

## ASSIGNMENT-5

Let us consider a sample dataset have one input ( $x_i$ ) and one output ( $y_i$ ) and number of samples of, Develop a SLR model using MBGD?

sample (i)	$x_i$	$y_i$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

→ Do Manual calculations for 2 iterations  
with  $bs=2$

batch -1	x	y
	0.2	3.4
	0.4	3.8
batch 2	0.6	4.2
	0.8	4.6

### Steps

Step 1 :  $[x, y]$ ,  $\eta=0.1$ , epochs = 2,  $bs=2$

$$m=1, c=-1$$



$$\text{step 2: } nb = \frac{ns}{bs} = \frac{4}{2} = 2$$

$$\text{step 3: } iter = 1$$

$$\text{step 4: } Batch = 1$$

$$\text{step 5: } \frac{\partial E}{\partial m} = -\frac{1}{bs} \sum_{i=1}^{bs} (y_i - mx_i - c)x_i$$

$$= -\frac{1}{2} [(3.4 - 1(0.2) + 1)0.2] \\ + [3.8 - 0.4 + 1]0.4]$$

$$= -1.34$$

$$\frac{\partial E}{\partial c} = -\frac{1}{2} [(3.4 - 0.2 + 1) + (3.8 - 0.4 + 1)]$$

$$= -4.3$$

$$\text{step 6: } \Delta m = -(0.1)(-1.34) = 0.134$$

$$\Delta c = -(0.1)(-4.3) = 0.43$$

$$\text{step 7: } m = m + \Delta m = 1 + 0.134 = 1.134$$

$$c = c + \Delta c = -1 + 0.43 = -0.57$$

$$\text{step 8: } Batch = Batch + 1$$

$$1 + 1 = 2$$

$$\text{step 9: } \text{if } (Batch > nb)$$

go to step 10



else

goto step 5

$$\begin{aligned}\text{step 5: } \frac{\partial f}{\partial m} &= -\frac{1}{2} \left[ (4.2) - [1.134)(0.6) + 0.57) \right. \\ &\quad \left. + (4.6 - (1.134)(0.8) + 0.57) \right] \\ &= -4.1762\end{aligned}$$

$$\text{step 6: } \Delta m = -(0.1)(-2.932) = 0.2932$$

$$\Delta c = -(0.1)(-4.1762) = 0.41762$$

$$\begin{aligned}\text{step 7: } m &= m + \Delta m = 1.134 + 0.2932 \\ &= 1.4272\end{aligned}$$

$$\begin{aligned}c &= c + \Delta c = -0.57 + 0.4176 \\ &= -0.1523\end{aligned}$$

$$\text{step 8: } \text{Batch} = \text{Batch} + 1$$

$$\Rightarrow 2 + 1 = 3$$

$$\text{step 9: } \text{if } (\text{Batch} > nb) \quad \text{go to step 10}$$

$$3 > 2$$

$$\text{else go to step 5}$$

$$\text{step 10: } \text{iter} = \text{iter} + 1$$

$$= 1 + 1 = 2$$



Step 11: if (iter > epochs) : go to step 12  
2 > 2  
else : goto step 4

Step 4: Batch = 1

Step 5:  $\frac{\partial E}{\partial m} = -\frac{1}{2} \left[ (3.4) - (1.4272)(0.2) + 0.1523 \right]$   
 $0.2 + (3.8 - (1.4272)(0.4) + 0.1523)(0.4)$

$$\frac{\partial E}{\partial m} = -1.0029$$

$$\frac{\partial E}{\partial c} = -\frac{1}{2} \left[ (3.4) - (1.4272)(0.2) + 0.1523 \right] +$$
$$(3.8 - (1.4272)(0.4) + 0.1523)$$
$$= -3.3241$$

Step 6:  $\Delta m = (-0.1) (-1.0029) \Rightarrow 0.1002$

$\Delta c = (-0.1) (-3.3241) \Rightarrow 0.332$

Step 7:  $m = m + \Delta m \Rightarrow 1.4272 + 0.1002$   
 $= 1.5274$

$c = c + \Delta c \Rightarrow -0.1523 + 0.332$   
 $= 0.1797$

Step 8: Batch = Batch + 1

$$1 + 1 = 2$$



step 9: if (Batch > nb) goto step 10

else

goto step 5

$$\begin{aligned}\text{step 5: } \frac{\partial E}{\partial m} &= -\frac{1}{2} \left[ (4.2 - (1.5274)(0.6) - 0.1797)0.6 \right. \\ &\quad \left. + [4.6 - (1.5274)(0.8) - 0.1797]0.8 \right] \\ &= -2.21\end{aligned}$$

$$\frac{\partial E}{\partial c} = -3.151$$

$$\text{step 6: } \Delta m = -0.1 \times -2.21$$

$$\boxed{\Delta m = 0.221}$$

$$\Delta c = -0.1 \times -3.151$$

$$\boxed{\Delta c = 0.315}$$

$$\text{step 7: } m = m + \Delta m$$

$$= 1.5274 + 0.221 = 1.748$$

$$c = c + \Delta c = 0.1797 + 0.315$$

$$= 0.494$$

$$\text{step 8: } \text{Batch} = \text{Batch} + 1$$

$$= 2 + 1 = 3$$



step 9: if (epochs > 10)  
if (Batch > nb) go to step 10  
else  
goto step 5

step 10: iter = iter + 1  
 $2 + 1 \Rightarrow 3$

step 11: if (iter > epochs) ( $3 > 2$ )  
goto step 12  
else goto step 4

step 12: print m & C

$m = 1.748$

$C = 0.494$