

# Assignment-3

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Sample (i)	$X_i^2$	$Y_i^2$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

→ Do manual calculations for 2 iterations with 1st 2 samples.

→ Write python code to build simple linear regression model using SGD optimizer (consider all 4 samples)

step 1:  $[x, y], m=1, c=-1, \eta=0.1, \text{epochs}=2, n_s=2$

step 2:  $\text{itr}=1$

step 3:  $\text{sample}=1$

$$\text{step 4: } \frac{dE}{dm} = (-3.4(1))(0.2) - (-1)(0.2) \\ = -0.84$$

$$\frac{dE}{dc} = -(3.4)(1)(0.2+1) \\ = -4.2$$

$$\text{step 5: } \Delta m = -(0.1)(-0.84) = 0.084$$

$$\Delta c = -(0.1)(-4.2) \\ = 0.42$$

$$\text{step 6: } m = m + \Delta m$$

$$1 + 0.084 = 1.084$$

$$c = c + \Delta c$$

$$= -1 + 0.42 = -0.58$$

$$\text{step 7: } \text{sample} += 1 \Rightarrow 1+1=2$$

$$\text{step 8: } \text{if } (\text{sample} > n_s)$$

$$2 > 2$$

goto step 9

else  
goto step 4

$$\text{step 4: } \frac{\partial F}{\partial m} = -(3.8 - (1.084)(0.4) + 0.58)0.4$$
$$\frac{\partial F}{\partial m} = -1.57$$

$$\frac{\partial E}{\partial c} = -(3.8 - (1.084)(0.4) + 0.58)$$
$$= -3.9464$$

$$\text{step 5: } \Delta m = -(0.1)(-1.5785) = 0.157$$

$$\Delta c = -(0.1)(-3.9464) = 0.3966$$

$$\text{step 6: } \text{sample} = 2 + 1 = 3$$

$$\text{step 7: } m = m + \Delta m = 1.084 + 0.157$$
$$= 1.2418$$

$$c = c + \Delta c = -0.58 + 0.3946$$
$$= -0.1854$$

step 8: if (sample > n<sub>s</sub>)

$$3 > 2$$

goto step-9

else goto step-4

step 9: i<sub>bt</sub> = 1

$$1 + 1 = 2$$

step 10: if (i<sub>bt</sub> > epochs)

$$2 > 2$$

goto step-11

else

goto step-3

step 3 - sample = 1

$$\text{step 4 - } \frac{\partial E}{\partial m} = -(3.4 - (1.2)(0.2) + 0.18)0.2$$
$$= -(3.34)0.2 = -0.668$$

$$\frac{\partial E}{\partial c} = -(3.4 - (1.2)(0.2) + 0.18)$$

$$= -3.34$$

step 5:  $\Delta m = -(0.1)(-0.668)$

$$= 0.0668$$

step 6:  $m = m + \Delta m \Rightarrow 1.24 + 0.0668 = 1.3$

$$c = c + \Delta c = 0.18 + 0.33 = 0.15$$

step 7: sample = sample + 1

$$= 1 + 1 = 2$$

step 8: if (sample > n<sub>s</sub>)

$$2 > 2$$

goto step 9

else

goto step -4

step 4:  $\frac{\partial E}{\partial m} = -(3.8 - (1.3)(0.4) - 0.15)0.4$

$$= -1.25$$

$$\frac{\partial E}{\partial c} = -(3.8 - (1.3)(0.4) - 0.15)$$

$$= -3.13$$

step 5:  $\Delta m = -(0.1)(-1.25) = 0.12$

$$\Delta c = -(0.1)(-3.13) = 0.31$$

step 6:  $m = m + \Delta m = 1.3 + 0.12 = 1.42$

$$c = c + \Delta c = 0.15 + 0.31 = 0.46$$

step 7: sample = sample + 1

step 8: if (sample > n<sub>s</sub>)

$$3 > 2$$

goto step 9

else

goto step -4

step 9  $iter = iter + 1$   
 $= 2 + 1 = 3$

step 10 if ( $itr > epochs$ )

$3 > 2$

goto step -11

else

goto step -3

step -11 print m & c

$m = 1.42, c = 0.46$