

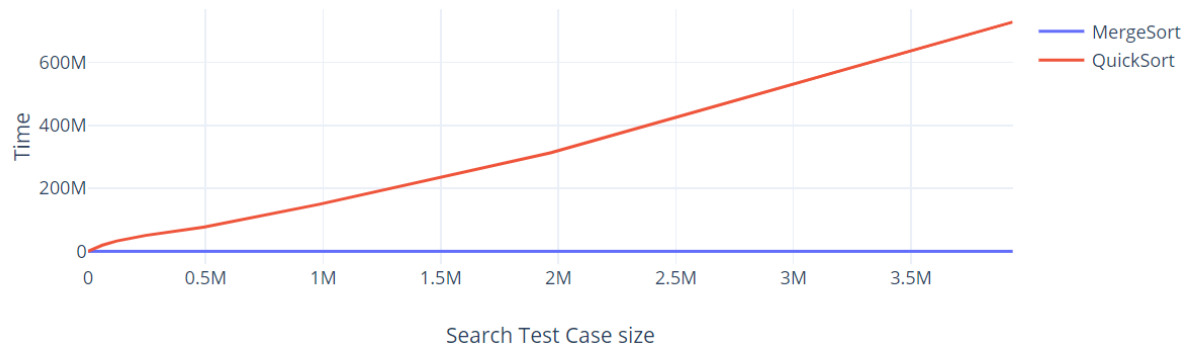
Lab 7

Ex 1:

Function	Big O
<pre>void swap (int *a, int *b) { int temp=*a; *a=*b; *b=temp; }</pre>	O(1)[declaration and assignment]
<pre>int partition(int array[], int low, int high) { int pivot= array[high]; int i=(low-1); for(int j=low; j<=high-1; j++) { if(array[j]<pivot) { i++; swap(&array[i],&array[j]); } } swap(&array[i+1], &array[high]); return (i+1); }</pre>	
<pre>void quicksort(int array[], int low, int high) { if (low<high) { int x= partition(array, low, high); quicksort(array, low, x-1); quicksort(array, x+1, high); } }</pre>	$ \begin{array}{cc} & n \\ / & \backslash \\ 0 & n-1 \\ & / \backslash \\ & 0 \quad n-2 \end{array} $ <p> $cn + c(n-1) + c(n-2) + \dots + 2c$ $c\left(\frac{n(n+1)}{2} - 1\right)$ O(n²) </p>
<pre>void merge(int array[], int l, int m, int r) { int i, j, k; int n1=m-l+1; int n2=r-m; int L[n1], R[n2]; for (i = 0; i < n1; i++) L[i] = array[l + i]; for (j = 0; j < n2; j++) R[j] = array[m + 1 + j]; }</pre>	

<pre> i = 0; j = 0; k = l; while (i < n1 && j < n2) { if (L[i] <= R[j]) { array[k] = L[i]; i++; } else { array[k] = R[j]; j++; } k++; } while (i < n1) { array[k] = L[i]; i++; k++; } while (j < n2) { array[k] = R[j]; j++; k++; } } </pre>	
<pre> void mergeSort(int array[], int l, int r) { if (l < r) { int m = l + (r - l) / 2; mergeSort(array, l, m); mergeSort(array, m + 1, r); merge(array, l, m, r); } } </pre>	$T(n) = \begin{cases} b & \text{if } n = 1 \\ T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + cn & \text{otherwise} \end{cases}$ $T(n) = 2(2T(n/2^2) + cn/2) + cn$ $T(n) = 2^2T(n/2^2) + 2cn$ $T(n) = 2^kT(n/2^k) + kcn$ $n/2^k = 1 \Rightarrow k = \ln n$ $T(n) = nb + cn \cdot \ln n$ $\mathbf{O(n)=n \cdot \ln n}$

Time complexity of QuickSort and MergeSort



Ex 2:

Function	Big O
<pre> void Split(Node* source, Node** frontRef, Node** backRef) { Node* fast; Node* slow; slow = source; fast = source->next; while (fast != NULL) { fast = fast->next; if (fast != NULL) { slow = slow->next; fast = fast->next; } } *frontRef = source; *backRef = slow->next; slow->next = NULL; } </pre>	<p>While loop would continue for $n-1$ times where n is the number of elements in source node.</p> <p>Hence $O(n)$</p>
<pre> Node* SortedMerge(Node* a, Node* b) { Node* result = NULL; if (a == NULL) return (b); else if (b == NULL) return (a); if (a->data <= b->data) { result = a; result->next = SortedMerge(a- >next, b); } } </pre>	

<pre> else { result = b; result->next = SortedMerge(a, b->next); } return (result); } </pre>	<p>$O(n)$[as n comparisons]</p>
<pre> void MergeSort(Node** headRef) { Node* head = *headRef; Node* a; Node* b; if ((head == NULL) (head->next == NULL)) { return; } Split(head, &a, &b); MergeSort(&a); MergeSort(&b); *headRef = SortedMerge(a, b); } </pre>	<p>$O(n)$[discussed above]</p> <p>$O(n)$</p> <p>$O(n)$</p>
<pre> void printList(Node* node) { while (node != NULL) { cout << node->data << " "; node = node->next; } } </pre>	<p>$O(n)$[elements in node]</p>
<pre> void push(Node** head_ref, int new_data) { Node* new_node = new Node(); new_node->data = new_data; new_node->next = (*head_ref); (*head_ref) = new_node; } </pre>	<p>$O(1)$[declaration, assignment]</p>

```
Enter no of elements to be sorted: 6
Enter element: 0
Enter element: -5
Enter element: 8
Enter element: -10
Enter element: 23
Enter element: 4

UnSorted Linked List is:
4 23 -10 8 -5 0
Sorted Linked List is:
-10 -5 0 4 8 23
```