

Assignment 5

* Mini batch Gradient descent Algo

sample(i)	x_i	y_i
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

→ Manual Calculations

→ $itc = 2$

→ $n_s = 4$

→ Step 1: $[x, y]$, $m = 1$, $c = -1$, $\eta = +0.1$
epochs = 2, $n_s = 4$, $b_s = 2$

$$nb = (n_s / b_s) = 2$$

Step 2: $it = 1$, Step 3: $bt = 1$

$$\text{Step 4: } \frac{\partial E}{\partial m} = -\frac{1}{b_s} \sum_{i=1}^{b_s} (y_i - mx_i - c) x_i$$

$$= -\frac{1}{2} \left[(3.4 - 1(0.2) + 1)(0.2) + (3.8 - 1(0.4) + 1)(0.4) \right]$$

$$= -\frac{1}{2} \left[(4.2)(0.2) + (4.4)(0.4) \right]$$

$$= -\frac{1}{2} [0.84 + 1.76]$$

$$\begin{array}{r} 4.2 \\ 0.2 \\ \hline 4.4 \\ 0.4 \\ \hline 4.8 \\ 0.6 \\ \hline 5.4 \\ 0.8 \\ \hline 6.2 \end{array}$$

$$= -\frac{1}{2} \left[(4 \cdot 2)(0 \cdot 2) + (4 \cdot 4)(0 \cdot 4) \right] \quad \begin{array}{r} 0.84 \\ 1.76 \\ \hline 2.60 \end{array}$$

$$= -\frac{1}{2} \left[0.84 + 1.76 \right]$$

$$= -\frac{1}{2} (2.6) = \cancel{0} - 1.3 \checkmark$$

$$\frac{\partial E}{\partial b_j} = -\frac{1}{b_j} \sum_{i=1}^n (y_i - m x_i - c)$$

$$= -\frac{1}{2} \left[(3 \cdot 4 - 1(0.2) + 1) + (3 \cdot 8 - 1(0.4) + 1) \right]$$

$$= -\frac{1}{2} \left[4 \cdot 2 + 4 \cdot 4 \right]$$

$$= -\frac{1}{2} \left[\begin{array}{r} 4.2 \\ 8.6 \end{array} \right]$$

Step 5, $\Delta m = (-1)(-1.3)$

$$= (-0.1)(-1.3)$$

$$= 0.13$$

$\Delta c = (-0.1)(-4.2)$

$$= 0.42$$

$$\text{step 6, } m = 1 + 0.13$$

$$= 1.13$$

$$c = -1 + 0.43$$

$$= -0.57$$

$$\text{step 7 : } bt = 2$$

step 8 : $2 > 2$ false go to step 4,

$$\begin{array}{r} 1.13 \\ 0.43 \\ \hline 0.5 \end{array}$$

Step 4:

$$\begin{aligned}
 &= -\frac{1}{2} \left[(4.2 - (1.13)(0.6) + 0.57) 0.6 \right. \\
 &\quad \left. + (4.6 - (1.13)(0.8) + 0.57) 0.8 \right] \\
 &= -\frac{1}{2} (2.4552 + 3.41) \\
 &= -\frac{1}{2} (5.865) \\
 &= -2.93 \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \frac{\partial E}{\partial c} &= -\frac{1}{2} \left[(4.2 - (1.13)(0.6) + 0.57) \right. \\
 &\quad \left. + (4.6 - (1.13)(0.8) + 0.57) \right] \\
 &= -\frac{1}{2} (4.092 + 4.266) \\
 &= -\frac{1}{2} (8.358) \\
 &= -4.179
 \end{aligned}$$

Step 5: $\Delta m = (-\eta) (-2.93)$

$$= -(0.1) (-2.93)$$

$$= 0.293$$

$$\Delta c = (-0.1) (-4.17)$$

$$= 0.417$$

Step 6: $m = 1.13 + 0.293$

$$m = 1.423$$

$$\begin{array}{r} 1.130 \\ 0.293 \\ \hline 1.423 \end{array}$$

$$c = -0.57 + 0.417$$

$$= -0.153$$

Step 7: $bt = 3$

Step 8: if $(bt \leq nb)$ go to Step 9

else ~~stop~~ next step

Step 9: $it = 2$

Step 10: if $(it > epochs)$ next step

else

go to Step 3.