

Assignment 3

18K41A05E4

let us consider a sample dataset have one input (x_i^a) and one output (y_i^a) and number of samples 4.

Develop a simple linear regression model using

stochastic gradient descent optimizer

Sample (i)	x_i^a	y_i^a
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

⇒ Do manual calculations for 2 iterations, 2 samples

Step 1 : $x, y, m=1, c=-1, \eta=0.1, \text{epochs}=2, ns=2$

Step 2 : $iter=1$

Step 3 : $sample=1$

Step 4 :
$$\frac{\partial E}{\partial m} = -(3.4 - (1)(0.2) - (-1)) 0.2$$
$$= -0.84$$

$$\frac{\partial E}{\partial c} = -(3.4 - (1)(0.2) + 1)$$
$$= -4.2$$

step 5 : $\Delta m = -(0.1) (-0.94)$

$$= 0.094$$

$$\Delta C = -0.1 (-4.2)$$

$$= 0.42$$

step 6 : $m = m + \Delta m = 1 + 0.094 = 1.094$

$$C = C + \Delta C = -1 + 0.42 = -0.58$$

step 7 : $\text{sample} = \text{sample} + 1$

$$= 1 + 1 = 2$$

step 8 : $\text{if } (\text{sample} > n_s)$
 goto step 9

else
 goto step 4

step 4 : $\frac{\partial E}{\partial m} = -(3.8 - (1.094)(0.4) + 0.58) 0.4$
 $= -1.5785$

$$\frac{\partial E}{\partial C} = -(3.8 - (1.094)(0.4) + 0.58)$$

$$= -3.9464$$

Step 5: $\Delta m = -10.1) (-1.5785) = 0.1578$

$\Delta C = -(0.1) (-3.9464) = 0.3946$

Step 6: $m = m + \Delta m = 1.084 + 0.1578 = 1.2418$

$C = C + \Delta C = -0.58 + 0.3946 = -0.1854$

Step 7: $Sample = Sample + 1$

$= 2 + 1$

$= 3$

Step 8 :- $if (sample > ns)$
 $3 > 2$

goto step 9

else

goto step 4.

Step 9 :- $iter = iter + 1$

$= 1 + 1 = 2$

Step 10 : $if (iter > epochs)$
 $2 > 21$

goto step 11

else

goto step 3

Step 3 : $Sample = 1$

step 4 : $\frac{\partial E}{\partial m} = -(3.4 - (1.2)(0.2) + 0.18) 0.2$

$$= -(3.4)$$

$$= -(3.4 - 0.24 + 0.18) 0.2$$

$$= -(3.34) 0.2$$

$$= -0.668$$

$$\frac{\partial E}{\partial c} = -(3.4 - (1.2)(0.2) + 0.18)$$

$$= -3.34$$

step 5 : $\Delta m = -(0.1)(-0.668)$

$$= 0.066$$

$$\Delta c = -(0.1)(-3.34)$$

$$= 0.33$$

step 6 : $m = m + \Delta m = 1.24 + 0.066 = 1.3$

$$c = c + \Delta c = -0.18 + 0.33 = 0.15$$

step 7 : $\text{sample} = \text{sample} + 1$

$$= 1 + 1 = 2$$

step 8 : if $\begin{matrix} \text{sample} > n \\ 2 > 2 \end{matrix}$

goto step 9

else

goto step 4

Step 4 :- $\frac{\partial E}{\partial M} = -(3.8 - (1.3)(0.4) - 0.15) \cdot 0.4$

$$= -(3.8 - 0.52 - 0.15) \cdot 0.4$$

$$= -1.25$$

$$\frac{\partial E}{\partial C} = -(3.8 - (1.3)(0.4) - 0.15)$$

$$= -3.13$$

Step 5 :- $\Delta m = \text{old} - (0.1)(-1.25)$

$$= 0.12$$

$$\Delta C = - (0.1)(-3.13)$$

$$= 0.31$$

Step 6 :- $m = m + \Delta m = 1.3 + 0.12 = 1.42$

$$C = C + \Delta C = 0.15 + 0.31 = 0.46$$

Step 7 :- $\text{sample} = \text{sample} + 1$

$$= 2 + 1 = 3$$

Step 8 if (sample > ns)

$$3 > 2$$

goto step 9

else

step 4

step 9: $iku = iku + 1$
 $= 2 + 1$
 $= 3$

step 10: if ($iku > epochs$)
 $3 > 2$
goto step 11
else
goto step 3

step 11: print m & C
 $m = 1.42$ $C = 0.46$