

### ASSIGNMENT-3

Let us consider sample dataset have one Input ( $x_i$ ) and one output ( $y_i$ ) and number of samples develop a sample Regression model using stochastic Gradient descent optimizer

sample(i)	$x_i$	$y_i$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

→ DO Manual calculations for 2 iterations & sampler

Step 1:  $x, y, m=1, c=-1, \eta=0.1, \text{epoch}=2$   
 $ns=2$

Step 2:  $itr=1$

Step 3:  $\text{sample}=1$

$$\begin{aligned}\text{Step 4: } \frac{\partial \mathcal{L}}{\partial m} &= -(y_i - m \times x_i - c)(x_i) \\ &= -(3.4 - 1 \times 0.2 + 1)(0.2) \\ &= -0.84\end{aligned}$$



$$\frac{\partial F}{\partial c} = 7(3.4) - (3.4 - (1)(0.2) + 1)$$

$$= -4.2$$

Step 5:  $\Delta m = -\eta \frac{\partial F}{\partial m} = -(0.1)(-0.84)$

$$= 0.084$$

$$\Delta c = -(0.1)(-4.2)$$

$$= 0.42$$

Step 6:  $m = m + \Delta m$

$$= 1 + 0.084 = 1.084$$

$$c = c + \Delta c$$

$$= -1 + 0.42 = -0.58$$

Step 7:  $\text{sample} = \text{sample} + 1$

$$= 1 + 1$$

$$= 2$$

Step 8: if (sample > ns)

$$2 > 2$$

goto step 9

else

goto step 4

Step 4:



$$\text{step 4: } \frac{\partial F}{\partial m} = -(3.8 - (1.084)(0.4) + 0.58)(0.4) \\ = -1.5785$$

$$\frac{\partial F}{\partial c} = -(3.8 - (1.084)(0.4) + 0.58) \\ = -3.9464$$

$$\text{step 5: } \Delta m = -(0.1)(-1.5785) \\ = 0.1578$$

$$\Delta c = -(0.1)(-3.9464) \\ = 0.3946$$

$$\text{step 6: } m = m + \Delta m \\ = 1.084 + 0.1578 = 1.2418 \\ c = c + \Delta c \\ = -0.58 + 0.3946 \\ = -0.1854$$

$$\text{step 7: } \text{sample} = \text{sample} + 1$$

$$\text{step 8: } \text{if (sample} > \text{ns)} \\ 3 > 2$$

goto step 9  
else  
goto step 4



$$\begin{aligned}\text{step 9: } itx &= itx + 1 \\ &= 1 + 1 \\ &= 2\end{aligned}$$

$$\begin{aligned}\text{step 10: } &\text{if } (itx > \text{epochs}) \\ &\quad 2 > 2 \\ &\quad \text{goto step 11} \\ &\quad \text{else} \\ &\quad \text{goto step 3}\end{aligned}$$

$$\text{step 3: } \text{sample} = 1$$

$$\begin{aligned}\text{step 4: } \frac{\partial E}{\partial m} &= -(3.4 - (1.2)(0.2) + 0.18)0.2 \\ &= -(3.34)0.2 \\ &= 0.668\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} &= -(3.4 - (1.2)(0.2) + 0.18) \\ &= -3.34\end{aligned}$$

$$\begin{aligned}\text{step 5: } \Delta m &= -(0.1)(-0.668) \\ &= 0.0668\end{aligned}$$

$$\begin{aligned}\text{step 6: } m &= m + \Delta m = 1.24 + 0.066 = 1.306 \\ c &= c + \Delta c = 0.18 + 0.33 = 0.15\end{aligned}$$



step 7:  $\text{sample} = \text{sample} + 1$

$$= 1 + 1 = 2$$

step 8: if ( $\text{sample} > \text{ns}$ )

$$2 > 2$$

go to step 9

else

go to step 4

$$\text{step 4: } \frac{\partial E}{\partial m} = -(3.8 - (1.3)(0.4) - 0.15) 0.4$$

$$= -1.25$$

$$\frac{\partial E}{\partial c} = -(3.8 - (1.3)(0.4) - 0.15)$$

$$= -3.13$$

$$\text{step 5: } \Delta m = -(0.1)(-1.25) = 0.12$$

$$\Delta c = -(0.1)(-3.13) = 0.31$$

$$\text{step 6: } m = m + \Delta m = 1.3 + 0.12 = 1.42$$

$$c = c + \Delta c = 0.15 + 0.31 = 0.46$$

step 7:  $\text{sample} = \text{sample} + 1$

$$= 2 + 1 = 3$$

step 8: if ( $\text{sample} > \text{ns}$ )

$$3 > 2$$



goto step 9

else

goto step 4

step 9:  $iter = iter + 1$   
 $= 2 + 1 = 3$

step 10: if ( $iter > epoch$ )  
 $3 > 2$

go to step 11

else

goto step 3

step 11: Print  $m$  &  $c$

$m = 1.42$        $c = 0.46$