

Assignment - 2

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Step 1: $f(x, y) = x^2 + y^2 + 10$

$$\frac{\partial f}{\partial x} = 2x \quad ; \quad \frac{\partial f}{\partial y} = 2y$$

Step 2: Initialising parameter

$$x = 1, y = -1, \eta = 0.1, \text{iteration} = 1, \text{epochs} = 2$$

Step 3: $\left(\frac{\partial f}{\partial x}\right)_{x=1} \Rightarrow 2(1) \Rightarrow 2, \left(\frac{\partial f}{\partial y}\right)_{y=-1} = 2(-1) \Rightarrow -2$

Step 4: $\Delta x = -\eta \frac{\partial f}{\partial x} \Rightarrow (-0.1) \times 2 \Rightarrow -0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} \Rightarrow -(0.1)(-2) \Rightarrow 0.2$$

Step 5: $x = x + \Delta x \quad \left| \quad y = y + \Delta y \right.$
 $= 1 + (-0.2) \quad \left| \quad = -1 + 0.2 \right.$
 $\Rightarrow \underline{0.8} \quad \left| \quad = \underline{-0.8} \right.$

Step 6: iteration - iteration + 1 $\Rightarrow 1 + 1 = 2 \leq \text{epochs}$ go to step 7

Step 7: $\left(\frac{\partial f}{\partial x}\right)_{x=0.8} \Rightarrow 2(0.8) \Rightarrow \underline{1.6}$

$$\left(\frac{\partial f}{\partial y}\right)_{y=-0.8} \Rightarrow 2(-0.8) \Rightarrow \underline{-1.6}$$

$$\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(1.6) \Rightarrow \underline{-0.16}$$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(-1.6) \Rightarrow \underline{0.16}$$

$$\text{Step 9: } x = x + Dx$$

$$= (0.8) - (0.16) \\ = \underline{\underline{0.64}}$$

$$y = y + Dy$$

$$= -0.8 + 0.16$$

$$= \underline{\underline{-0.64}}$$

$$\text{Step 10: } \text{iteration} = \text{iteration} + 1 \Rightarrow 2 + 1 = 3 > \text{epochs}$$

go to step 11

$$\text{Step 11: } f(x, y) \Rightarrow (0.16)^2 + (-0.16)^2 + 10$$

$$\Rightarrow \underline{\underline{10.0512}}$$