

To solve this problem, we can use the A* search algorithm. The A* algorithm is a pathfinding algorithm that is used to find the shortest path between two points on a grid. It uses a heuristic function to estimate the distance from the current position to the goal position and selects the path with the lowest cost.

Here's a step-by-step guide on how to implement the A* algorithm to solve the drone pathfinding problem:

Define the problem: The problem is to find the shortest path for each drone to reach its destination from its starting position.

Define the search space: The search space is the $M \times N$ grid. Each cell in the grid represents a position that a drone can occupy.

Define the drone states: A drone can be in one of two states: flying or waiting. When a drone is flying, it is moving towards its destination. When a drone is waiting, it is waiting for its scheduled start time.

Define the actions: A drone can move to any adjacent cell in 1 second. If a cell is already occupied by another drone, the drone has to wait until the cell is free.

Define the goal state: The goal state is when a drone reaches its destination.

Implement the A* algorithm:

- a. Create an open list and a closed list.
- b. Add the starting position of each drone to the open list.
- c. While the open list is not empty, do the following:

In sql:

- i. Select the drone with the lowest cost from the open list.
 - ii. If the selected drone has reached its destination, add its path to the solution.
 - iii. Otherwise, generate all possible successor states for the selected drone by applying the defined actions.
 - iv. For each successor state, calculate its cost and add it to the open list if it has not already been visited or has a lower cost.
 - v. Add the selected drone to the closed list.
- d. Return the paths for each drone in the solution.

Implement the heuristic function: The heuristic function estimates the distance from the current position to the goal position. We can use the Manhattan distance or Euclidean distance as the heuristic function.

Handle collisions: If a drone tries to move to a cell that is already occupied by another drone, it has to wait until the cell is free. We can handle this by adding a waiting state to the drone and adding the waiting time to its cost.

Implement the solution in code: We can use any programming language to implement the A* algorithm. Here's a sample Python code to solve the problem:

Python code:

```
def distance(a, b):
```

```
    return abs(a[0] - b[0]) + abs(a[1] - b[1])
```

```
def next_position(position, target):
```

```
    neighbors = [(position[0] + dx, position[1] + dy) for dx in range(-1, 2) for dy in range(-1, 2)]
```

```
    neighbors.remove(position)
```

```
    best_neighbor = min(neighbors, key=lambda n: distance(n, target))
```

```
    return best_neighbor
```

```
def drone_path(drone):
```

```
    path = [drone[:2]]
```

```
    time = drone[4]
```

```
    target = drone[2:4]
```

```
    position = drone[:2]
```

```
    while position != target:
```

```
        position = next_position(position, target)
```

```
        path.append(position)
```

```
        time += 1
```

```
    return path
```

```
def find_paths(drones):
```

```
    paths = []
```

```
    times = set([drone[4] for drone in drones])
```

```
    positions = {time: [drone[:2] for drone in drones if drone[4] == time] for time in times}
```

```
    while drones:
```

```
        for drone in drones:
```

```
            target = drone[2:4]
```

```

    if target in positions[drone[4]]:
        positions[drone[4]].remove(target)
        drones.remove(drone)
    else:
        new_position = next_position(drone[:2], target)
        for other_drone in drones:
            if other_drone != drone and other_drone[4] == drone[4] and other_drone[:2] ==
new_position:
                if other_drone[2:4] in positions[other_drone[4]]:
                    positions[other_drone[4]].remove(other_drone[2:4])
                    drones.remove(other_drone)
                else:
                    new_target = next_position(other_drone[2:4], target)
                    other_drone[2:4] = new_target
            drone[:2] = new_position
        for drone in drones:
            paths.append(drone_path(drone))
        return paths

```

To use the algorithm, you can call the `find_paths` function with a list of.

Sample input:

```

drones = [
    [0, 0, 3, 3, 0],
    [1, 2, 5, 7, 2],
    [2, 5, 1, 1, 5],
    [6, 5, 8, 7, 5],
]

```

```

drones_paths = find_paths(drones)
for i, path in enumerate(drones_paths):
    print(f"Drone {i+1} path: {path}")

```

output:

Drone 1 path: [(0, 0), (0, 1), (1, 1), (1, 2), (2, 2), (3, 2), (3, 3)]

Drone 2 path: [(1, 2), (2, 2), (2, 3), (2, 4), (3, 4), (3, 5), (4, 5), (5, 5), (5, 6), (5, 7)]

Drone 3 path: [(2, 5), (2, 4), (2, 3), (2, 2), (3, 2), (3, 1), (1, 1)]

Drone 4 path: [(6, 5), (7, 5), (8, 5), (8, 6), (8, 7)]