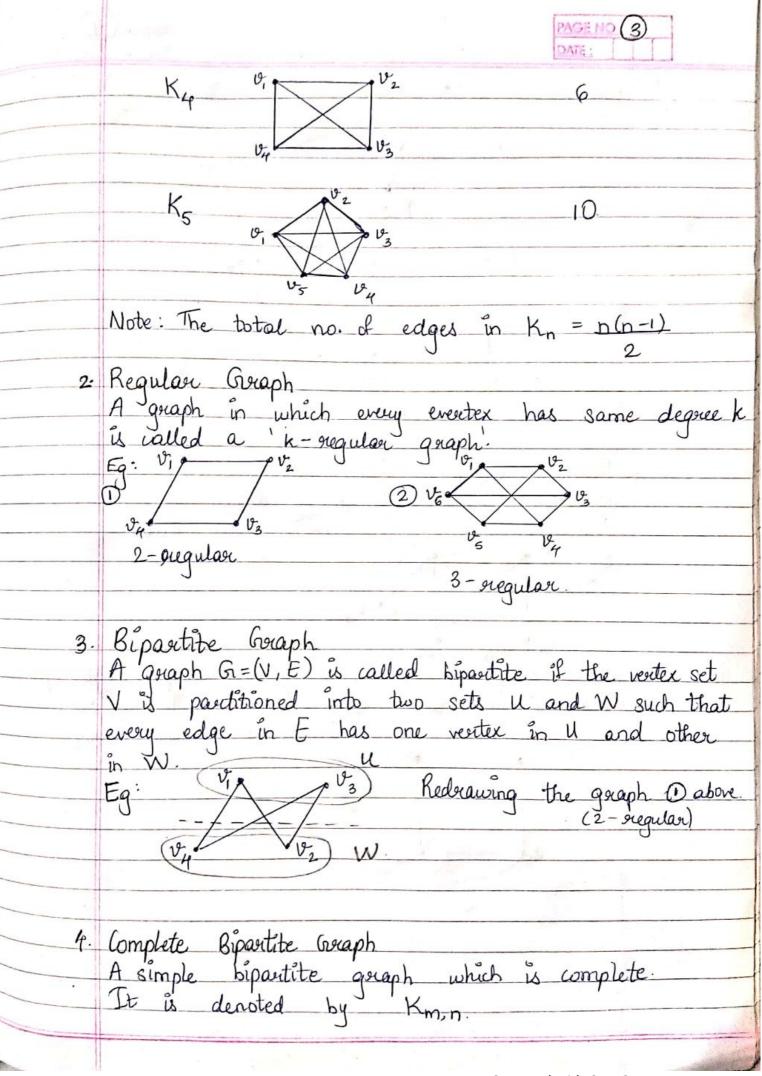
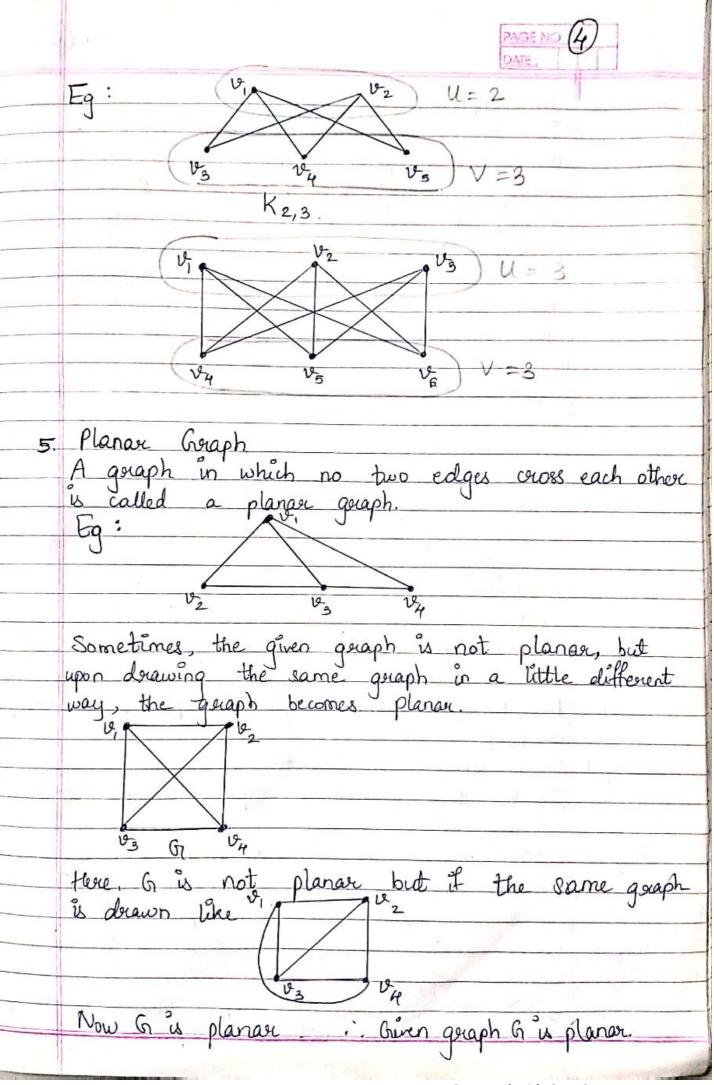


Graph Theory. · A graph is an ordered pair (V, E) where V = non-empty set of vertices. E = set of edges.

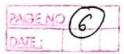
A vertex is a point I node. An edge is a curve/ line joining two vertices. A loop is an edge joining a vertex to itself fariable / Multiple edges means more than one edges joining the same eq: G= (, E) where V= {v, v2, v3, v4, v5}, E={e, e2, e3, e4}e5} Here, e, = v, v2 (edge e, joins vertices votos e2= V2 V4 e3 = e4 = v2v3. -> multiple edges. es = v,v, -> loop graph without loops and multiple edges A graph which is not simple is called multigraph. It edge e is formed by vertices to, and to then v, v, are called adjacent vertices. is common between west edges e, and ez then e, ez are called adjacent edges Eg: In above example, v, v, are adjacent restries while v, v, and not adjacent vertices. e, e, are adjacent edges but e, es are not.

	£421	
•	Degree of a vertex v is the	e number of edges
9	starting or ending at the	vertex v, wouther as d(v).
	Eq: (n aganh G of page 1.	
	d(v,) = 3 (as loop is con	inted 2 times)
1	d(02) = 4	
- N	$d(v_3) = 2$	
	d(v4) = 1 , 2, is calle	ed pendant vertex.
	$d(v_4) = 1 \cdot \cdot \cdot v_4 \text{ is called}$ $d(v_5) = 0 \cdot \cdot \cdot v_5 \text{ is called}$	ed isolated vertex.
	Handball'as Theorem:	
	The sum of degrees of all notice the number of edges	evitices in a graph is
-	twice the number of edges	in that gouph
	ve. 20(0) = 2t	-
	In graph a of page 1:	. 10. 11. 1()
	Sd(0) = d(0,) + d(0) + d(0)	$+a(v_4)+a(v_5)$
	= 3 + 4 + 2	+ + 0
I Total	E = no. of edges in G	= 6
	t = n0.04 eages in 07 $i - Zd(u) = 10 = 2 \times 5 =$	2 E.
	7:04(0)=10=223	
	Types of goraph:	
	. Complete Graph	
	A simple ascaph in which eve	by vertex is adjacent
1	A simple graph in which ever with every other reacter.	J
	ie. A simple graph on n verdices in which degree	
	of every vertex is n-1.	· U
	It is denoted by Kn.	no of the
	Eq: K, ·v,	no of edges
1.7	K ₂ v ₁ ····································	
	K ₃ V ₁ V ₂	3
	V.	



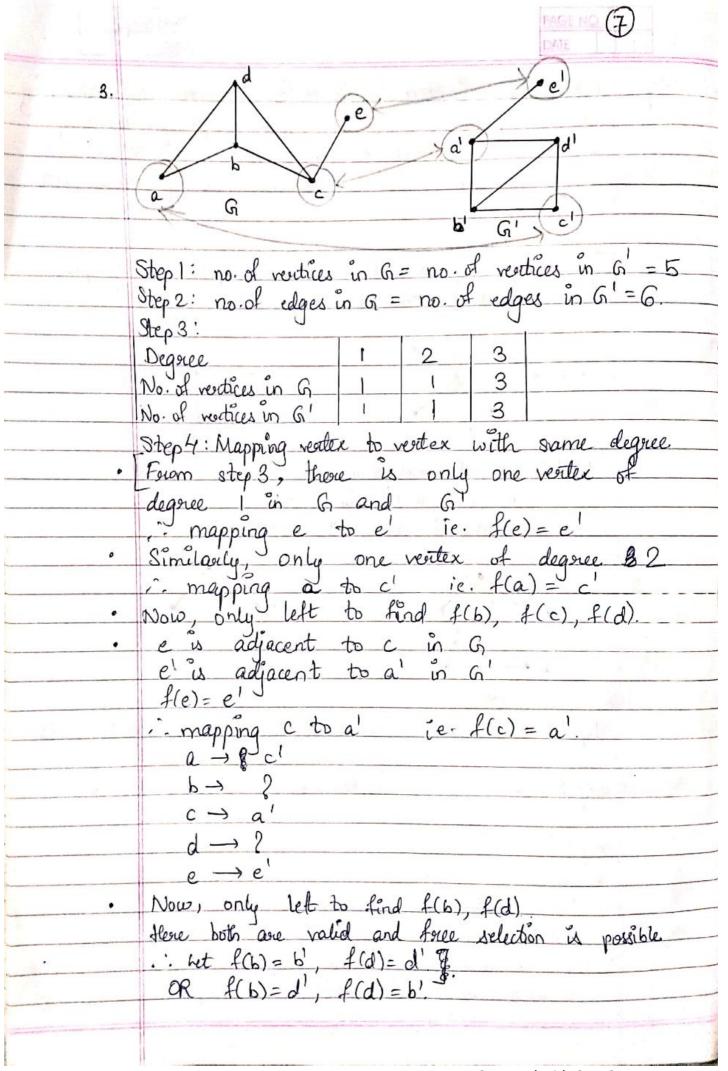


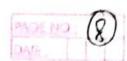
	T		
-	Isomosephism of graphs: Two graphs G = (V, E) and G'=(V', E') are said		
9	to be isomosphic if there is a one-to-one		
	osviespondence f: V -> V' such that for &v, v2 EV		
	$v'_1, v'_2 \in V'$, $f(v_1) = v'_1$, $f(v_2) = v'_2$ and v'_1 is		
	adjacent to ve then vi is adjacent to ve.		
	e. It we can find a brective function		
	four vertices to a to vertices of a s.l.		
	two vertices adjacent in a have their		
	images adjacent in Gire adjacency preserving.		
	Eg. pa		
	62 c 92 691		
1 1	Here a and b are adjacent		
	• If $f(a) = q$, $f(b) = p^{-1}$		
	then p,q. are adjacent		
	- pour per mapping - can be considered.		
	then a and a gare not adjacent		
	then q and or are not adjacent improper mapping - cannot be considered.		
Note: Tf	f(a) = b then dog a = dea h.		
	f(a) = b then cleg a = deg b. How to cheek whether given graphs are isomosphic ox not?		
	ox not?		
Step 1:	Check whether no of vertices in a = no of vertices in a!		
	If Yes then proceed to step 2, otherwise		
	G and G are not isomorphic		
Step 2:	Check whether no of edges in G = no of edges in G.		
-	If Yes then peroued to step 3, otherwise conclude		
	to and to are not isomorphic.		
Step 3:	Check whether degree of reactives in G and G are		
	Same on not.		
	If Yes then proceed to step 4, otherise conclude. 'Go and Go are not isomorphic!		
	and the somosphic.		



Stepte: Define a function $f: G \to G'$ on vertices satisfying adjacency of vertices ie adjacency priezerving map.

It finding such f is possible then G and G' are isomorphic otherwise they are not Eg: Check whether the following pair of graphs are isomorphic on not. Step 1: no. of vertices in G = 7 vertices in G = 5 ... Grand Grane not isomosphic Step 1: no. of vertices in G = no. of vertices in G'= 5 Step 2: no. of edges in G= no. of edges in G= 7. Step 3: no of vertices in G no of vertices in G!





Consider a map f: G -> G' defined by f(a) = c' f(a) = c' f(b) = b' f (b)= d' f(d) = b' f(e) = e1 f(e) = e' This is an adjacency pouseoung map.

Step1: no. of reactices in 6 = no. of reactices in 61. = 8 Step 2: no. of colges in G = no. of edges in G = 10 Step 3:

Dégoue No. of redices in G

No. of vertices in G'

Step 4: het f(d) = d to the

Now, d is (connected) to lead facent to a, e, c. of which deg a = deg c = 2, deg e = 3.

And, d' is adjacent to a', e', c' of which

deg e' = deg c' = 3, deg a' = 2 ... d cannot be mapped to d!

d cannot be mapped to e', f', c'

i - Find f: G → G' is not possible.

i G is not isomorphic to G!.

Path is an atternating sequence of vertices and edges of a graph in which neither vertex non edge is superated.

Length of path = no. of edges in the path Path TI, = v, e, v, e, v, e, v, e, v, length = 2. Path TI = v, e, v, e, v, e, v, e, v, length = 4. A path that begins and ends at the same vertex is called a circuit. It is also called a Connected graph

A graph is called connected if there is a path
between every pair of vertices in that graph. is a direct path a e3b a-d => TT: ae, ce d TT: ae, be, d.

a-e => 70; ae, c c, des e

Similarly, we can find a path the between NOTE: Hore,

oriting acd as a path is easier than wonting ae, ce, d.

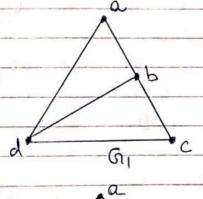
· Length of path $\pi = 2 = no \cdot of$ edges.

Ederian Graph.

A path on circuit which includes every edge of the graph is said to be an Ederian path / circuit.

If a graph has an Ederian circuit, it

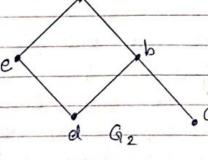
is called Eulerian goraph.



· a-b-c-d-a is a circuit but it leaves edge b-d so it is not Ellerian cruit.

-a-b-d-c-b & an Euleonan path.

· There is no possible Eulequan circuit so the given graph Gr, is not Euleonan.

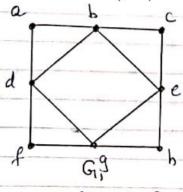


· C-b-a-e-d-b is Enlevian path

There is no possible Enlevian circuit, so graph G2
is not Enlevian.

	DATE
	a-b-d-c-€a is an
	Edeniar circuit
	be de Go de
	d Gs
-	How to check whether the given graph is Eulerian on not? Theorem:
	How to check whether the given grapes
-	Eulerian ou not?
•	Theorem:
_	A connected graph is Edwar He and only if degree of every vertex is even. Exa: In above example, there were odd
_	dequee of every vertex is even.
	Eq: In above example, there were odd
	Eg: In above example, there were odd degree vertices in G, and G2 but in G3
	at ventries had even degree
	So, only G3 is Eulerian
	Theorem:
_	A connected graph of has an Eulerian path but not on Eulerian circuit if there
	path but not on Eulerian circuit if there
	are exactly two vertices of odd degree
	i.e. If a goraph has exactly two vertices of
	odd degree - i and je then there is an
	Eulerian path between u and v.
	NOTE: As there are two odd degree to vertices,
	the graph will not have Eulerian circuit.
	Ex: In above example, G. and G. had 2
	vortices of odd degree 80 they had Eilerian path but were not Eilerian. Gy had
	Exterior outh but were not Exterior G had
	all restricts of meteren degree so it had Filerian circuit there Go has I does not have Filerian path.] Can a circuit be treated a path?
	Concret Hone Co. has I done not have Edwar north
5	Land Churt by hastal a total
5.	Juli a france be france a pain

path and lose circuit. whenever we say that the graph how Eulesian path / circuit, we need to specify that particular path / corcuit. Just mentioning it has path / circuit is not a pocopeois.



0

(2)

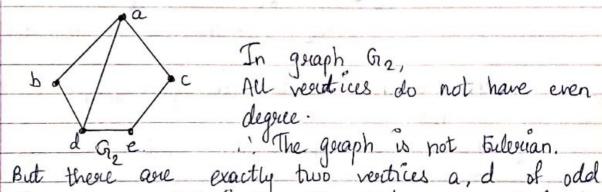
In graph Gr,,

All redices have even degree

e ... The graph is Enlevian.

Tt; a-b-c-e-h-g-f-d-g-e-b-

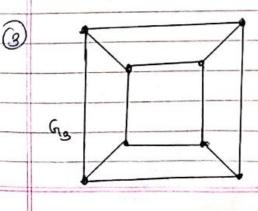
is an bilouan coicuit. Every concruit is a path. II, is an Euleonan path.



To graph Giz,

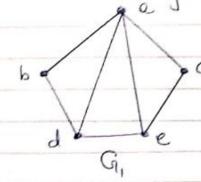
All residices do not have even dequee.

degree so an Eilerian path between a and d exists. Tto: a-b-d-a-c-e-d. NOTE: There is no Edeman path between any other pair of vertices.



In Greaph Gz, All resitives have odd degree i. The gouph does not have an Eulerian path with non Bulerian cucuit. Hamiltonian Crocaph.

A path on which includes every 'voitex' of the graph is said to be an Hamiltonian path on which includes. a graph has an Hamiltonian circuit, it is called Hamiltonian graph.



In graph G1,

c π=a-b-d-e-c-a is

a Hamiltonian circuit

Hence, G1, is Hamiltonian.

To Goraph Giz,

The a-b-d-c is

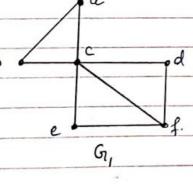
How to check whether the given graph is tamiltonian on not?
Checking for tlamiltonian is not as easy as checking for Eulerian.

Finding trong connected graph.
Finding flamiltonian path / circuit is not difficult.
When concluding that the graph is not tlamiltonian, below stated theorems should be used.

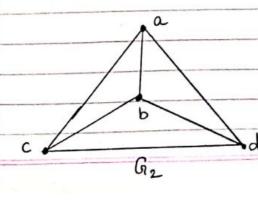
1. If G is connected graph with n vertices and if sum of degrees of each pair of vertices is greater than on equal to n-1 then there is Hamiltonian circuit.

2. In a simple connected graph with n vertices, if degree of each vertex is greater than or equal to n/2 then there is tamiltonian Circuit.

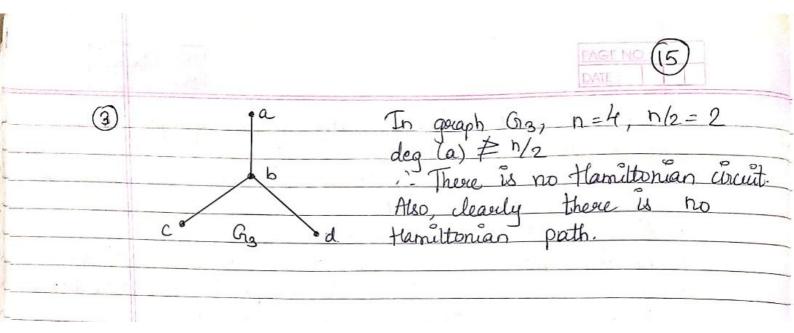
Check whether the following graphs have Hamiltonian path and on circuit.

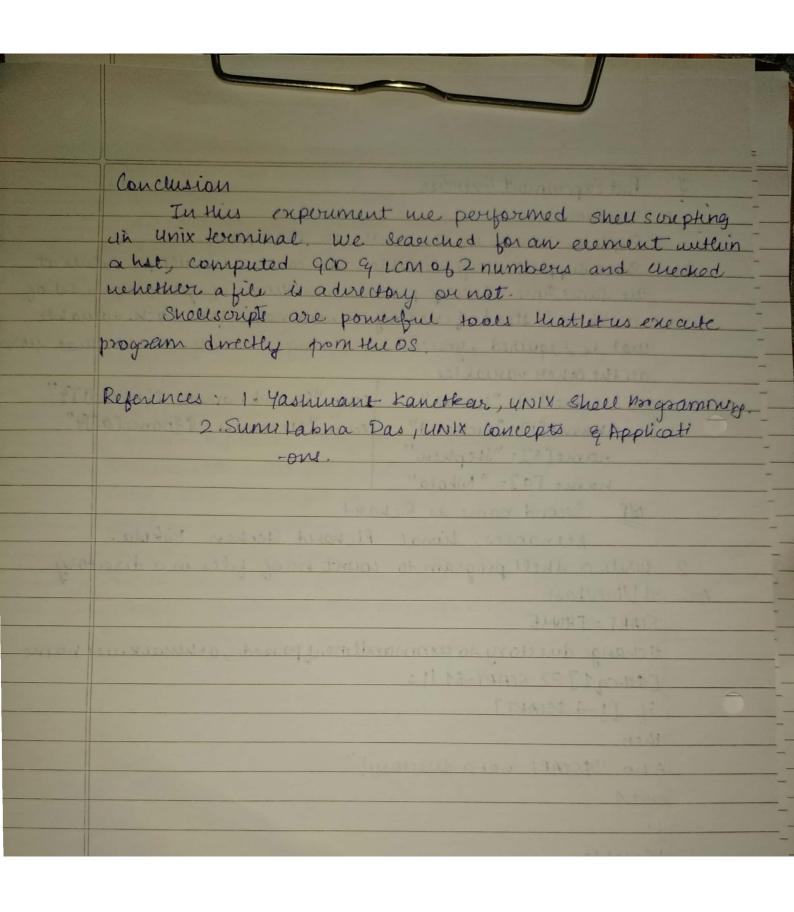


In Greaph G., n = 6. $\frac{1}{2} - \frac{1}{2} = 3$ deg. (a) = 2 $\frac{1}{2} - \frac{1}{2} = \frac{1}{2}$ $\frac{1}{2} - \frac{1}{2} = \frac{1}{2}$ But flamiltonian path exist - π : a - b - c - d - f - e.



In goiaph Ge, n=4. 1. 1/2=2 deplosed degoice of all veodices=3, which is goicated than 1/2 . Hamiltonian circuit exist To: a-c-b-d-a.





	7	Post Experiment Exercise
The same	В	
	Mille 1	Explain arrays in shell with an example
No. of Lot,	Ans.	Shell supports array variable. This can hold nultiple values at -
-		the same time. Array provide a method of grouping a set of
	Stupe	raviables. Instead of creating a new name for each variable
_		that is required, you can use a single array variable that stores
		all the other variables.
_	ANOIROS	ex name [0]= "lianae" ecuo "second name is \$? name[]?"
	O He	name[1]="Richard" ecuo "Aunames: \$\foane(@]\"
		name[3]="Stephen"
		name [4]="Nikola"
		off Second name is Richard
		beinames: Lional Richard Stephen Nikola.
	2.	write a shell program to count no of files in a directory.
		#1/bun/bash
		START = SHOME
		Houange dure ctory to commandline if passed, otherwise home.
		[\$#-eq1]82 START=\$1 1:
		ît [1-d \$STAPT]
		then
		echo "\$START nota directory!"
	the state of the s	out 1
	7.0	<i>ti</i>
		Variable Hackner Huge d)
		DIRS = S(find "\$START" - type d)
		Hoop Hirough each dur to get all subder files
		for d in soles
*		["\$d"]=""-a"\$d"]=" "] & 2 echo \$d directory has. \$ (U-L\$d lwc-L) files "11"?
	0	FOR EDUCATIONAL USE
	Sundaram	\$ (U-L Sd lwc-L) full "112
		done.

