## Reading Quiz #2

1 This is a preview of the published version of the quiz

Started: Feb 1 at 11:42am

## **Quiz Instructions**

To prepare for this quiz, please read sections 5.1 to 5.3 (inclusive) in the Kleinberg + Tardos textbook.

The goal of this quiz is to lightly assess a first quick reading of these resources to prepare for class. You should definitely return to this material for a more thorough read to solidify your learning and prepare for assignments and exams.

Note that you are limited to only *3 attempts* on this quiz.

Best of luck! :-)

| Question 1 | 1 pts |
|------------|-------|
|            |       |

What is the tightest bound for a function T with the following recursion formula:

$$T\left(n
ight) \,=\, T\left(rac{n}{4}
ight) \,+\, T\left(rac{3n}{4}
ight) \,+\, cn$$
  $T\left(1
ight) \,=\, 1$ 

|     | $\sim 1$ | ٠. ١ |
|-----|----------|------|
| ( ) | ( )(     | n    |

$$\bigcirc$$
 O(n^(3/2))

## Question 2 1 pts

Is this approach for showing merge-sort is O(n logn) correct? (Think about why or why not)

By guessing T(n) is O(n logn) we have for  $n>N_0$ :

$$T\left(n
ight) \,=\, 2T\left(rac{n}{2}
ight) \,+\, cn \,\leq\, 2k\left(rac{n}{2}
ight)\log\left(rac{n}{2}
ight) + cn$$
 ,

so:

$$\leq 2k\left(rac{n}{2}
ight)\log\left(rac{n}{2}
ight) + cn\,\log\left(rac{n}{2}
ight) \ = \ (k+c)\,n\,\log\left(rac{n}{2}
ight) \ \leq (k+c)\,n\,\log(n)$$

and now we take  $\mathbf{k} + \mathbf{c}$  to be our constant and we're done.

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(You can assume that the base-case of T(1) is handled correctly, and to simplify things, n is always a power of 2, so that  $\lfloor \frac{n}{2} \rfloor = \frac{n}{2} = \lceil \frac{n}{2} \rceil$  everywhere)

- Yes, this approach is correct.
- No, this approach is not correct.

## Question 3 1 pts

What are the tightest bounds for the functions  $T_1$  and  $T_2$  (respectively from left to right) such that:

$$T_1\left(n
ight) \,=\, T_1\left(rac{3n}{4}
ight) \,+\, cn$$

$$T_2(n) = T_2(n-4) + cn$$

- O(n), O(n^2)
- O(n), O(n)
- O(n logn), O(n logn)

| Question 4   | 1 pts                      |
|--|----------------------------|
| Can the merging step in "Counting Inversions" problem with n done in $O(n)$ time? Why?   | integers, be               |
| $\circ$ No. When merging, we should sort all the values form the first a of elements. This takes time $O(nlogn)$ .   | and second half            |
| O No. When merging, we should first find the minimum of the small in the first half of elements and second half of elements. Then we compare this value with all the elements in the opposite set. (If the first half, it should be compared to all the values in the second takes time $O(n^2)$ . | we should<br>minimum is in |
| Yes. When merging, we compare the smallest value of first half<br>with the smallest value of the second half of elements and, add<br>of these two to the output and erase if from its list. This takes to  | I the minimum              |
| Yes. When merging, we add the values of first half of elements first. Then we add the values of second half of elements. This to $O(n)$ .  | ·                          |

O(n), O(n logn)

Not saved

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