

18K41A0420

Assignment - 13

Let us consider a sample dataset share one input ( $x_i^a$ ) & one output ( $y_i^a$ ) & no of samples 4. Develop a simple linear regression model using ADAGRAD optimiser.

sample(i)	$x_i^a$	$y_i^a$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Do manual calculations for 2 iterations with first 2 samples.

Step-1:  $[x, y]$ , epochs = 2,  $m = 1$ ,  $c = -1$ ,  $G_m = G_c = 0$ ,  $\eta = 0.1$ ,  $\delta = 10^{-8}$

Step-2: iter = 1

Step-3: sample = 1

$$g_m = -(3.4 - (-1)(0.2) + 1) 0.2 = -0.84$$

$$g_c = -(3.4 - (-1)(0.2) + 1) = -4.2$$

$$G_m = 0 + (-0.84)^2 = 0.7056$$

$$G_c = 0 + (-4.2)^2 = 17.64$$

$$\underline{\text{step 6:}} \quad \Delta m = \frac{-\eta}{\sqrt{G_m + \epsilon}} g_m = \frac{-0.1}{\sqrt{0.7056 + 10^{-8}}} \times 0.8 \\ = 0.09$$

$$\Delta c = \frac{-0.1}{\sqrt{17.64 + 10^{-8}}} \times -4.2 \\ = 0.09$$

$$\underline{\text{step 7:}} \quad m = m + \Delta m = 1 + 0.09 = 1.09 \\ c = c + \Delta c = -1 + 0.09 = -0.91$$

$$\underline{\text{step 8:}} \quad \text{sample} = \text{sample} + 1 \\ = 1 + 1 \\ = 2$$

step 9: if (sample > ns) goto step 10  
 $2 > 2$

else : step 4

$$\underline{\text{step 4:}} \quad g_m = -(3.5 - (1.09)(0.4) + 0.91)0.4 = -1.7 \\ g_c = -(3.84 - (1.09)(0.4) + 0.91) = -4.27$$

$$\underline{\text{step 5:}} \quad G_m = 0.7056 + (-1.7)^2 = 3.58 \\ G_c = 17.64 + (-4.27)^2 = 35.37$$

$$\underline{\text{step 6:}} \quad \Delta m = \frac{-0.1}{\sqrt{3.58 + 10^{-8}}} = 0.08$$

$$\Delta c = \frac{-0.1}{\sqrt{35.37 + 10^{-8}}} \times -4.27 = 0.08$$

$$\underline{\text{Step 7:}} \quad m = m + \Delta m = 1.09 + 0.08 = 1.17$$

$$c = c + \Delta c = -0.91 + 0.07 = -0.84$$

Step 8: sample + 1  $\Rightarrow 2+1 \Rightarrow 3$

Step 9: if (sample > ns) goto ⑩  
else goto ④

Step 10: iter + 1  $\Rightarrow 1+1 \Rightarrow 2$

Step 11: if (iter > epochs) goto 12  
 $2 > 2$

use goto step 3

Step 3: sample = 1

$$g_m = (-3.4 - (1.17)(0.2) + 0.84) \cdot 0.2 = -0.80$$

$$\underline{\text{Step 4:}} \quad g_m = (-3.4 - (1.17)(0.2) + 0.84) = -4.0$$

$$g_c = -((3.4 - (1.17)(0.2) + 0.84)^2 = 4.23$$

$$\underline{\text{Step 5:}} \quad G_m = 3.59 + (-0.80)^2 = 4.23$$

$$G_c = 35.89 + (-4.0)^2 = 51.89$$

$$\underline{\text{Step 6:}} \quad \Delta m = \frac{-0.1}{\sqrt{4.23 + 10.8}} \times -0.80 = 0.038$$

$$\Delta c = \frac{-0.1}{\sqrt{51.89 + 10.8}} \times -4.0 = 0.05$$

$$\underline{\text{Step 7:}} \quad m = m + \Delta m = 0.038 + 1.17 = 1.208$$

$$c = c + \Delta c = -0.84 + 0.05 = -0.79$$

Step 8: if (sample > ns) goto step 10  
else goto step 4.

$$\underline{\text{Step 4:}} \quad g_m = -(3.8 - (-1.20)(0.4) + 0.79) \times 0.4 \\ = -1.64$$

$$g_c = -(3.8 - (-1.20)(0.4) + 0.79) = -4.11$$

$$\underline{\text{Step 5:}} \quad G_m = 4.23 + (-1.64)^2 = 6.9$$

$$G_c = 51.89 + (-4.11)^2 = 68.7$$

$$\underline{\text{Step 6:}} \quad \Delta m = \frac{-0.1}{\sqrt{6.8+15^2}} \times -1.64 = 0.06$$

$$\Delta c = \frac{-0.1}{\sqrt{68.7+15^2}} \times -4.11 = 0.04.$$

$$\underline{\text{Step 7:}} \quad m = m + \Delta m = 1.208 + 0.06 = 1.26$$

$$c = c + \Delta m = -0.79 + 0.04 = -0.75$$

Step 8: sample + = 1  $\Rightarrow$  3

Step 9: if (sample > nS) goto step 10

3 > 2

else goto ④.

Step 10: iter + = 1  $\Rightarrow$  2 + 1 = 3

Step 11: if (iter > epochs) goto ⑫  
else goto ③

Step 12:  $m = 1.76$   
 $c = -0.75$