

# Assignment - 13

## ADAGRAD Optimizing technique

sample (i)	$x_i$	$y_i$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

→ Manual Calculations.

Step 1 :-  $[x, y], \eta = 0.1, ep = 2, m = 1, c = 1$   
 $G_m = G_c = 0, \epsilon = 10^{-8}$

Step 2 :  $it = 1$       Step 3 :  $sample = 1$

$$\begin{aligned} \text{Step 4 : } g_m &= -(3.4 - 1(0.2) + 1)0.2 \\ &= -0.84 \\ g_c &= -(3.4 - 1(0.2) + 1) \\ &= -4.2 \end{aligned}$$

$$\begin{aligned} \text{Step 5 : } G_m &= G_m + (g_m)^2 \\ &= 0 + (-0.84)^2 \\ &= 0.7056 \end{aligned}$$

$$\begin{aligned} G_c &= G_c + (g_c)^2 = 0 + (-4.2)^2 \\ &= 17.64 \end{aligned}$$



Step 6:

$$\Delta m = \frac{-\eta}{\sqrt{\eta_m + \epsilon}} g_m$$

$$\Delta c = \frac{-\eta}{\sqrt{\eta_c + \epsilon}} g_c$$

$$\Delta m = \frac{-0.1}{\sqrt{0.704 + 10^{-8}}} (-0.84)$$

$$= \frac{-0.084}{0.836}$$

$$= +0.1$$

$$\Delta c = \frac{-0.1}{\sqrt{17.64 + 10^{-8}}} \times (-4.2)$$

$$= \frac{-0.42}{4.2}$$

$$= +0.1$$

Step 7:

$$m = 1 + 0.1$$

$$= 1.1$$

$$c = -1 - 0.1$$

$$= -0.9 \checkmark$$

$$\frac{1 - 0.1}{1 + 0.1}$$

$$= 1.1$$

$$\frac{-1 + 0.1}{-1 - 0.1}$$

$$= -0.9 \checkmark$$



Step 8:  $s = 2$

Step 9: if  $(s > n_s)$  go to next step  
else go to Step 4

$$\begin{aligned} \text{Step 4: } g_m &= - (3.8 - (1.1)(0.4) \\ &\quad + 0.9)0.4 \\ &= - (4.7 - 0.44)0.4 \\ &= -1.7 \end{aligned}$$

$$g_c = -4.26$$

Step 5: 
$$h_m = 0.7056 + (-1.7)^2$$

$$= 3.59$$

$$\begin{aligned} h_c &= 17.64 + (-4.26)^2 \\ &= 35.78 \end{aligned}$$

Step 6: 
$$\Delta m = \frac{-0.1}{\sqrt{3.59 + 10^{-8}}} (-1.7)$$

$$= \frac{0.17}{1.89}$$

$$= 0.089$$



$$\Delta C = \frac{-0.1}{\sqrt{25.71 + 20}} (-4.26)$$

$$= \frac{0.426}{5.98}$$

$$= 0.07 \checkmark$$

Step 7:  $m = 1.1 + 0.089$

$$= 1.189 \checkmark$$

$$c = -0.9 + 0.07$$

$$= -0.83 \checkmark$$

Step 8:  $s = 3 > n$ , go to next step

Step 9:  $it = 2$

Step 10: if  $(2 > 2)$  go to Step 3.

Step 3: sample = 1

Step 4:

$$g_m = - (3.4 - ((1.189)(0.2) + 0.83)) 0.2$$

$$= - \left( \frac{4.23 - 0.23}{4} \right) 0.2$$

$$= -0.8$$

$$g_c = - (3.4 - ((1.189)(0.2) + 0.83))$$

$$= -4$$



$$\text{Step 5: } G_m = 3.59 + (-0.8)^2$$

$$= 4.23$$

$$G_c = 35.78 + (-4)^2$$

$$= 51.78$$

$$\text{Step 6: } \Delta m = \frac{-0.1}{\sqrt{4.23 + 25^8}} \times (-0.8)$$

$$= \frac{0.08}{2.056}$$

$$= 0.038$$

$$\Delta c = \frac{(-0.1)(-4)}{\sqrt{51.78 + 25^8}}$$

$$= \frac{0.4}{7.195}$$

$$= 0.056$$

$$\text{Step 7: } m = 1.489 + 0.038 = 1.227$$

$$c = -0.83 + 0.056$$

$$= -0.774$$



Step 8:  $s = 2$

Step 9:  $2 > n_s$  go to step 4.

Step 4:

$$g_m = - \left( 3.8 - (1.227)(0.4) + 0.274 \right) 0.4$$

$$= - (4.574 - 0.49) 0.4$$

$$= - (4.084) (0.4)$$

$$= -1.633$$

$$g_c = -4.084$$

$$\begin{aligned} \text{Step 5: } h_m &= 4.23 + (-1.633)^2 \\ &= 6.89 \end{aligned}$$

$$\begin{aligned} h_c &= 51.78 + (4.084)^2 \\ &= 68.45 \end{aligned}$$

$$\begin{aligned} \text{Step 6: } \Delta m &= \frac{-0.1}{\sqrt{6.89 + 50^8}} (-1.633) \\ &= \frac{0.0633}{2.6248} \\ &= 0.024 \end{aligned}$$



$$DC = \frac{(6.1)(-4.084)}{\sqrt{68.45 + 10^{-8}}}$$

$$= \frac{0.4084}{8.2734}$$

$$= 0.049 \checkmark$$

Step 7,  $m = 1.227 + 0.024$   
 $= 1.251$

$$C = -0.774 + 0.049$$

$$= -0.725$$