

Let us consider a sample dataset have one i/p ( $x_i$ ) & 1 o/p ( $y_i$ ) & no. of samples 4. Develop a simple linear regression model using ADAGRAD optimizer.

Sample ( $i$ )	$x_i$	$y_i$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Do manual calculations for 2 iteration with 1<sup>st</sup> 2 samples.

step 1 :  $[x, y]$ , epochs = 2,  $m = 1$ ,  $c = -1$ ,  $G_m = 0$ ,  $G_c = 0$ ,  $\eta = 0.1$ ,  $\epsilon = 10^{-8}$

2. iter = 1

3. sample = 1

$$4. g_m = -(3.4 - (-1)(0.2) + 1) \cdot 0.2 = -0.84$$

$$g_c = -(3.4 - (-1)(0.2) + 1) = -4.2$$

$$5. G_m = 0 + (-0.84)^2 = 0.7056$$

$$G_c = 0 + (-4.2)^2 = 17.64$$

$$6. \Delta m = \frac{-\eta}{\sqrt{G_m + \epsilon}} g_m = \frac{-0.1}{\sqrt{0.7056 + 10^{-8}}} \times -0.84 = 0.09$$

$$\Delta c = \frac{-0.1}{\sqrt{17.64 + 10^{-8}}} \times -4.2 = 0.09$$

$$4. \quad m = m + \Delta m = 1 + 0.09 = 1.09$$

$$C = C + \Delta C = -1 + 0.09 = -0.91$$

$$8. \quad \text{sample} = \text{sample} + 1 \\ 1 + 1 = 2$$

$$9. \quad \text{if}(\text{sample} > n_s) \quad \text{step 10} \\ 2 > 2 \\ \text{else} \quad \text{step 4}$$

$$9. \quad g_m = -(3.8 - (1.09)(0.4) + 0.91)0.4 = -1.2$$

$$g_c = -(3.8 - (1.09)(0.4) + 0.91) = -4.27$$

$$5. \quad q_m = 0.7056 + (1.7)^2 = 3.59$$

$$q_c = 17.64 + (-4.27)^2 = 35.87$$

$$6. \quad \Delta m = \frac{-0.1}{\sqrt{3.59 + 10^8}} \times -1.2 = 0.08$$

$$\Delta C = \frac{-0.1}{\sqrt{35.87 + 10^8}} \times -4.27 = 0.07$$

$$7. \quad m = m + \Delta m = 1.17$$

$$C = C + \Delta C = -0.84$$

$$8. \quad \text{sample} = \text{sample} + 1 = 2 + 1 = 3$$

$$9. \quad \text{if}(\text{sample} > n_s) \quad \text{step 10} \\ 3 > 2 \\ \text{else} \quad \text{goto step 4}$$

$$10. \quad \text{iter} = \text{iter} + 1 = 1 + 1 = 2$$

$$11. \quad \text{if}(\text{iter} > \text{epochs}) \quad \text{goto step 12} \\ 2 > 2 \\ \text{else} \quad \text{goto step 3}$$

$$3. \quad \text{sample} = 1$$

$$4. \quad g_m = -(3.4 - (1.17)(0.2) + 0.84)0.2 = -0.30$$

$$g_c = -(3.4 - (1.17)(0.2) + 0.84) = -4.0$$

$$5. \quad G_m = 3.59 + (-0.3)^2 = 4.23$$

$$G_c = 35.89 + (-4.0)^2 = 51.89$$

$$6. \quad \Delta m = \frac{-0.1}{\sqrt{4.23 + 10^{-8}}} \times -0.8 = 0.038$$

$$\Delta C = \frac{-0.1}{\sqrt{51.89 + 10^{-8}}} \times -4.0 = 0.05$$

$$7. \quad m = m + \Delta m = 1.208$$

$$C = C + \Delta C = -0.79$$

$$8. \quad \text{sample} = \text{sample} + 1 = 1 + 1 = 2$$

$$9. \quad \text{if (sample} \geq n_s) \quad \text{step 10}$$

$$2 > 2$$

$$\text{else step 4.}$$

$$4. \quad g_m = -(3.8 - (1.20)(0.4) + 0.79) \times 0.4 = -1.64$$

$$g_c = -(3.8 - (1.20)(0.4) + 0.79) = -4.11$$

$$5. \quad G_m = 4.23 + (-1.64)^2 = 6.9$$

$$G_c = 51.89 + (-4.11)^2 = 68.7$$

$$6. \quad \Delta m = \frac{-0.1}{\sqrt{6.9 + 10^{-8}}} \times -1.64 = 0.06$$

$$\Delta C = \frac{-0.1}{\sqrt{68.7 + 10^{-8}}} \times -4.11 = 0.04$$

$$7. \quad m = m + \Delta m = 1.26$$

$$C = C + \Delta C = -0.75$$



8.  $\text{sample} = \text{sample} + 1 = 2 + 1 = 3$

9. if ( $\text{sample} > n$ ) step 10

$$3 > 2$$

else

step 4

10.  $\text{iter} = \text{iter} + 1$

$$\begin{aligned} & 2 + 1 \\ & = 3 \end{aligned}$$

11. if ( $\text{iter} > \text{epochs}$ ) step 12

$$3 > 2$$

else

step 3.

12.  $m = 1.26$

$$C = -0.75 //$$