

Find global minimum point and value for function:  $f(x) = x^4 + 3x^2 + 10$ .

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step 1: Initialize variables

$$x = 1, \eta = 0.1, \text{epochs} = 2$$

$$\text{step 2: } \left( \frac{\partial f}{\partial x} \right)_{x=1} = (4x^3 + 6x)_1 = 4(1) + 6(1) = 10.$$

step 3: calculate change in  $x$

$$\Delta x = -\eta \frac{\partial f}{\partial x}$$

$$= - (0.1)(10)$$

$$\Delta x = -1$$

$$\text{step 4: } x = x + \Delta x$$

$$= 1 + (-1)$$

$$x = 0$$

step 5:  $itr = itr + 1$

step 6: if ( $itr > \text{epochs}$ ) then

go to step 7

else, go to step 2

$$itr = 2, \text{epochs} = 2$$



272  $\rightarrow$  false

hence, go to step 2

step 2: calculate first order derivative of  $f(x)$  at  $x=0$ .

$$\left(\frac{\partial f}{\partial x}\right)_{x=0} = (4x^3 + 6x)_0 = 0$$

step 3: calculate change in  $x$

$$\Delta x = -\eta \frac{\partial f}{\partial x}$$

$$= -(0.1)0 = 0$$

step 4:  $x = x + \Delta x$   
 $= 0 + 0 = 0$

step 5:  $itr = itr + 1$

step 6: if( $itr > epochs$ ) go to step 7

else go to step 2

here,  $itr = 3$ ,  $epochs = 2$

3 > 2, True

go to step 7



Step 7: print variable  $x \Rightarrow x=0$ .

at  $x=0$  we find minimum value of function  $f(x)$  that minimum value =  $f(0) = 10$ .