

# ARTIFICIAL INTELLIGENCE

## ARTIFICIAL NEURAL NETWORKS-II

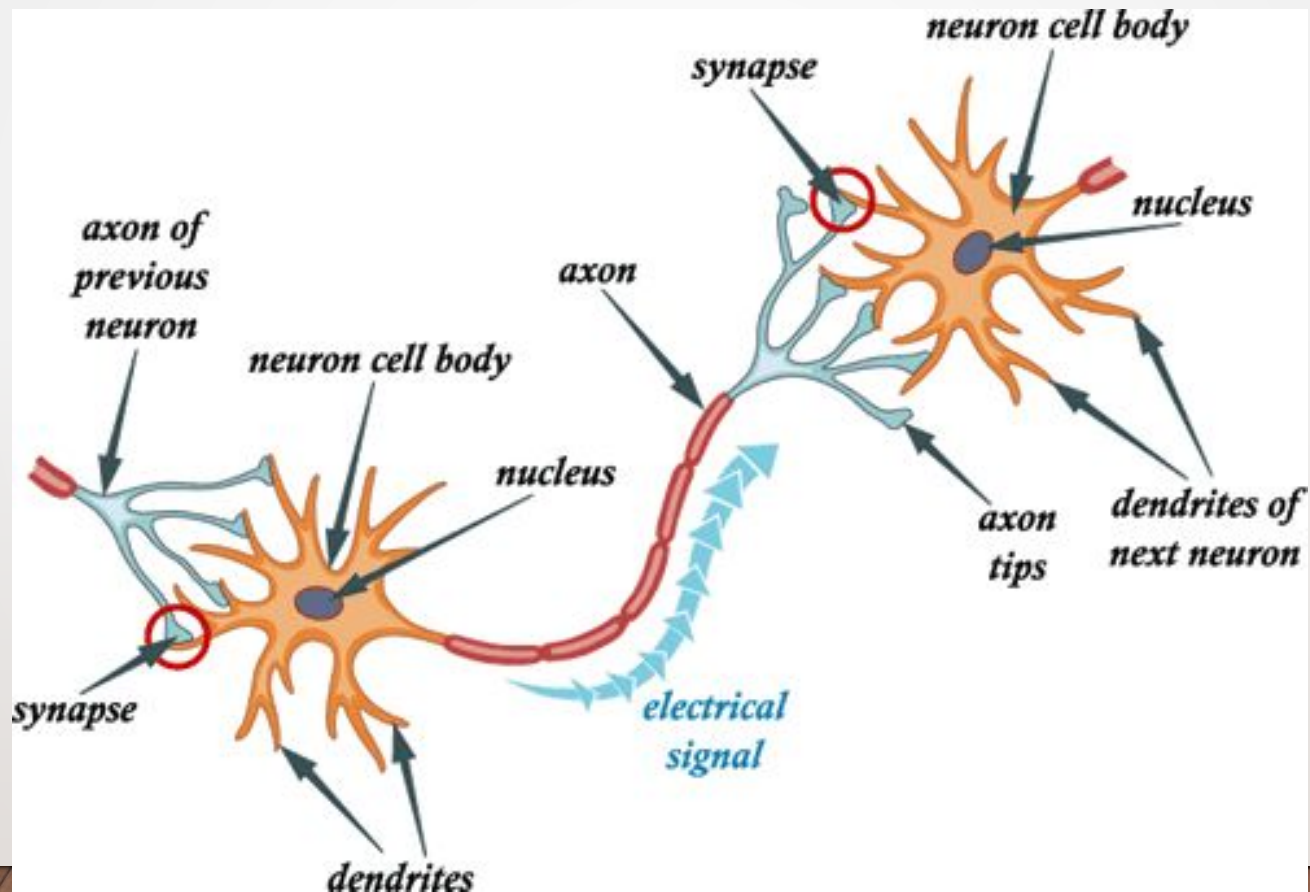


**CS-632**

**Dr. Muhammad Aqib**

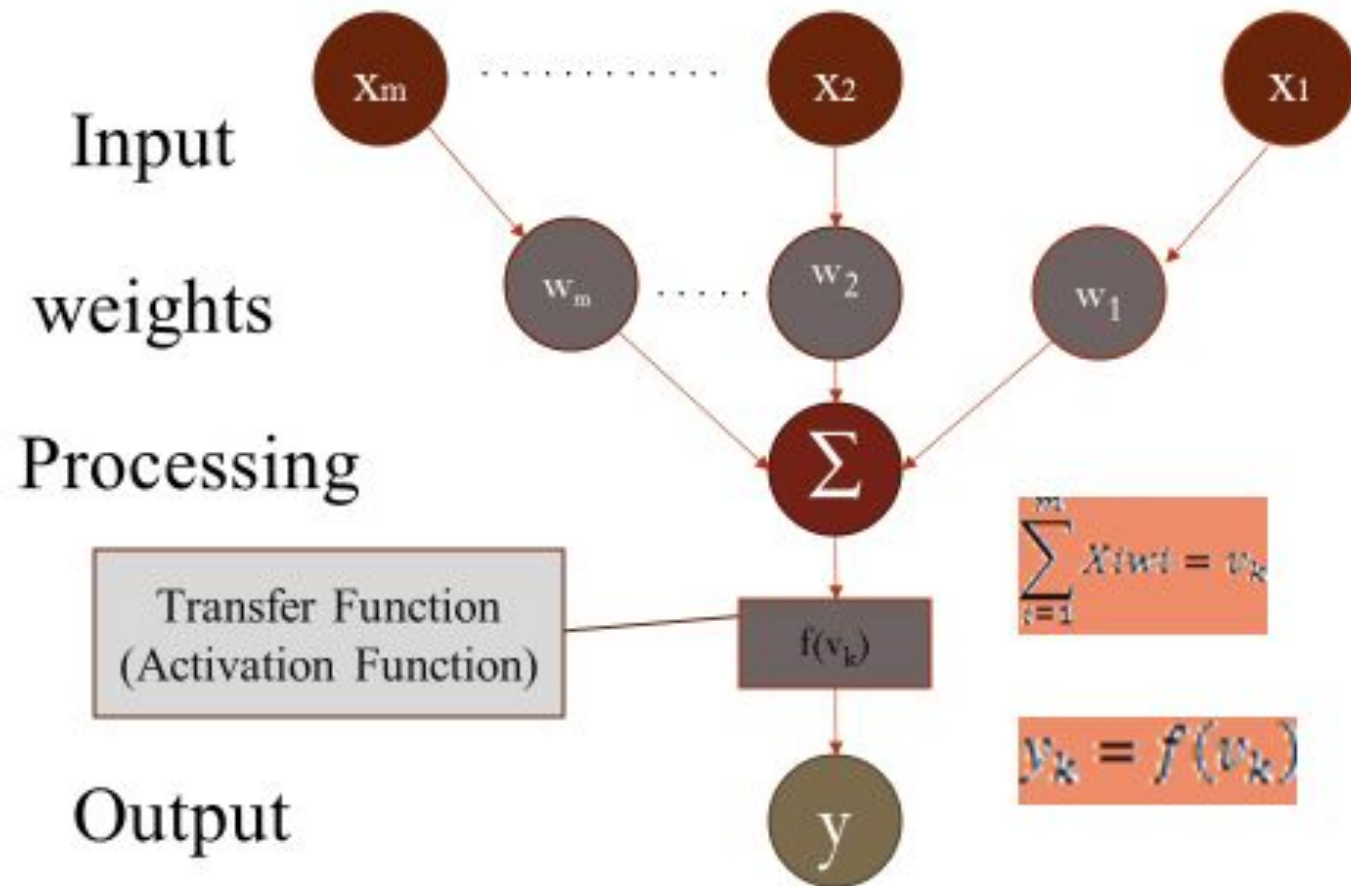
**University Institute of Information Technology  
PMAS-Arid Agriculture University Rawalpindi**

# THE PARTS OF A NEURON



# How do ANNs work?

The signal is not passed down to the next neuron verbatim



# ACTIVATION FUNCTIONS

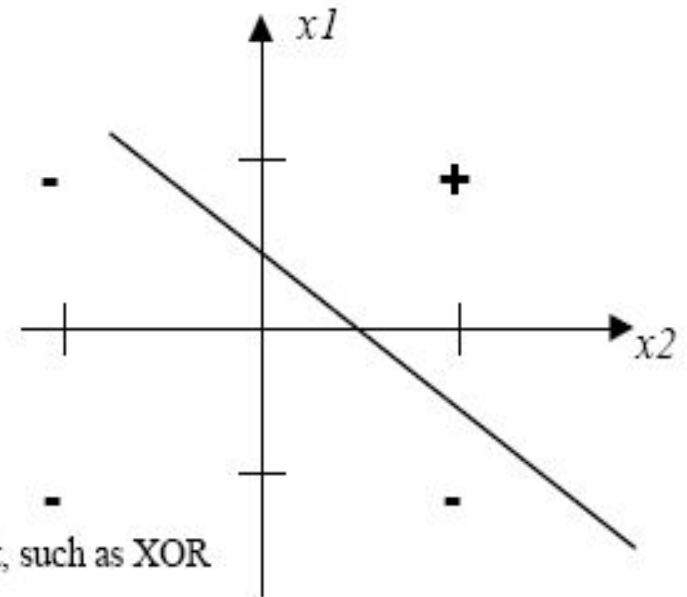
- Step(x) = 1 if  $x \geq t$ , else 0
- Sign(x) = +1 if  $x \geq 0$ , else -1
- Sigmoid(x) =  $1/(1+e^{-x})$
- Identity Function  $A(x) = X$

# REPRESENTATIONAL POWER OF PERCEPTRONS

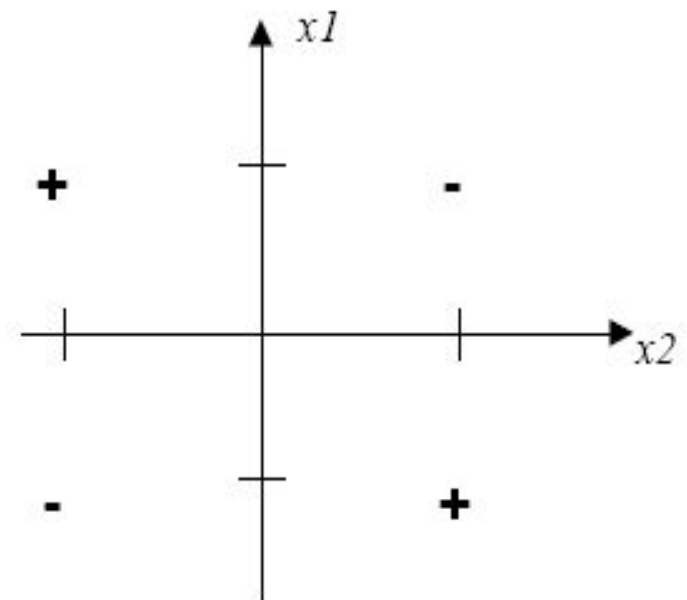
- Perceptrons can represent the logical AND, OR, and NOT functions as above.
- we consider 1 to represent True and  $-1$  to represent False.

In general, perceptrons can learn linearly separable functions, such as AND:

- Here there is no way to draw a single line that separates the "+" (true) values from the "-" (false) values.



But not those that are not, such as XOR



# TRAIN A PERCEPTRON

- At start of the experiment there are  $W$  random values
- Then the training begins with objective of teaching it to differentiate two classes of inputs I and II
- The goal is to have the nodes output  $o = 1$  if the input is of class I, and to have  
 $o = -1$  if the input is of class II
- You can free to choose any inputs ( $X_i$ ) and to designate them as being of class I or II



# TRAIN A PERCEPTRON

- If the node happened to output 1 signal when given a class II input or output -1 signal when given a class I input the weight  $W_i$  has no change.
- Then the training is complete.



# SINGLE LAYER PERCEPTRON

- For a problem which calls for more than 2 classes, several perceptrons can be combined into a network.
- Can distinguish only linear separable functions.

# SINGLE LAYER PERCEPTRON

Single layer, five nodes. 2 inputs and 3 outputs

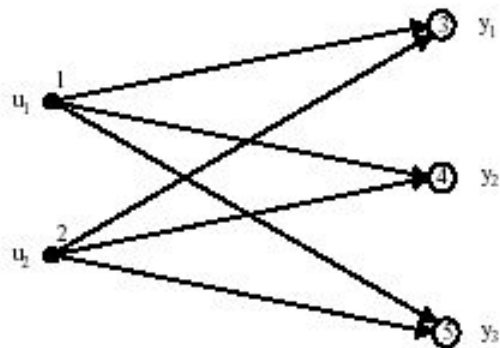


Figure 6: Single layer perceptron network with three output neurons.

Recognizes 3 linearly separable classes, by means of 2 features

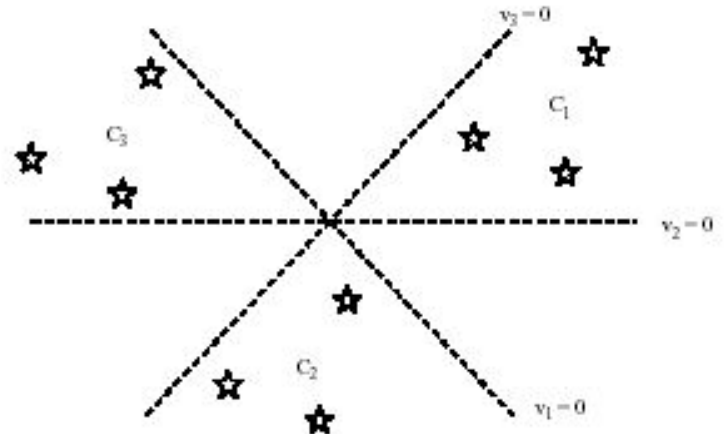
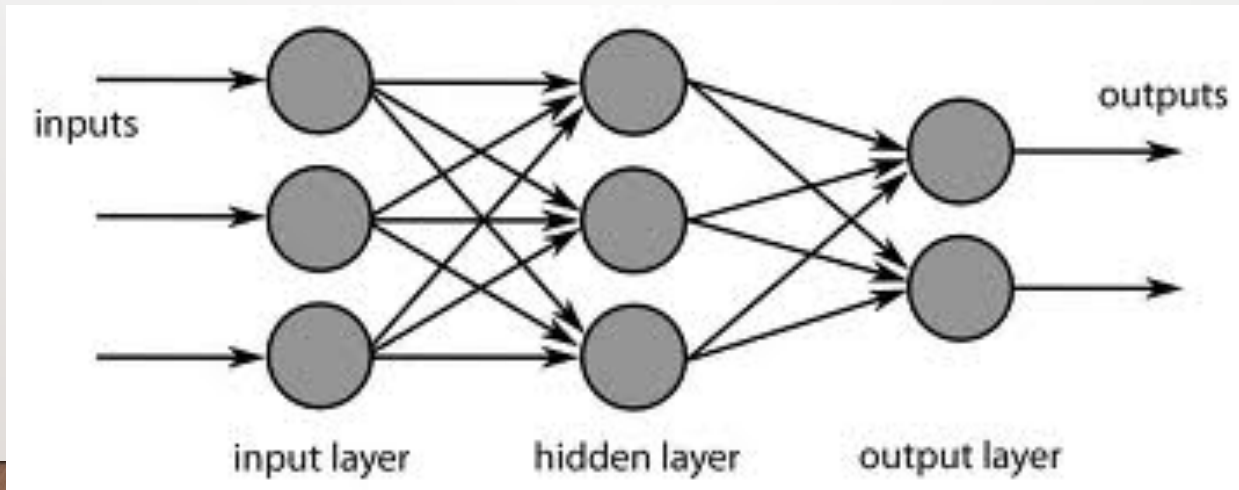


Figure 7: Three linearly separable classes.

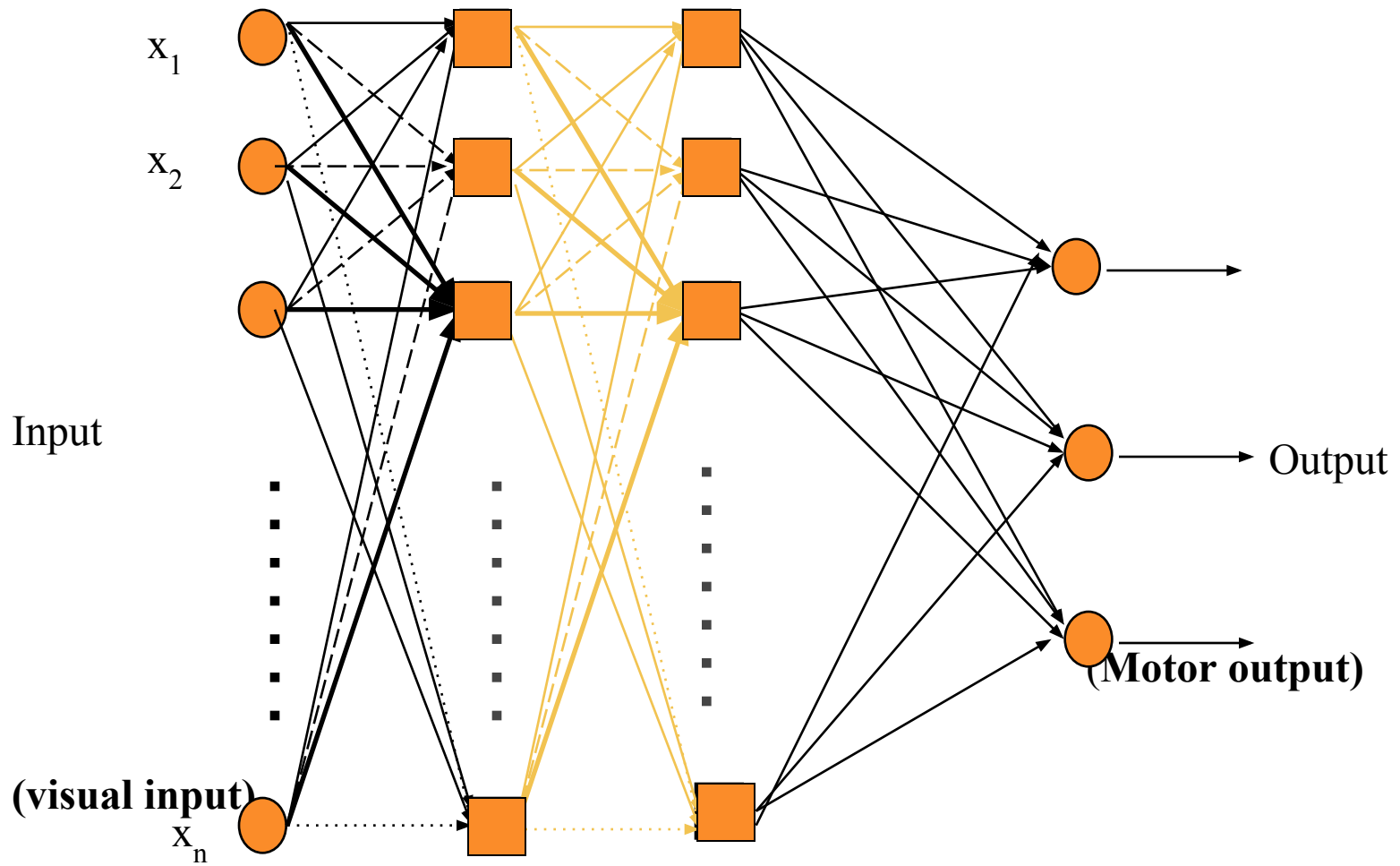
# MULTI-LAYER NETWORKS

# MULTI-LAYER NETWORKS

- A Multi layer perceptron can classify non linear separable problems.
- A Multilayer network has one or more hidden layers.



## Multi-layer networks

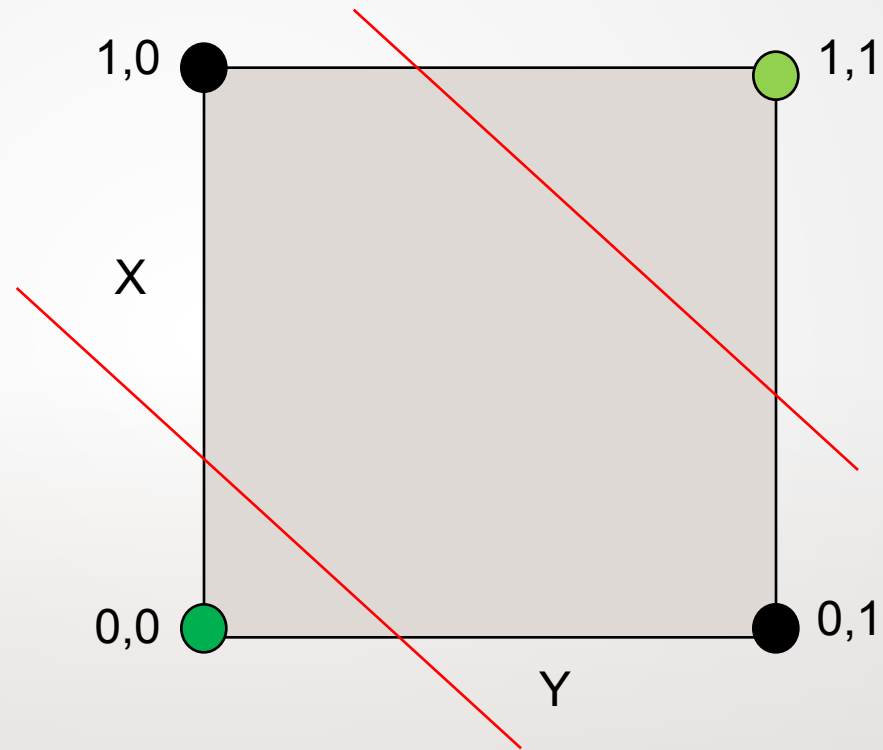


*Hidden layers*

# EXAMPLE

Logical XOR  
Function

<u>X</u>	<u>Y</u>	<u>output</u>
0	0	0
0	1	1
1	0	1
1	1	0



# XOR

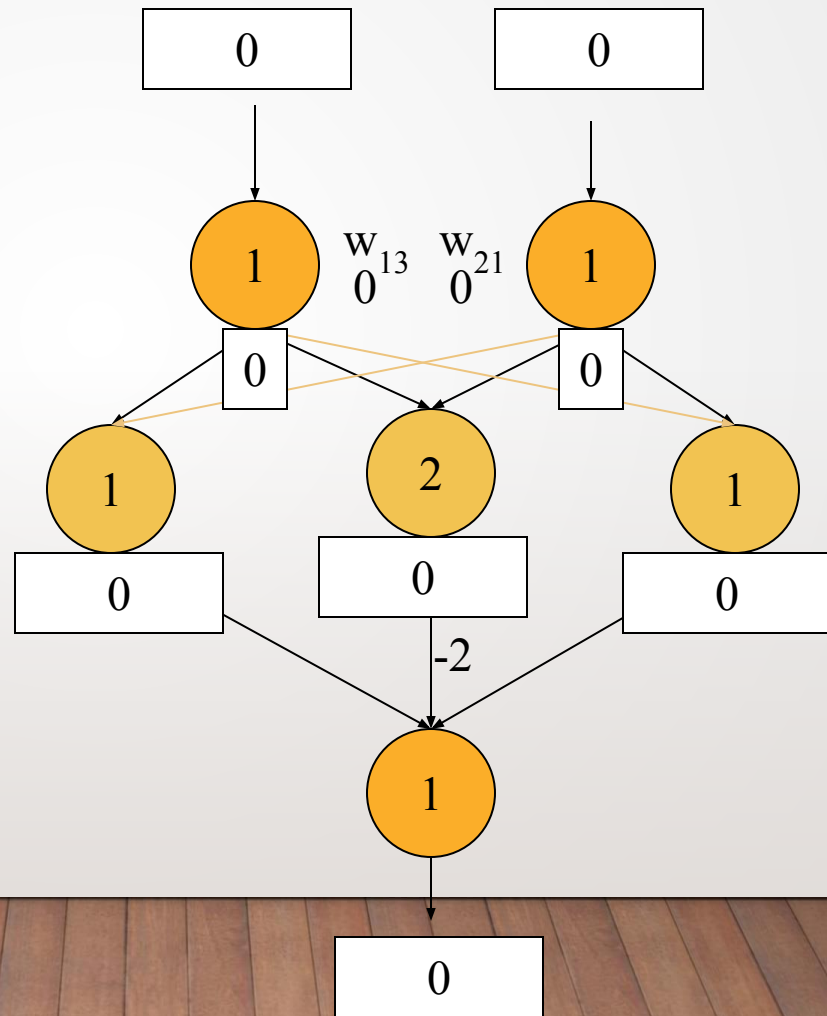
- XOR

Activation Function:

if (input  $\geq$  threshold), fire

else, don't fire

All weights are 1, unless  
otherwise labeled.





# XOR

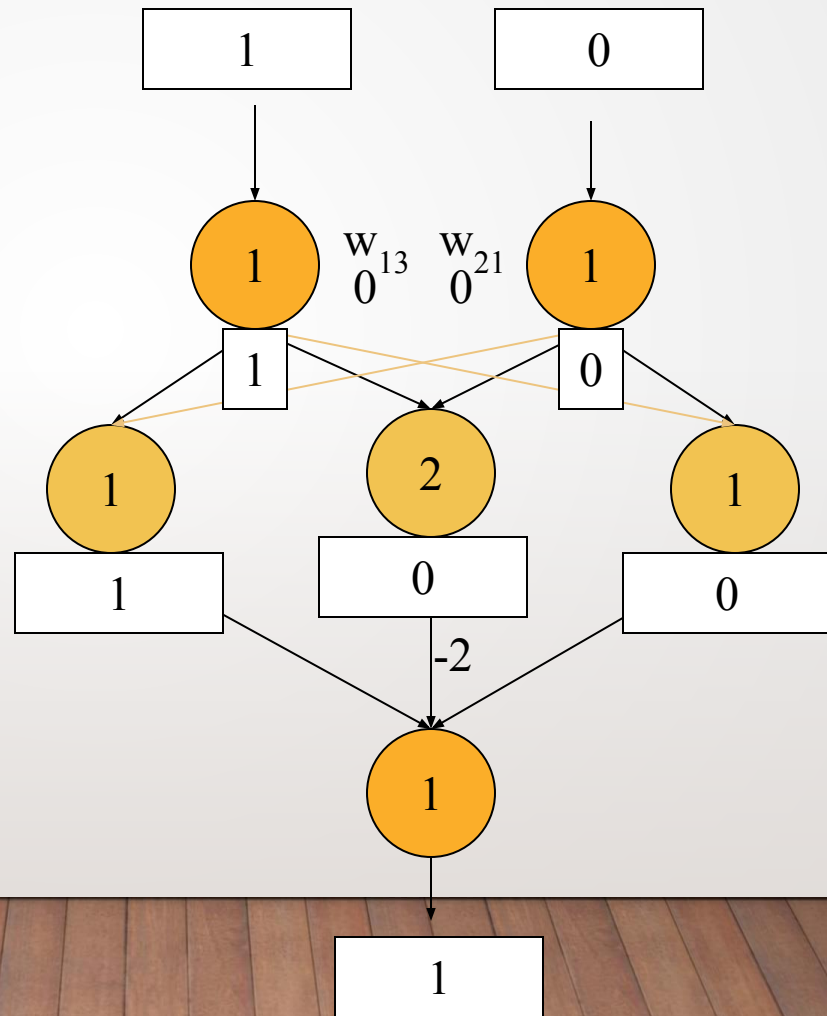
- XOR

Activation Function:

if (input  $\geq$  threshold), fire

else, don't fire

All weights are 1, unless  
otherwise labeled.



# XOR

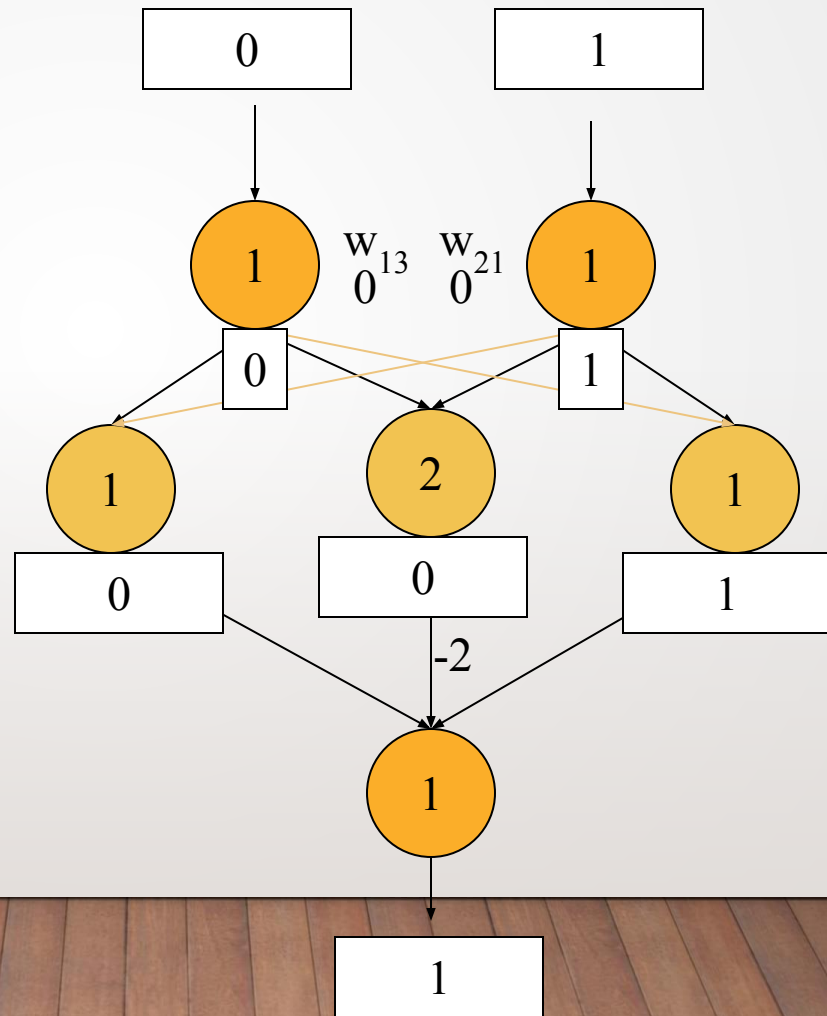
- XOR

Activation Function:

if (input  $\geq$  threshold), fire

else, don't fire

All weights are 1, unless  
otherwise labeled.



# XOR

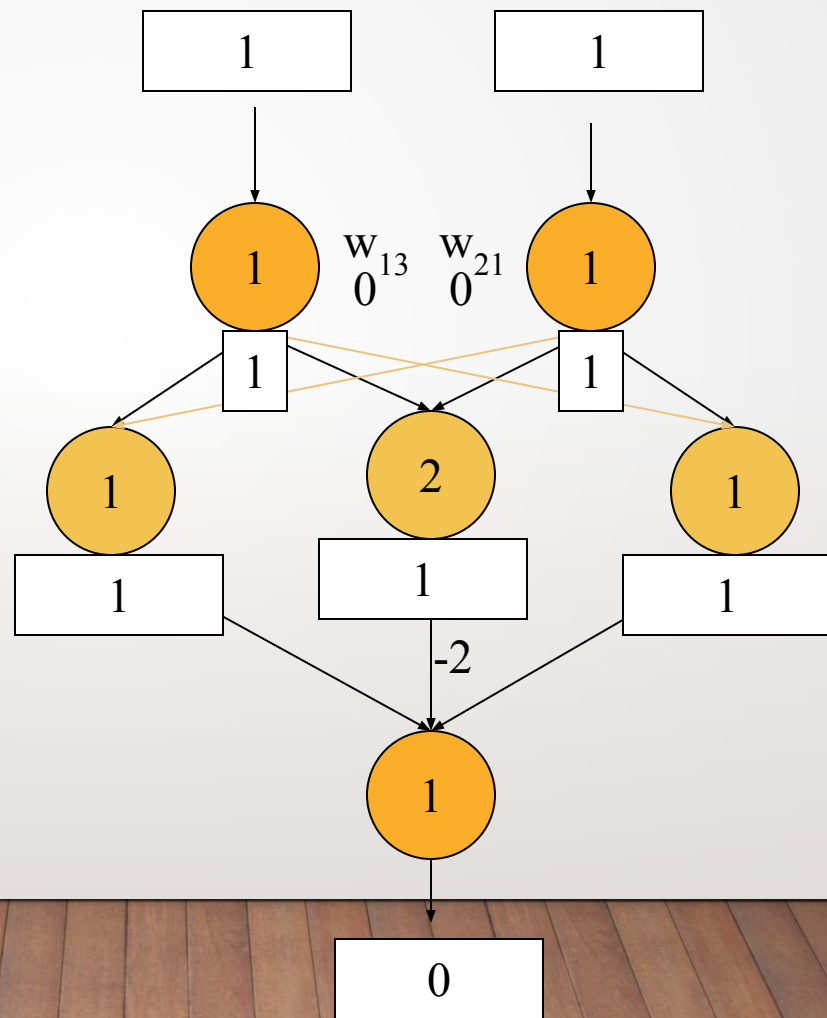
- XOR

Activation Function:

if (input  $\geq$  threshold), fire

else, don't fire

All weights are 1, unless  
otherwise labeled.



# Example: A Classification Task

- A typical **neural network application** is **classification**. Consider the simple **example** of classifying trucks given their masses and lengths

MASS	LENGTH	CLASS
10.0	6	LORRY
20.0	5	LORRY
5.0	4	VAN
2.0	5	VAN
2.0	5	VAN
3.0	6	LORRY
10.0	7	LORRY
15.0	8	LORRY
5.0	9	LORRY

*How do construct a neural network that can classify any Lorry and Van?*

# TRAINING MULTILAYER PERCEPTRON

- The training of multilayer networks raises some important issues:
- How many layers ?, how many neurons per layer ?
- **Too few neurons** makes the network unable to learn the desired behavior.
- **Too many neurons** increases the complexity of the learning algorithm.

# TRAINING MULTILAYER PERCEPTRON

- A desired property of a neural network is its ability to generalize from the training set.
- If there are **too many neurons**, there is the danger of over fitting.

# TRAINING PERCEPTRONS

- Learning involves choosing values for the weights
- The perceptron is trained as follows:
  - First, inputs are given random weights (usually between  $-0.5$  and  $0.5$ ).
  - An item of training data is presented. If the perceptron mis-classifies it, the weights are modified according to the following:
$$w_i \leftarrow w_i + (a \times x_i \times (t - o))$$
    - where  $t$  is the target output for the training example,  $o$  is the output generated by the perceptron and  $a$  is the learning rate, between 0 and 1 (usually small such as 0.1)
- Cycle through training examples until successfully classify all examples
  - Each cycle known as an **epoch**



# BACKPROPAGATION

- Multilayer neural networks learn in the same way as perceptrons.
- However, there are many more weights, and it is important to assign credit (or blame) correctly when changing weights.
- $E$  sums the errors over all of the network output units

$$E(\mathbf{w}) \equiv \frac{1}{2} \sum_{d \in D} \sum_{k \in \text{outputs}} (t_{kd} - o_{kd})^2$$

# BACKPROPAGATION ALGORITHM

- Create a feed-forward network with  $n_{in}$  inputs,  $n_{hidden}$  hidden units, and  $n_{out}$  output units.
- Initialize all network weights to small random numbers
- Until termination condition is met, Do
  - For each  $\langle x, t \rangle$  in training examples, Do
    - Propagate the input forward through the network:*
      1. Input the instance  $x$  to the network and compute the output  $o_u$  of every unit  $u$  in the network
    - Propagate the errors backward through the network:*
      2. For each network output unit  $k$ , calculate its error term  $\delta_k$ 
$$\delta_k \leftarrow o_k(1 - o_k)(t_k - o_k)$$
      3. For each hidden unit  $h$ , calculate its error term  $\delta_h$ 
$$\delta_h \leftarrow o_h(1 - o_h) \sum_{k \in \text{outputs}} w_{kh} \delta_k$$
      4. Update each network weight  $w_{ji}$ 
$$w_{ji} \leftarrow w_{ji} + \Delta w_{ji}$$

where

$$\Delta w_{ji} = \alpha \delta_j x_{ji}$$

# PROBLEMS WITH TRAINING:

- Nets get stuck
  - Not enough degrees of freedom
  - Hidden layer is too small
- Training becomes unstable
  - too many degrees of freedom
  - Hidden layer is too big / too many hidden layers
- Over-fitting
  - Can find every pattern, not all are significant. If neural net is “over-fit” it will not generalize well to the testing dataset

**Thank  
You**