

let us consider a sample dataset have one input ( $x_i^0$ ) and one output ( $y_i^0$ ) and number of samples  $n$ . develop a simple linear regression model using BGD.

sample $i$	$x_i^0$	$y_i^0$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

step 1:  $[x, y]$ ,  $m = 1$ ,  $c = -1$ ,  $\eta = 0.1$ , epochs = 2,  $ns = 2$

step 2:  $itr = 1$

$$\begin{aligned} \text{step 3: } \frac{\partial E}{\partial m} &= \frac{-1}{ns} \sum_{i=1}^{ns} (y_i - mx_i - c) x_i \\ &= \frac{-1}{2} [(3.4 - (1)(0.2) + 1) 0.2 + (3.8 - (1)(0.4) + 1) 0.4] \\ &= -1.34 \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial c} &= \frac{-1}{2} [(3.4 - 0.2 + 1) + (3.8 - 0.4 + 1)] \\ &= -4.3 \end{aligned}$$

$$\begin{aligned} \text{step 4: } \Delta m &= -\eta \frac{\partial E}{\partial m} \\ &= -0.1 \times -1.34 \\ &= 0.134 \\ \Delta c &= \eta \frac{\partial E}{\partial c} \\ &= -0.1 \times -4.3 = 0.43 \end{aligned}$$

step 5:  $m + \Delta m$

$$1 + 0.134$$

$$= 1.134$$

$$c + \Delta c$$

$$= -0.1 + 4.3$$

$$= 4.2$$

$$\text{Step 6: } \text{itr} + 1$$

$$1 + 1 = 2$$

Step 7: if (itr > epochs)

goto step 8

$$2 > 3$$

else

goto step 3

$$\text{Step 3: } \frac{\partial E}{\partial m} = \frac{-1}{2} \left[ (3.4 - (1.134)(0.2) + (0.57)(0.2) + 3.8 - (1.134)(0.4) + 0.57)(0.4) \right]$$

$$= -1.157$$

$$\frac{\partial E}{\partial c} = \frac{-1}{2} \left[ (3.4 - (1.134)(0.2) + 0.57) + (3.8 - (1.134)(0.4) + 0.57) \right]$$

$$= -3.829$$

$$\text{Step 4: } \Delta m = 0.1 \times -1.157 = 0.1157$$

$$\Delta c = -0.1 \times 3.829 = 0.3829$$

$$\text{Step 5: } m + \Delta m$$

$$= 1.134 + 0.1157$$

$$= 1.2497$$

$$c + \Delta c$$

$$= 2.057 + 0.3829 = -0.187$$

$$\text{Step 6: } \text{itr} + 1$$

$$2 + 1 = 3$$

Step 7: if (itr > epochs)

3 > 2 goto step-8

else

goto step -3

$$\text{Step 8: } m = 1.2497, c = -0.187$$