

ASSIGNMENT - II

18K41A0536
CSE-A

Nesterov Accelerated Gradient

(NAG) optimizer:-

sample	x_i^a	y_i^a
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Manual calculation:-

step 1: initialization

$$[x, y], \eta = 0.1, \gamma = 0.9, \text{epoch} = 10^2$$

$$m = 1, c = -1, v_m = v_c = 0, \beta =$$

step 2: iter = 1

step 3: sample = 1

$$\text{step 4: } \hat{f}_m = -(y_i - (m + \beta v_m)x_i - (c + \beta v_c)x_i)$$

$$g_m = -(3.4 - (1)(0.2) + 1)(0.2)$$

$$= 0.84$$

$$g_c = -(3.4 - (1)(0.2) + 1) = -4.2$$

$$v_m = \delta v_m - \eta g_m = 0 - (0.1)(0.84)$$

$$= 0.084$$

$$v_c = \delta v_c - \eta g_c = (0.9 \times 0) - (0.1)(-4.2)$$

$$v_c = 0.42$$

$$\text{Step 6: } m = m + v_m = 1 + 0.084 = 1.084$$

$$c = c + v_c = -1 + 0.42 = -0.58$$

$$\text{Step 7: } \text{sample} = 1 + 1 = 2$$

$$\text{Step 8: } \text{if } (2 > ns) \quad \text{if } (2 > 2)$$

go to step 4

else go to next step

$$\text{Step 4: } g_m = -(3.8 - (1.084 + (0.9)(0.084))$$

$$(0.4))$$

$$g_m = -1.41$$

$$g_c = -3.54$$

$$\text{step 5: } V_m = (0.9)(0.084) - (0.1)(-1.41)$$

$$V_m = 0.075 + 0.141$$

$$\boxed{V_m = 0.216}$$

$$V_c = (0.9)(0.42) - (0.1)(-3.54)$$

$$= 0.37 + 0.354$$

$$\boxed{V_c = 0.724}$$

$$\text{step 6: } m = 1.084 + 0.216 = 1.3$$

$$c = -0.8 + 0.724 = -0.076$$

$$\text{step 7: } m_x = 1.084 + 1.$$

$$\text{sample} = 3 > 2$$

true go to next step

$$\text{step 8: } it = 2$$

$$\text{step 9: } \text{if } (2 > 2) \text{ go to step 3}$$

$$\text{step 3: } \text{sample} = 1$$

$$\text{step 4: } g_m = -(3.4 - (1.3 + (0.9)(0.216)))$$

$$0.2$$

$$g_m = -(2.32)(0.2)$$

$$g_m = -0.46, \quad g_c = -2.32$$

$$\text{step 5: } V_m = (0.9)(0.216) - (0.1)(-0.46)$$

$$= 0.194 + 0.046$$

$$= 0.24$$

$$V_c = (0.9)(0.724) - (0.1)(-2.3)$$

$$= 0.65 + 0.23$$

$$\boxed{V_c = 0.88}$$

$$\text{Step 6: } m = 1.3 + 0.24 = 1.54$$

$$c = 0.14 + 0.88$$

$$c = 1.02$$

$$\text{step 7: } \text{sample} = 2 > 2$$

GO to step 4

$$\text{step 4: } g_m = -(3.8 - (1.54) + (0.9)(0.24))$$

$$0.4 - (1.02 + (0.9)(0.88)0.4)$$

$$g_m = -(3.8 - 0.7 - 1.81)0.4$$

$$g_m = -0.51$$

$$g_c = -1.29$$

$$\text{step 5: } V_m = (0.9)(0.24) - (0.9)(-0.51) \\ = 0.216 + 0.051$$

$$V_m = 0.26$$

$$V_c = (0.9)(0.88) - (0.1)(-1.29) \\ = 0.792 + 0.129$$

$$\boxed{V_c = 0.921}$$

$$\text{Step 6: } m = 1.54 + 0.26$$

$$\boxed{m = 1.80}$$

$$C = 1.028 + 0.921$$

$$\boxed{C = 1.941}$$

Step 7: $s = \text{sample} + 1 = 3 > 2$ True
go to next step

step 8: $it = 3$

step 9: if $(3 > 2)$ goto next step.

step 10: Print m & C values

$$m = 1.8$$

$$C = 1.941$$