

### Assignment - 3.

\* Stochastic gradient descent optimizes

Sample(i)	$X_i$	$Y_i$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

→ Manual calc.

Step 1 :  $[x, y]$ ,  $m = 1$ ,  $c = -1$ ,  $\eta = 0.1$ ,

epochs = 2

Step 2 : ite = 1

Step 3 : sample = 1

Step 4 :  $\frac{\partial E}{\partial m} = -(y_i - m(x_i) - c)x_i$

$$= -(3.4 - 1(0.2) + 1)0.2$$

$$= -0.84$$

$$\frac{\partial E}{\partial c} = -(y_i - m(x_i) - c)$$

$$= -(3.4 - 1(0.2) + 1)$$

$$= -4.2$$



$$\begin{aligned}\text{Step 5: } \Delta m &= -\eta \left( \frac{\partial E}{\partial m} \right) \\ &= (-0.4) (-0.84) \\ &= 0.084\end{aligned}$$

$$\begin{aligned}\Delta c &= -\eta \left( \frac{\partial E}{\partial c} \right) \\ &= (-0.4) (-4.2) \\ &= 0.42\end{aligned}$$

$$\begin{aligned}\text{Step 6: } m &= m + \Delta m = 1 + 0.084 = 1.084 \\ c &= c + \Delta c = -1 + 0.42 \\ &= -0.58\end{aligned}$$

$$\text{Step 7: } \text{sample}++ = 2$$

Step 8: if (sample >  $n_s$ ) next  
else go to step 4.

$$\begin{aligned}\text{Step 4: } \frac{\partial E}{\partial m} &= - \left( 3.8 - (1.084)(0.4) \right. \\ &\quad \left. + 0.58 \right) 0.4 \\ &= - (3.8 - 0.43 + 0.58) 0.4 \\ &= - (3.95) 0.4 \\ &= - 1.58\end{aligned}$$



$$\frac{\partial E}{\partial c} = - \left( 3.8 - (1.084)(0.4) + 0.58 \right)$$

$$= -3.95$$

Steps:

$$\Delta m = -(0.1)(-1.58)$$

$$= 0.158$$

$$\Delta c = -(0.1)(-3.95)$$

$$= 0.395$$

Steps:

$$m = 1.084 + 0.158$$

$$= 1.242$$

$$c = -0.58 + 0.395$$

$$= -0.185$$

Step 7: sample = 3

Step 8: if (sample >  $n_s$ )  
next.

Step 9: it = it + 1      2 ✓

Step 10: if (it > epoch)      2  
next  
else  
goto Step 3



59)

step 3 : sample = 1

$$\begin{aligned}
 \text{step 4 : } \frac{\partial E}{\partial m} &= -(y_i - m(x_i) - c) \cdot x_i \\
 &= -(3.4 - (1.242)(0.2) + 0.185) \cdot 0.2 \\
 &= -(3.4 - (0.24) + 0.185) \cdot 0.2 \\
 &= -(3.34)(0.2) \\
 &= -0.66
 \end{aligned}$$

$$\begin{aligned}
 \frac{\partial E}{\partial c} &= -(3.4 - (0.24) + 0.185) \\
 &= -3.34
 \end{aligned}$$

$$\begin{aligned}
 \text{step 5 : } \Delta m &= -(0.1)(-0.66) \\
 &= 0.066
 \end{aligned}$$

$$\begin{aligned}
 \Delta c &= -(0.1)(-3.34) \\
 &= 0.334
 \end{aligned}$$

$$\begin{aligned}
 \text{step 6 : } m &= 1.242 + 0.066 \\
 &= 1.3
 \end{aligned}$$

$$\begin{aligned}
 c &= -0.185 + 0.334 \\
 &= 0.14
 \end{aligned}$$



step 7: sample = 2

step 8: if (2 > 2)  
neat

else

step 4.

$$\text{step 4: } \frac{\partial E}{\partial m} = - \left( 3.8 - (1.3)(0.4) - 0.14 \right)$$

$$= - \left( 3.8 - 0.52 - 0.14 \right)$$

$$= - (3.14)(0.4)$$

$$= - 1.25$$

$$\frac{\partial E}{\partial c} = - \left( 3.8 - (1.3)(0.4) - 0.14 \right)$$

$$= - (3.14)$$

step 5:

$$\Delta m = - (0.1)(-1.25)$$

$$= + 0.125$$

$$\Delta c = - (0.1)(-3.14)$$

$$= + 0.314$$



Step 6,

$$m = 1.3 + 0.125$$

$$m = 1.425$$

$$c = 0.14 + 0.314$$

$$c = 0.454$$

Step 7,

$$\text{sample} = 3$$

Step 8 :

$$\text{if } (3 > 2)$$

next

Step 9,

$$it = 2 + 1 = 3$$

next

$$m = 1.425$$

$$c = 0.454,$$