

Assignment-2:

Find the global minimum point and value for the function $f(x, y) = x^2 + y^2 + 10$.

Do manual calculation for 2 iterations.

Step 1: $x = -1, y = 1, \eta = 0.1, \text{epochs} = 2$

Step 2: $\text{iter} = 1$

Step 3: $\frac{\partial f}{\partial x} = 2x = -2$

$$\frac{\partial f}{\partial y} = 2y = 2$$

Step 4: $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-2) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(2) = -0.2$$

Step 5: $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

Step 6: $\text{iter} = \text{iter} + 1 = 1 + 1 = 2$

Step 7: if ($\text{iter} > \text{epochs}$)

$2 > 2$
false
goto step 3

Step 3: $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

Step 4: $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-1.6)$

$$\Delta x = 0.16$$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(1.6) = -0.16$$

Step 5: $x = x + \Delta x = -0.8 + 0.16 = -0.64$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

Step 6: $\text{iter} = \text{iter} + 1 = 2 + 1 = 3$

Step 7: $\text{if}(\text{iter} > \text{epochs})$
 $3 > 2$

True
goto next step

Step 8: print ~~x~~ y values, $f(x, y)$

$$x = -0.64$$

$$y = 0.64$$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$f(x, y) = \underline{\underline{10.81}}$$