

## Assignment-2

- 18K41A0502

find the global minimum point and value for the function  $f(x,y) = x^2 + y^2 + 10$

- Do manual calculations for two iterations
- find the optimal solution using python programming.

S-1:  $x = -1$   $y = +1$   $\eta = 0.1$  epochs = 2

S-2: itr = 2

S-3:  $\frac{df}{dx} = 2x = -2$

$$\frac{df}{dy} = 2y = 2$$

S-4:  $\Delta x = -\eta \frac{df}{dx} = -2(-0.1)$

$$= +0.2$$

$$\Delta y = -\eta \frac{df}{dy} = -(0.1)(2)$$

$$= -0.2$$

S-5:  $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

S-6: itr = itr + 1  
 $= 1 + 1 = 2$

S-7: if (itr > epochs)

goto S-5

else

goto S-3

S-3:  $\frac{df}{dx} = 2x = 2(-0.8) = -1.6$

$$\frac{df}{dy} = 2y = 2(0.8) = 1.6$$

$$S-4: \Delta x = -\eta \frac{\partial f}{\partial x}$$

$$= - (0.1)(-1.6) = 0.16$$

$$\Delta y = -\eta \frac{\partial f}{\partial y}$$

$$= - (0.1)(1.6)$$

$$= -0.16$$

$$S-5: x = x + \Delta x$$

$$= 0.8 + 0.16$$

$$= 0.96$$

$$y = y + \Delta y$$

$$= 0.8 - 0.16$$

$$= 0.64$$

$$S-6: itr = itr + 1$$

$$= 2 + 1 = 3$$

$$S-7: \text{if } (itr > \text{epochs})$$

$$3 > 2$$

$$\text{goto } S-8$$

$$\text{else}$$

$$\text{goto } S-3$$

$$S-8: x = -0.64$$

$$y = 0.64$$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$= 0.4 + 0.4 + 10$$

$$= 10.8$$