

Date: April 12 2021

Write a program that implements the following subroutines and hence the task below:

(a) $\text{min-heapify}(A[], n, i)$

//a recursive procedure takes an array of n elements (indexed $1 \dots n$) and an index $i < n$ as input and performs at most $\text{depth}(i)$ swaps (where $\text{depth}(i)$ is the number of edges in the path from node i to the farthest leaf in the subtree rooted at i) to convert the subtree rooted at i to a min-heap. Further, $\text{min-heapify}()$ assumes both the left and right subtrees of i to be min-heaps.

(b) $\text{build-heap}(A[], n)$

//a procedure that converts an arbitrary input array to a min-heap (bottom-up) using the above procedure $\text{min-heapify}()$ as a subroutine in $O(n)$ time.

(c) $\text{sort}(A[], n)$

//sorts the numbers in descending order using the above $\text{min-heap}()$ procedure.

```
sort(A[], n)
    build-heap(A[], n)
    for(i ← 1 to n-1)
        swap(A[1], A[n+1-i])
        min-heapify(A[], n-i, 1)
```

(d) $\text{printFirst-k-Smallest}(A[], n, k)$

//Prints the first k smallest elements in the list in $O(k \log n)$ time provided the array $A[1 \dots n]$ is a min-heap.

```
printFirst-k-Smallest(A[], n, k)
    for(i ← 1 to k)
        Print A[1]
        swap(A[1], A[n+1-i])
        min-heapify(A[], n-i, 1)
```

As we had before, you are being provided with two files `testCaseSize.txt` and `searchTestCase.txt` containing 18 test cases. Your program should read each of those test cases, convert each to a min-heap using your $\text{build-heap}()$ procedure and write the resultant heaps to a file `heapLists.txt`. In the meantime, compute the number of pairwise swaps performed by your $\text{build-heap}()$ procedure and print the same as output (your program would output 18 values).

Further, use your `sort()` procedure to sort each of those test cases and write the resultant lists to a file *sortedLists.txt*.

To end with, use your `printFirst-k-Smallest()` procedure to print the k smallest elements in each of those lists, where $k = n \% 100 + r$ for n being the size of the list, and r being your roll number (the integer composed of last 3 digits). Your procedure should read each of those heaps from the file *heapLists.txt* to begin with, so as to have the input being a `min-heap()`, thereby satisfying the constraint associated with the function `printFirst-k-Smallest(A[], n, k)`.