

let us consider a sample dataset have one input (x_i^a) and one output (y_i^a) and number of samples 4. develop a simple linear regression model using stochastic gradient descent optimizer

sample(i)	x_i^a	y_i^a
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

- Do manual calculations for two iterations with first two samples.
- write the program python code to build simple linear regression model using SGD optimizer consider all 4 samples.

Step 1: $x, y, m=1, c=-1, \eta=0.1, \text{epochs}=2, \text{hs}=2$

Step 2: $\text{itr}=1$

Step 3: $\text{sample}=1$

$$\text{step 4: } \frac{dE}{dm} = -(84(1))(0.2) - (-1)(0.2) \\ = -0.84$$

$$\text{step 5: } \Delta m = -(0.1)(-0.84) = 0.084$$

$$\Delta c = -(0.1)(-4.2)$$

$$= 0.42$$

$$\text{step 6: } m = m + \Delta m$$

$$= 1 + 0.084 = 1.084$$

$$c = c + \Delta c$$

$$= -1 + 0.42 = -0.58$$

Step 7: $\text{sample} += 1$

$$\text{itr} += 1$$

Step 8: if ($\text{sample} > \text{hs}$)

$$2 > 2$$

goto step-9

else

goto step-4

$$\text{Step 4: } \frac{\partial F}{\partial m} = -(3.8 - (1.084)(0.4) + 0.54)0.4$$

$$= 1.5785$$

$$\frac{\partial F}{\partial c} = -(3.8 - (1.084)(0.4) + 0.58)$$

$$= -3.9464$$

$$\text{Step 5: } \Delta m = -(0.1)(-1.5785) = 0.1578$$

$$\Delta c = -(0.1)(-3.9464) = 0.3946$$

Step 7: sample $t+1$

$$2+1=3$$

$$\text{Step 8: } m = m + \Delta m = 1.084 + 0.1578$$

$$= 1.2418$$

$$c = c + \Delta c = 0.584 + 0.3946$$

$$= 0.9786$$

Step-8: if (sample > ns)

$$3 > 2$$

goto step-9

else

goto step-4

Step 9: itr $+$ 1

$$1+1=2$$

Step 10: if (itr > epochs)

$$2 > 2$$

goto step-11

else

goto step-3

Step-3: sample = 1

$$\text{Step-4: } \frac{\partial F}{\partial m} = -(3.4 - (1.2)(0.2) + 0.18)0.2$$

$$= -(3.34)(0.2)$$

$$= -0.668$$

$$\frac{\partial F}{\partial c} = -(3.4 - (1.2)(0.2) + 0.18)$$

$$= -3.34$$

$$\text{Step 5: } \Delta m = -(0.1)(-0.668)$$

$$= 0.0668$$

$$\text{Step 6: } m = m + \Delta m = 1.24 + 0.0668 = 1.3$$

$$c = c + \Delta c = 0.18 + 0.33 = 0.51$$

Step-7: sample $t=1$

$$t+1=2$$

Step 8: if (sample $> n_s$)

$$2 > 2$$

goto step-9

else

goto step-4

$$\begin{aligned}\text{Step 4: } \frac{\partial E}{\partial m} &= -(3.8 - (1.3)(0.4) - 0.15)0.4 \\ &= -1.25\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} &= -(3.8 - (1.3)(0.4) - 0.15) \\ &= -3.13\end{aligned}$$

$$\text{Step 5: } \Delta m = -(0.1)(-1.25) = 0.12$$

$$\Delta c = -(0.1)(-3.13) = 0.31$$

$$\text{Step 6: } m \leftarrow m + \Delta m = 1.3 + 0.12 = 1.42$$

$$c \leftarrow c + \Delta c = 0.15 + 0.31 = 0.46$$

Step 7: sample = sample $+1$

$$2+1=3$$

Step 8: if (sample $> n_s$)

$$3 > 2$$

goto step-9

else

go to step-4

Step-9: itr = itr $+1$

$$= 2+1=3$$

Step-10: if (itr $> \text{epochs}$)

$$3 > 2$$

goto step 11

else

goto step-3

Step-11: print m & c

$$m = 1.42, c = 0.46$$