

Assignment - 15

-18K41A0515

Let us consider a sample dataset have one input (x_i^a) and one output (y_i^a) and number of samples 2.
Develop a simple linear regression model using RMS prop optimizer.

sample(i)	x_i^a	y_i^a
1	0.2	3.4
2	0.4	3.8
3	0.6	2.2
4	0.8	4.6

Do manual calculations for 2 iterations with first two samples.

Step-1: $[x, y]$, $\eta = 0.1$, epochs = 2, $m = 1$, $b = -1$, $\theta = 0.9$,
 $E_m = E_c = 0$, $\epsilon = 10^{-8}$.

Step 2: $itr = 1$

steps: sample = 1

step 4: $g_m = -(3.4 - (1)(0.2) + 1)(0.2) = -0.84$

$g_c = -(3.4 - (1)(0.2) + 1) = -4.2$

steps: $E_m = (0.9)(0) + (1 - 0.9)(-0.84)^2 = 0.07$

$E_c = (0.9)(0) + (1 - 0.9)(-4.2)^2 = 1.764$

step 6: $\Delta m = \frac{-0.1}{\sqrt{0.07 + 10^{-8}}} * -0.84 = 0.31$

$$\Delta C = \frac{-0.1}{\sqrt{1.764 + 10^{-8}}} * -0.2 = 0.31$$

step 7: $m = m + \Delta m = 1 + 0.31 = 1.31$

$c = c + \Delta c = -1 + 0.31 = -0.69$

step 8: $sample = sample + 1$
 $= 1 + 1 = 2$

step 9: $if (sample > ns)$ goto step -10
 2 > 0

else
 goto step -4:

step 4: $g_m = -(3.8 - (1.31)(0.4) + 0.69)0.4 = -1.5$

$g_c = -(3.8 - (1.31)(0.4) + 0.69) = -3.9$

step 5: $E_m = (0.9)(0.07) + (0.1)(-1.5)^2 = 0.28$

$E_c = (0.9)(1.76) + (0.1)(-3.9)^2 = 3.1$

step 6: $\Delta m = \frac{-0.1}{\sqrt{0.28 + 10^{-8}}} * +1.5 = 0.28$

$\Delta c = \frac{-0.1}{\sqrt{3.1 + 10^{-8}}} * -3.9 = 0.22$

step 7: $m = m + \Delta m = 1.31 + 0.28 = 1.59$

$c = c + \Delta c = -0.69 + 0.22 = -0.47$

step 8: $sample = sample + 1$
 $= 2 + 1 = 3$

step 9: $if (sample > ns)$ goto step -10
 3 > 2
 else step 4

step-10: $itr = itr + 1$
 $-1 + 1 = 2$

step 11: $g(itr > epochs)$
goto step-12
clr
goto step-3

step-3: $sample = 1$

step 4: $g_m = -(3.4 - (1.59)(0.2) + 0.47)(0.2) = -0.7$
 $g_c = -(3.4 - (1.59)(0.2) + 0.47) = -3.5$

step 5: $E_m = (0.9)(0.28) + (0.1)(0.7)^2 = 0.3$
 $E_c = (0.9)(3.1) + (0.1)(-3.5)^2 = 4.0$

step 6: $\Delta m = \frac{-0.1}{\sqrt{0.3 + 10^{-8}}} * -0.9 = 0.12$

$\Delta c = \frac{-0.1}{\sqrt{4.0 + 10^{-8}}} * -3.5 = 0.17$

step 7: $m = m + \Delta m = 1.59 + 0.12 = 1.71$
 $c = c + \Delta c = -0.47 + 0.17 = -0.3$

step 8: $sample = sample + 1$
 $1 + 1 = 2$

step 9: $if (sample > ns)$
 $2 > 2$
goto step-10

clr
goto step-4

step 4: $g_m = -(3.8 - (1.71)(0.4) + 0.3) * 0.4 = -1.4$
 $g_c = -(3.8 - (1.71)(0.4) + 0.3) = -3.6$

Step 5: $E_m = (0.9)(0.3) + (0.1)(-1.4)^2 = 0.46$
 $E_c = (0.9)(4.0) + (0.1)(-3.6)^2 = 4.89$

Step 6: $\Delta m = \frac{-0.1}{\sqrt{0.46 + 10^{-8}}} \quad * -1.4 = 0.2$

$\Delta c = \frac{-0.1}{\sqrt{4.89 + 10^{-8}}} \quad * -3.6 = 0.16$

Step 7: $m = m + \Delta m = 1.71 + 0.2 = 1.91$
 $c = c + \Delta c = -0.3 + 0.16 = -0.14$

Step 8: $\text{sample} = \text{sample} + 1$
 $= 2 + 1 = 3$

Step 9: $\text{if}(\text{sample} \geq ns)$
 $372 \text{ goto step } -10$

else
 $\text{goto step } -11$

Step -10: $itr = itr + 1$
 $= 2 + 1 = 3$

Step -11: $\text{if}(itr \geq \text{epochs})$
 $372 \text{ goto step } -12$

else
 $\text{goto step } -3$

Step -12: $m = 1.91$
 $c = -0.14$