

First Missing Positive Integer

Ex:-

arr[5] → 3 -2 1 2 7 ans = 4

arr[7] → -8 2 6 4 -7 1 3 ans = 5

arr[6] → 2 1 6 4 3 5 ans = 7

arr[5] → -4 8 3 -1 0 ans = 1

//idea-1

Sort the array & traverse upto last element

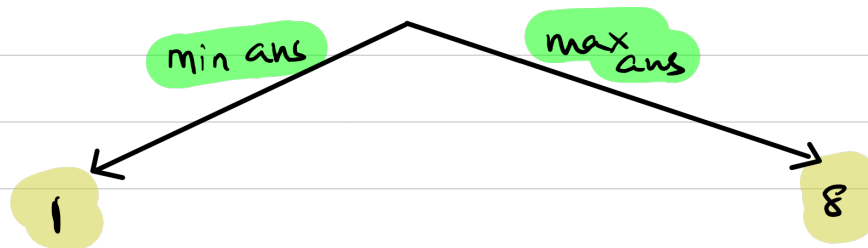
$$T.C : O(n \log n) + O(n) \approx O(n \log n)$$

//idea 2

if numbers are assigned properly

Observation - 1

arr[7]: $\frac{1}{0} \quad \frac{2}{1} \quad \frac{3}{2} \quad \frac{4}{3} \quad \frac{5}{4} \quad \frac{6}{5} \quad \frac{7}{6}$

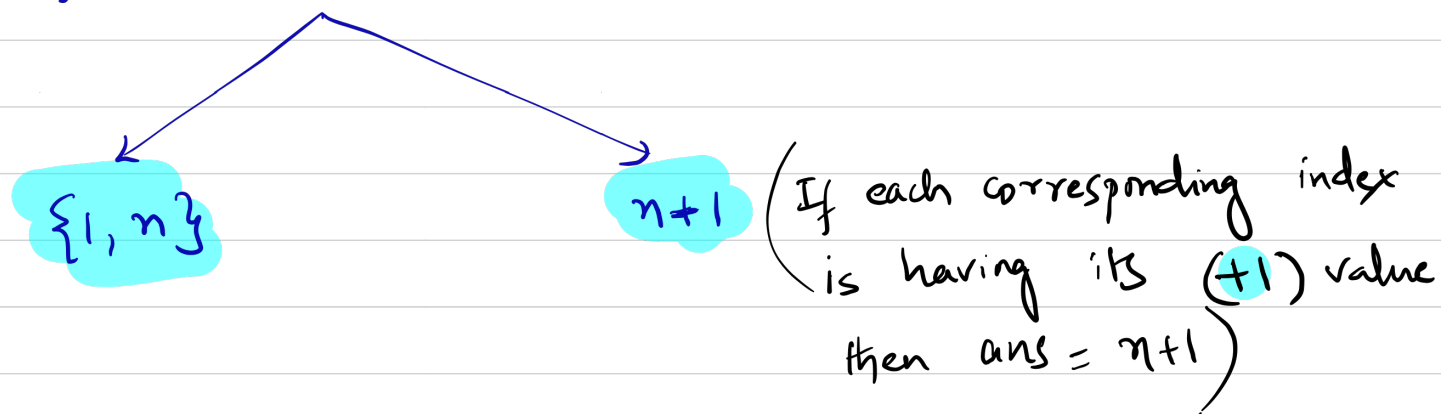


So, for array size = 7 \Rightarrow Range = (1, 8)

In general

Size = $n \Rightarrow$ Range = (1, $n+1$)

Answer could be from (1 \rightarrow $n+1$)



arr[8] :

⁰ <u>1</u>	¹ <u>2</u>	² <u>3</u>	³ <u>4</u>	⁴ <u>5</u>	⁵ <u>6</u>	⁶ <u>7</u>	⁷ <u>8</u>
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 } Each corresponding index has its value as (index + 1)

Our main moto is to convert given array into above pattern , from that we can easily get the first missing value by $O(n)$

So, how to do that Mapping? \Rightarrow By "Swapping"

arr[8] :

⁰ 4	¹ 2	² -7	³ 6	⁴ 9	⁵ 1	⁶ -8	⁷ 3
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Assumption[]:

1	2	3	4	5	6	7	8
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arr[0] = 4 \longrightarrow index = 3 , swap(0, 3)

If we observe arr, arr[0] = 4 (According to our assumption value 4 need to be index = 3)
So swap Current idx with 3

Writing every iteration in-detail \downarrow

$\text{arr}[0] = 4 \implies \text{Actual Index} = 3, \text{Swap}(0, 3)$

$\text{arr}[0] = 6 \implies \text{Actual Index} = 5, \text{Swap}(0, 5)$

$\text{arr}[0] = 1 \implies \text{Actual Index} = 0, \text{increment } i$

$\text{arr}[1] = 2 \implies \text{Actual Index} = 1, \text{increment } i$

$\text{arr}[2] = -7 \implies \text{Irrelevant}, \text{increment } i$

$\text{arr}[3] = 4 \implies \text{Actual Index} = 3, \text{increment } i$

$\text{arr}[4] = 9 \implies \text{Irrelevant}, \text{increment } i$

$\text{arr}[7] = 3 \implies \text{Actual Index} = 2, \text{Swap}(7, 2)$

Note:

If Swapping values are same \implies increment i ← just $i++$

for example:

$\text{arr}[5] = \{4, 1, 8, 2, 2\}$

$\begin{matrix} & & 3 & & 4 \\ & \swarrow & & \searrow & \\ 3 & & & & \end{matrix}$

Here if we swap $(\text{arr}[0], \text{arr}[2])$

No use

```

1 class Solution {
2     public int firstMissingPositive(int[] nums) {
3         int n = nums.length;
4
5         int i = 0;
6         while(i < n){
7             if(nums[i] < 1 || nums[i] > n || nums[i] == i+1){
8                 i++;
9             }
10            else{
11                int idx = nums[i]-1;
12                if(nums[i] == nums[idx]) i++;
13            }
14            else{
15                int temp = nums[i];
16                nums[i] = nums[idx];
17                nums[idx] = temp;
18            }
19        }
20    }
21    for(i = 0; i < n; i++){
22        if(nums[i] != i+1) return i+1;
23    }
24    return n+1;
25 }
26 }

```

case irrelevant
Already Solved
if Swapping values are same case