

Assignment - 2 :-

18K41A0400

Find the global minimum point and value for the function $f(x, y) = x^2 + y^2 + 10$

Do manual calculation for 2 iterations

Step 1: $x = -1, y = 1, \eta = 0.1, \text{epochs} = 2$

2) iter = 1

3) $\frac{\partial f}{\partial x} = 2x = -2$ $\frac{\partial f}{\partial y} = 2y = 2$

4) $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-2) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(2) = -0.2$$

5) $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

6) iter = iter + 1 = 1 + 1 = 2

7) if (iter > epochs)

$2 > 2$

false

goto step 3

3) $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

4) $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-1.6)$

$$\Delta x = 0.16$$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(1.6) = -0.16$$

$$5) x = x + \Delta x = -0.8 + 0.16 = -0.64$$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

$$6) \text{ iter} = \text{iter} + 1 = 2 + 1 = 3.$$

$$7) \text{ if } (\text{iter} > \text{epochs})$$

$$3 > 2.$$

true.

goto next step.

$$8) \text{ print } x, y \text{ values, } f(x, y)$$

$$x = -0.64$$

$$y = 0.64$$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$f(x, y) = 10.81$$