

Assignment - III

let us consider sample data set have one I/p ($x_i a$) and one output ($y_i a$) and no. of samples. develop a sample Regression model using stochastic gradient descent optimiser.

Sample (i)	$x_i a$	$y_i a$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

step 1: $x, y, m=1, c=-1, \eta=0.1, \text{epochs}=2, ns=2$

step 2: $itr=1$

step 3: sample = 1

$$\text{step 4: } \frac{dE}{dm} = -(8.4 - (1)) (0.2 - (-1)) 0.2$$
$$= -0.84$$

$$\frac{\partial E}{\partial c} = -(3.4 - (1)) (0.2 + 1) = -4.2$$

$$\text{step 5: } \Delta m = -(0.1) (-0.84) = 0.084$$
$$\Delta c = -(0.1) (-4.2) = 0.42$$

$$\text{step 6: } m = m + \Delta m \Rightarrow 1 + 0.084 = 1.084$$

$$c = c + \Delta c \Rightarrow -1 + 0.42 = -0.58$$

$$\text{step 7: sample} = 1$$
$$= 1 + 1 = 2$$

step 8: if (sample > ns)

$$2 > 2$$

go to step 9

else

go to step 4

$$\text{step 4: } \frac{\partial F}{\partial m} = -(3.8 - (1.084)(0.4) + 0.58)0.4$$

$$= -1.5785$$

$$\frac{\partial E}{\partial c} = -(3.8 - (1.084)(0.4) + 0.58)$$

$$= -3.9464$$

$$\text{step 5: } \Delta m = -(0.1)(-1.5785) = 0.1578$$

$$\Delta c = (0.1)(-3.9464) = 0.3846$$

$$\text{step 6: } m = m + \Delta m = 1.084 + 0.1578 = 1.2418$$

$$c = c + \Delta c = -0.58 + 0.3946 = -0.1854$$

$$\text{step 7: } \text{sample} + 1 = 2 + 1 = 3$$

step 8: if (sample > ns)

$$3 > 2$$

go to step 9

else

go to step 4

$$\text{step 9: } \text{itr} + 1 = 1$$

$$= 1 + 1 = 2$$

$$\text{step 10: if (itr > epochs)}$$

$$2 > 2$$

go to step 11

else

go to step 3

step 3 : sample = 1

$$\text{step 4 : } \frac{de}{dm} = -(3.4 - (1.2)(0.2) + 0.18)0.2$$
$$= -0.668$$

$$\frac{de}{dc} = -(3.4 - (1.2)(0.2) + 0.18)$$
$$= -3.34$$

$$\text{step 5 : } \Delta m = -(0.1)(-0.668)$$
$$= 0.0668$$

$$\text{step 6 : } m = m + \Delta m = 1.24 + 0.066 = 1.3$$

$$c = c + \Delta c = 0.18 + 0.33 = 0.15$$

$$\text{step 7 : } \text{sample} + 1$$
$$= 1 + 1 = 2$$

$$\text{step 8 : if (sample > ns)}$$
$$2 > 2$$

go to step 9

else

go to step 4

$$\text{step 4 : } \frac{de}{dm} = -(3.8 - (1.3)(0.4) - 0.15)0.4$$
$$= -1.25$$

$$\frac{de}{dc} = -(3.8 - (1.3)(0.4) - 0.15)$$
$$= -3.13$$

$$\text{step 5 : } \Delta m = -(0.1)(-1.25) = 0.12$$

$$\Delta c = -(0.1)(-3.13) = 0.31$$

step 6: $m = m + \Delta m = 1.3 + 0.12 = 1.42$

$$c = c + \Delta c = 0.15 + 0.31 = 0.46$$

step 7: $\text{sample} = \text{sample} + 1$
 $= 2 + 1 = 3$

step 8: if (sample > ns)

$$3 > 2$$

go to step 9

else

go to step 4

step 9: $\text{iter} = \text{iter} + 1$

$$= 2 + 1 = 3$$

step 10: if (iter > epochs)

$$3 > 2$$

go to step 11

else

go to step 3

step 11: print m & c

$$m = 1.42 \quad c = 0.46$$