

## Assignment-2

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a) Find global minimum point and value for function  $f(x,y) = x^2 + y^2 + 10$ .

So) Manual Calculations:

Step-1:  $x = -1, y = +1, \eta = 0.1, \text{epochs} = 2$

Step-2: iter = 1

Step-3:  $\frac{\partial f}{\partial x} = 2x = -2$

$$\frac{\partial f}{\partial y} = 2y = 2$$

Step-4:  $\Delta x = -\eta \frac{\partial f}{\partial x} = -0.1(-2) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -0.1(2) = -0.2$$

Step-5:  $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

Step-6: iter = iter + 1 = 1 + 1 = 2

Step-7: if (1 > 2)  
goto step 8

else  
goto step 3

Step-3:  $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

Step-4:  $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-1.6) = 0.16$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(1.6) = -0.16$$

Step-5:  $x = x + \Delta x = -0.8 + 0.16 = -0.64$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

Step-6:  $\text{itr} = \text{itr} + 1 = 2 + 1 = 3$

Step-7: if  $(3 > 2)$   
goto step 8

Step-8:  $x = -0.64$   
 $y = 0.64$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$= 0.4 + 0.4 + 10$$

$$= 10.8$$