

Three Sum

15. 3Sum

Solved

Medium Topics Companies Hint

Given an integer array `nums`, return all the triplets `[nums[i], nums[j], nums[k]]` such that `i != j`, `i != k`, and `j != k`, and `nums[i] + nums[j] + nums[k] == 0`.

Notice that the solution set must not contain duplicate triplets.

Example 1:

Input: `nums = [-1,0,1,2,-1,-4]`

Output: `[[-1,-1,2], [-1,0,1]]`

Explanation:

`nums[0] + nums[1] + nums[2] = (-1) + 0 + 1 = 0.`

`nums[1] + nums[2] + nums[4] = 0 + 1 + (-1) = 0.`

`nums[0] + nums[3] + nums[4] = (-1) + 2 + (-1) = 0.`

The distinct triplets are `[-1,0,1]` and `[-1,-1,2]`.

Notice that the order of the output and the order of the triplets does not matter.

Example 2:

Input: `nums = [0,1,1]`

Output: `[]`

Explanation: The only possible triplet does not sum up to 0.

Example 3:

Input: `nums = [0,0,0]`

Output: `[[0,0,0]]`

Explanation: The only possible triplet sums up to 0.

problem Statement-

* if we add 3 different indices values, that will equal 0

* if that happens, store such index values triplet and return all triplets

* No Duplicates are allowed

Suppose:-

`{-1, 0, 1, 2, 2, -1, 4}`

`ans1 = {-1, 0, 1, 2, 2, -1, 4}`

`ans2 = {-1, 0, 1, 2, 2, -1, 4}`

Both results in zero, But both triplets are same, So don't allow duplicates

For that to happen, Sort the elements and skip duplicates

And if we have a sorted array, and we are looking for a certain condition on index values,
we can use two pointers technique

→ $nums[i] + nums[j] + nums[k] == 0$

$$nums[i] = \{-1, 0, 1, 2, -1, 4\}$$

↓ sort

$$\{-1, -1, 0, 1, 2, 4\}$$

placing pointers

Initially :

$$\{-1, -1, 0, 1, 2, 4\}$$

↑ ↑ ↑
i j k

* We start with i , which traverse from $0 \rightarrow n-1$

* for every i , initialize 2 pointers (j, k)

j at $i+1$, k at $n-1$
(from front) (from Back)

* And apply 2 sum ideology b/w (j, k) pointers

for every (j, k) look up for $nums[i] + nums[j] + nums[k] == 0$?

* if $(sum < 0)$ \rightarrow As array is sorted, we have to increase sum value, increment j

* if $(sum > 0)$ \rightarrow As array is sorted, we have to decrease sum value, decrement k

* if $(sum == 0)$ \rightarrow Triplet found with, add it to ans & move (j, k)

$\{-1, -1, 0, 1, 2, 4\}$
 $i \quad j \quad k$

	<u>i</u>	<u>j</u>	<u>k</u>	<u>Sum</u>	<u>Operation</u>
$\{-1, -1, 0, 1, 2, 4\}$ $i \quad j \quad k$	0	1	5	$-1 - 1 + 4 = 2$	$2 > 0$ (k--)
$\{-1, -1, 0, 1, 2, 4\}$ $i \quad j \quad k$	0	1	4	$-1 - 1 + 2 = 0$	add this triplet
$\{-1, -1, 0, 1, 2, 4\}$ $i \quad j \quad k$	// skip all $k=2$'s & skip all $j=-1$'s				
	0	2	3	$-1 + 0 + 1 = 0$	add this triplet
	// skip all $k=1$'s & skip all $j=0$'s				

Because, with $i=0$,
 you can't form
 any other triplets
 with same values of $(i, k) \rightarrow$ So
 increment j ,
 decrement k } till we get new values
 if $(k \ \& \ j)$ crosses \rightarrow increment &
 do the same
 process again

* Above steps are for triplets which includes $i=0$

* Do same steps for $i \in 1, 2, 3, \dots, n$

* Then our ans will consists of every possible triplet.

Time Complexity

① Sorting the array $\rightarrow O(n \log n)$

② nearly $O(n^2)$ to traverse and check all triplets

$$\therefore \approx \underline{\underline{O(n^2)}}$$