

Assignment-2

Find global minimum point & value
for function $F(x, y) = x^2 + y^2 + 10$.

18K41A0420

→ DO manual calculations for 2 iterations.

step 1: $x = -1$ $y = +1$ $\eta = 0.1$ epochs = 2

step 2: iter = 1

step 3: $\frac{\partial f}{\partial x} = 2x = -2$

$$\frac{\partial f}{\partial y} = 2y = 2$$

step 4: $\Delta x = -\eta \frac{\partial f}{\partial x} = -2(-0.1) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(2) = -0.2$$

step 5: $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

step 6: iter = iter + 1 = 1 + 1 = 2

step 7: if (iter > epochs)

goto step 5

else

goto step 3

step 3: $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

step 4: $\Delta x = -\eta \frac{\partial f}{\partial x}$

$$= -(0.1)(-1.6) = 0.16$$

$$\Delta y = -\eta \frac{\partial f}{\partial y}$$

$$= -(0.1)(1.6) = -0.16$$

step 5: $x = x + \Delta x$
 $= -0.8 + 0.16 \Rightarrow -0.64$
 $y = y + \Delta y$
 $= 0.8 - 0.16 \Rightarrow 0.64$

step 6: $itr = itr + 1 = 2 + 1 \Rightarrow 3$

step 7: $\text{if } (itr > \text{epochs})$

$3 > 2$

goto step 8

else: goto step 3

step 8: $x = -0.64$
 $y = 0.64$

$$\begin{aligned} F(x, y) &= x^2 + y^2 + 10 \\ &= (-0.64)^2 + (0.64)^2 + 10 \\ &= 0.4 + 0.4 + 10 \\ &= 10.8, \end{aligned}$$