

## ASSIGNMENT - 2

$$f(x) = x^2 + y^2 + 10$$

Step 1: let  $x = -1$ ,  $y = 1$ ,  $\eta = 0.1$ , epoch = 2

Step 2: itr = 1

Step 3:  $\frac{\partial f}{\partial x} = 2x = -2$

$$\frac{\partial f}{\partial y} = 2y = 2$$

Step 4:  $\Delta x = -\eta \frac{\partial f}{\partial x} = -0.1(-2) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -0.1(2) = -0.2$$

Step 5:  $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

Step 6: itr = itr + 1  $\Rightarrow 1 + 1 = 2$

Step 7: if (itr > epoch)

if (2 > 2)

false so go to step (3)

Step 3:  $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

Step 4:  $\Delta x = -\eta \frac{\partial f}{\partial x} = -0.1(-1.6) = 0.16$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -0.1(1.6) = -0.16$$

Step 5:  $x = x + \Delta x = -0.8 + 0.16 = -0.64$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

Step 6: itr = itr + 1  $\Rightarrow 2 + 1 = 3$

Step 7: if (3 > 2) true so

$$x = -0.64, y = 0.64$$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$\therefore f(x, y) = 10.8192$$

Sample	$x_i^a$	$y_i^a$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Step 1:  $m=1$ ,  $c=-1$ ,  $\eta=0.1$ ,  $x_{\text{pool}}=2$

Step 2:  $itr=1$

Step 3: Sample = 1

$$\begin{aligned} \text{Step 4: } \frac{\partial F}{\partial m} &= -(y_i - mx_i - c) \times x_i \\ &= -(3.4 - (1)(0.2) - (-1))(0.2) \\ &= -0.84 \end{aligned}$$

$$\begin{aligned} \frac{\partial F}{\partial c} &= -(y_i - mx_i - c) \\ &= -(3.4 - (1)(0.2) - (-1)) \\ &= -4.2 \end{aligned}$$

$$\begin{aligned} \text{Step 5: } \Delta m &= -\eta \frac{\partial F}{\partial m} = -0.1(-0.84) = 0.084 \\ \Delta c &= -\eta \frac{\partial F}{\partial c} = -0.1(-4.2) = 0.42 \end{aligned}$$

$$\begin{aligned} \text{Step 6: } m &= m + \Delta m = 1 + 0.084 = 1.084 \\ c &= c + \Delta c = -1 + 0.42 = -0.58 \end{aligned}$$

Step 7: if (2 > 2)  
false

$$\begin{aligned} \text{Step 8: } \frac{\partial F}{\partial m} &= -(3.8 - (1.084)(0.4) - (-0.58))(0.4) \\ &= -1.528 \\ \frac{\partial F}{\partial c} &= -(3.8 - (1.084)(0.4) - (-0.58)) \\ &= -2.5064 \end{aligned}$$

Step (E):

$$\Delta m = -n \frac{dG}{dm} = 0.1578$$

$$\Delta C = -n \frac{dE}{dC} = 0.39464$$

Step (G):

$$m = m + \Delta m = 1.084 + 0.1578 = 1.2418$$

$$C = C + \Delta C = -0.58 + 0.39464 = -0.18536$$

## Assignment 5

sample $i$	$x_i^a$	$y_i^a$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

} batch=1  
} batch=2

1)  $\{x, y\}; m=1, c=-1, \eta=0.1, \text{epochs}=2, bs=2$

2)  $nb = \frac{ns}{bs} = \frac{4}{2} = 2$

3)  $itr = 1$

4)  $Batch = 1$

5)  $\frac{\partial E}{\partial m} = \frac{-1}{bs} \sum_{i=1}^{bs} (y_i - mx_i - c) x_i$

$$= \frac{-1}{2} \left[ (3.4 - (1)(0.2) + 1)0.2 \right] + \left[ (3.8 - 0.4 + 1)0.4 \right]$$
$$= -1.34$$

$$\frac{\partial E}{\partial c} = \frac{-1}{2} \left[ (3.4 - 0.241) + (3.8 - 0.4 + 1) \right]$$
$$= -4.3$$

6)  $\Delta m = -(0.1)(-1.34) = 0.134$   
 $\Delta c = -(0.1)(-4.3) = 0.43$

7)  $m = m + \Delta m = 1 + 0.134 = 1.134$

$$c = c + \Delta c = -1 + 0.43 = -0.57$$

8)  $Batch + 1$

9) if (batch > nb)

$$3 > 2$$

goto next step

10)  $itr = itr + 1$

11) if ( $itr > 2$ ) goto step 12 else step 4

4) Batch = 1

$$\frac{\partial E}{\partial m} = -\frac{1}{2} \left[ 3.4 - (1.4)(0.2) + (0.5)(0.2) + 3.8 - (1.4)(0.4) + 0.15(0.4) \right]$$

$$= -1.0029$$

$$5) \frac{\partial E}{\partial c} = -\frac{1}{2} \left[ 3.4 - (1.42)(0.2) + 0.1523 \right] + 3.8 - (1.4)(0.4) + 0.15$$

$$= -3.3241$$

$$6) \Delta m = -0.1(-1.0029) = 0.1002$$

$$\Delta c = -0.1(-3.3241) = 0.3324$$

$$7) m+ = \Delta m = 1.42 + 0.1002 = 1.5$$

$$c+ = \Delta c = -0.15 + 0.3 = 0.15$$

8) Batch + = 1

9) if (272) go to step 10 else step 7

$$10) \frac{\partial E}{\partial m} = -\frac{1}{2} \left[ 4.2 - (1.5)(0.6) - 0.17(0.6) + 4.6 - (1.5)(0.8) - 0.17(0.8) \right]$$

$$= -2.21$$

$$\frac{\partial E}{\partial c} = -3.15$$

$$6) \Delta m = -0.1 \times -2.21 = 0.221$$

$$\Delta c = -0.1 \times -3.15 = 0.315$$

$$7) m+ = \Delta m = 1.5 + 0.22 = 1.7$$

$$c+ = \Delta c = 0.15 + 0.3 = 0.4$$

8) Batch + = 1

9) if (Batch > nb) go to step 10 else step 7

10)  $itr = itr + 1$

11) if  $(3 > 2)$  go to step 12

12) print m, c

$m = 1.748$

$c = 0.494$

# Assignment - 7

Sample	$x_i$	$y_i$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

1)  $(x, y)$ ;  $n=1$ ,  $c=-1$ ,  $\eta=0.1$ ,  $epoch=2$ ,  $ns=1$

2)  $itr=1$

3)  $\frac{\partial E}{\partial m} = \frac{-1}{2} [3.4 - (-1)(0.2) + 1] 0.2 + (3.8 - (-1)(0.4) + 1) 0.4$   
 $= -1.34$

$$\frac{\partial E}{\partial c} = \frac{-1}{2} [3.4 - 0.2 + 1] + (3.8 - 0.4 + 1)$$
$$= -4.3$$

4)  $\Delta m = -\eta \frac{\partial E}{\partial m}$

$$= -0.1 \times -1.34 = 0.134$$

$$\Delta c = -\eta \frac{\partial E}{\partial c}$$
$$= -0.1(-4.3) = 0.43$$

5)  $m = m + \Delta m = 1 + 0.134 = 1.13$

$$c = c + \Delta c = -0.1 + 0.43 = 0.43$$

6)  $itr = itr + 1$

7)  $itr(2) > 2$   
go to step 3



$$3) \frac{\partial E}{\partial m} = \frac{1}{2} [ 3.4 - (1.134)(0.2) + 0.54(0.2) + 3.8 - (1.134)(0.4) - 10.57(0.4) ]$$

$$= -1.57$$

$$\frac{\partial E}{\partial c} = -3.829$$

$$4) \Delta m = -0.1 \times 1.57 = 0.157$$

$$\Delta c = -0.1 \times -3.8 = 0.3829$$

$$5) m = m + \Delta m = 1.2497$$

$$c = c + \Delta c = -0.187$$

$$6) \text{itr} = \text{itr} + 1$$

$$7) \text{if } (\text{itr} > \text{epoch})$$

$$3 > 2$$

$$8) m = 1.24, c = -0.187$$



## Assignment 7-9

$x$	$y$
0.2	3.4
0.4	3.8

1)  $(x, y)$ ,  $m=1$ ,  $c=-1$ ,  $\eta=0.1$ , epoch=2,  $\beta=0.9$ ,  $v_m=v_c=0$

2)  $itr=1$

3) sample=1

4)  $\frac{\partial E}{\partial m} = -0.84 = g_m$

$\frac{\partial E}{\partial c} = -4.2 = g_c$

5)  $v_m = \beta v_m - \eta g_m$

$$= (0.9)(0) - (0.1)(-0.84)$$

$$v_m = 0.084$$

$$v_c = \beta v_c - \eta g_c$$

$$= (0.9)(0) - (0.1)(-4.2)$$

$$v_c = 0.42$$

6) ~~steps~~  $m+1 = N_m = 1 + 0.084 = 1.084$

$$c+1 = N_c = -1 + 0.42 = -0.58$$

7) sample =  $1+1=2$

8) if (sample > n)  
2 > 2

9)  $g_m = \frac{\partial E}{\partial c} = -1.57856$

$$g_c = \frac{\partial E}{\partial c} = -3.9464$$

$$5) v_m = \delta v_m - \eta g_m$$

$$= 0.223456$$

$$v_c = \delta v_c - \eta g_c$$

$$= 0.97264$$

$$6) m = 1.3174$$

$$c = 0.19264$$

$$7) \text{sample} = 2 + 1 = 3$$

$$8) \text{if}(2 > 2)$$

$$9) \text{itr} = \text{itr} + 1 = 1 + 1 = 1$$

$$10) \text{if}(2 > 2)$$

$$3) \text{sample} = 1$$

$$4) g_m = \frac{\partial E}{\partial m} = -0.5887$$

$$g_c = \frac{\partial E}{\partial c} = -2.9438$$

$$5) v_m = \delta v_m - \eta g_m = 0.26892$$

$$v_c = \delta v_c - \eta g_c = 0.9892$$

$$6) m = m + v_m = 1.5863$$

$$c = c + v_c = 1.18234$$

$$7) \text{sample} = 1 + 1 = 2$$

$$8) \text{if}(\text{sample} > n)$$

$$2 > 2$$

$$4) g_m = -1.7391$$

$$g_c = -4.3499$$

$$5) v_m = \delta v_m - \eta g_m$$

$$= 0.41604$$

$$v_c = \delta v_c - \eta g_c$$

$$= 1.3255$$

$$6) m = m + v_m = 2.0023$$

$$c = c + v_c = 2.507$$

$$7) \text{sample} = 2+1 = 3$$

$$8) \text{if}(3 > 2)$$

$$9) \text{if } r = 2+1 = 3$$

$$10) \text{if}(3 > 2)$$

$$11) m = 2.00, c = 2.507$$