

Assignment - 7 &

develop a sample linear Regression model by using BGD.

Step 1: $[x, y], m=1, c=-1, \eta=0.1, \text{epochs}=2,$
 $ns=2$

step 2: iter = 1

$$\text{step 3: } \frac{dE}{dm} = -\frac{1}{ns} \sum_{i=1}^{ns} (y_i - mx_i - c) x_i$$

$$= -\frac{1}{2} [(3.4 - (1)(0.2) + 1)0.2 + (3.8 - (1)(0.4) + 1)0.4]$$
$$= -1.34$$

$$\frac{dE}{dc} = -\frac{1}{2} [(3.4 - 0.2 + 1) + (3.8 - 0.4 + 1)]$$
$$= -4.3$$

$$\text{step 4: } \Delta m = -\eta \frac{dE}{dm}$$
$$= -0.1 \times -1.34 = 0.134$$

$$\Delta c = -\eta \frac{dE}{dc}$$
$$= -0.1 \times -4.3 = 0.43$$

$$\text{step 5: } m += \Delta m$$
$$= 1 + 0.134 = 1.134$$

$$c += \Delta c$$
$$= -0.1 + 0.43 = 0.33$$

$$\text{step 6: iter} += 1 \\ = 1 + 1 = 2$$

$$\text{step 7: if (iter > epochs): go to step 8} \\ 2 > 2$$

else: go to step 3

$$\text{step 3: } \frac{\partial \epsilon}{\partial m} = -\frac{1}{2} \left[(3.4 - (1.34)(0.2) + 0.51) \right. \\ \left. (0.2) + (3.8 - (1.134)(0.4) + 0.57) \right. \\ \left. (0.4) \right] \\ = -1.157$$

$$\frac{\partial \epsilon}{\partial c} = -\frac{1}{2} \left[(3 + (1.134)(0.2) + 0.57) + (3.8 - \right. \\ \left. (1.134)(0.4) + 0.57) \right] \\ = -3.829$$

$$\text{step 4: } \Delta m = -0.1 \times -1.157 = 0.1157$$

$$\text{step } \Delta c = -0.1 \times -3.829 = 0.3829$$

$$\text{step 5: } m += \Delta m \Rightarrow 1.134 + 0.1157 \Rightarrow 1.2497$$

$$c += \Delta c \Rightarrow -0.57 + 0.3829 \Rightarrow -0.187$$

$$\text{step 6: iter} += 1 \Rightarrow 2 + 1 = 3$$

$$\text{step 7: if (iter > epochs): go to step 8} \\ 3 > 2$$

else: go to step 3

$$\text{step 8: } m = 1.2497, c = -0.187$$