

Max Chunks to make an array Sorted-1

Given an arr[N], containing permutation of the integers in the range $[0, n-1]$. you have to split the array into maximum possible no. of chunks, such that after individual sorting of those chunks, the whole array gets sorted.

Ex:- $\{ \overset{0}{1}, \overset{1}{0}, \overset{2}{2}, \overset{3}{2}, \overset{4}{4} \}$

The key understanding here is, if we sort the elements \Rightarrow the obtained answer will be our indexes,

Ex:- $\{ \overset{0}{1}, \overset{1}{0}, \overset{2}{2}, \overset{3}{2}, \overset{4}{4} \} \xrightarrow{\text{Sort}} \{0, 1, 2, 3, 4\}$

\hookrightarrow These are our indexes only

So, the question array will be a permutation of indexes only, it won't go beyond range of indexes.

Ex 2: $\{ \overset{0}{2}, \overset{1}{0}, \overset{2}{1}, \overset{3}{4}, \overset{4}{3}, \overset{5}{6}, \overset{6}{7}, \overset{7}{5}, \overset{8}{8} \} \xrightarrow{\text{Sort}} \{0, 1, 2, 3, 4, 5, 6, 7, 8\}$

\hookrightarrow indexes only

So, what are chunks here?

"partitions"

$\text{arr}[5] : \{ 1, 0 \mid 2 \mid 3 \mid 4 \}$ \Rightarrow if we split the array into 4 parts and sorting each part individually the whole array will be sorted

sorting individual chunk \Downarrow

$\{ 0 \mid 1 \mid 2 \mid 3 \mid 4 \}$ \Rightarrow So, the ans = 4 chunks

But, we can split as: $\{ 0 \mid 1 \mid 2 \mid 3 \mid 4 \}$ as well, like 2 chunks, this will also give us valid result of sorted array,

But, we need to split the array as Maximum Possible Chunks

arr[9] : { 2, 0, 1 | 4, 3 | 6, 7, 5 | 8 }

⇓ Sort individually

{ 1, 0, 2 | 3, 4 | 5, 6, 7 | 8 } → whole array is sorted

So, ans = 4 chunks

How

arr[9] : { 2, 0, 1, 4, 3, 6, 7, 5, 8 }

0 1 2 3 4 5 6 7 8

Steps

① if you want to make chunk, look for maximum index of the chunk

arr[9] : { 2, 0, 1 | 4, 3 | 6, 7, 5 | 8 }

0 1 2 3 4 5 6 7 8

i	arr[i]	max Value
0	2	-∞ 2
1	0	2
2	1	2 → in this case index & Max value are equal, so make a chunk here
3	4	2 4
4	3	4 → make a chunk again
5	6	4 6
6	7	6 7
7	5	7 → make a chunk again
8	8	7 8 → make a chunk again

So, simply if you look for (max value & Index position) You can make chunks

Note:- if already a number positioned in its perfect index, Chunk + 1