -(0.1) (-3.34) = 0.33$$

$$6. m = m + \Delta m = 1.24 + 0.0668 = 1.3068$$

$$c = c + \Delta c = 0.18 + 0.33 = 0.51$$

$$7. \text{sample} = \text{sample} + 1 = 1 + 1 = 2$$

$$8. \text{if (sample} > n_s) \quad 2 > 2 \text{ false}$$

next step

step 4

else

step 4

$$\frac{\partial E}{\partial m} = -(3.8 - (1.5)(0.4) - 0.15) 0.4 = -1.25$$

$$\frac{\partial E}{\partial c} = -(3.8 - (1.3)(0.4) - 0.15) = -3.13$$

$$\Delta m = -(0.1) (-1.25) = 0.125$$

$$\Delta c = -(0.1) (-3.13) = 0.313$$

$$6. m = m + \Delta m = 1.3 + 0.125 = 1.425$$

$$c = c + \Delta c = 0.51 + 0.313 = 0.823$$

$$7. \text{sample} = \text{sample} + 1 = 2 + 1 = 3$$

$$8. \text{if (sample} > n_s) \quad 3 > 2$$

true

next step

true

else

next step

step 4

9. $iter = iter + 1 = 2 + 1 = 3$

10. $if (iter > epochs)$ $3 > 2$ → true
 next step
 else $2.1 = 0.000.0 + 1.0 \cdot 1 = 1.0$ → true
 $\epsilon = 3$ next step

11. $m = 1.42$ $c = 0.46$