

Searching and Sorting

Searching

- We search everyday!
 - Search for your wallet before leaving home
 - Search for the answer of an assignment from the Internet
 - Search for your friends in the canteen.

Searching

- In chapter 1,
 - We search for the textbook from the library

EXAMPLE OF SEARCHING

- Algorithm 1
 - Input: Title/Author/Keywords/Call number
 - Output: Get the book
 - Procedures:
 - 1. Go to the library
 - 2. Scan all books in the library from the leftmost bookshelf
 - 3. Compare the book information with the input
 - 4. If they are matched, get the book. Otherwise, compare with the next book

EXAMPLE OF SEARCHING

- Algorithm 2

- Input: Title/Author/Keywords/Call number
- Output: Get the book
- Procedures:
 - 1. Go to the library
 - 2. Use a computer to find the call number of the book
 - 3. Directly go to the bookshelf stated in the call number
 - 4. Compare the book information with the input
 - 5. If they are matched, get the book. Otherwise, compare with the next book

Sequential Search

Sequential Search

- Consider the array of seven elements shown in below.

list	35	12	27	18	45	16	38
------	----	----	----	----	----	----	----

Sequential Search

- Suppose that you want to determine whether 27 is in the list



27

Sequential Search


- The sequential search works as follows:
 - 1. Compare 27 with list[0]
 - That is, compare 27 with 35.
 - 2. Because list[0] != 27, then compare 27 with list[1]
 - That is, compare 27 with 12
 - 3. Because list[1] != 27, then compare 27 with list[2]
 - That is, compare 27 with 27

Sequential Search

- The sequential search works as follows:
 - 4. Because `list[2] = 27`, the search stops.
- The is a successful search!

Sequential Search

- Now search for 10



10

Sequential Search

- As before, the search starts with the first element in the list – `list[0]`
- This time the search item, which is 10, is compared with every item in the list.
- Eventually, no more data is left in the list to compare with the search item.
- This is an unsuccessful search.

Sequential Search

- Two situation to stop the search
 - As soon as you find an element in the list that is equal to the search item
 - You stop the search and report “success”
 - Usually, you also tell the location in the list where the search item was found.

Sequential Search

- Two situation to stop the search
 - Otherwise, after the search item is compared with every element in the list
 - You must stop the search and report “failure”.

Binary Search

BINARY SEARCH

- Generally, to find a value in **unsorted array**, we should look through elements of an array **one by one**, until searched value is found.
- In case of searched value is **absent** from array, we go **through all** elements.
- In average, **complexity** of such an algorithm is **proportional** to the **length** of the array.

BINARY SEARCH

- Situation **changes** significantly, when array is sorted.
- If we know it, **random access capability** can be utilized very efficiently to find searched value quick.

BINARY SEARCH

- Cost of searching algorithm reduces to **binary logarithm** of the array length.
 - For reference, $\log_2(1\ 000\ 000) \approx 20$.
- It means, that **in worst case**, algorithm makes **20 steps** to find a value in sorted array of a **million** elements or to say, that it doesn't present it the array.

ALGORITHM

- Algorithm is quite simple. It can be done either recursively or iteratively:
 1. get the middle element;

ALGORITHM

- Algorithm is quite simple. It can be done either recursively or iteratively:
 2. if the middle element equals to the searched value, the algorithm stops;

ALGORITHM

- Algorithm is quite simple. It can be done either recursively or iteratively:
3. otherwise, two cases are possible:
- searched value is less than the middle element.
In this case, go to the step 1 for the part of the array, before middle element.
 - searched value is greater than the middle element.
In this case, go to the step 1 for the part of the array, after middle element.

ALGORITHM

- Now we should define, when iterations should stop.
 - First case is when searched element is found.
 - Second one is when subarray has no elements.
 - In this case, we can conclude, that searched value doesn't present in the array.

EXAMPLE

- *Example 1.*

Find 6 in $\{-1, 5, 6, 18, 19, 25, 46, 78, 102, 114\}$.

- Step 1 (middle element is $19 > 6$): -

1 5 6 18 19 25 46 78 102 114

- Step 2 (middle element is $5 < 6$): -

1 5 6 18 19 25 46 78 102 114

- Step 3 (middle element is $6 == 6$): -

1 5 6 18 19 25 46 78 102 114

EXAMPLE

- *Example 2.* Find 103 in {-1, 5, 6, 18, 19, 25, 46, 78, 102, 114}.
 - Step 1 (middle element is $103 > 19$): -
1 5 6 18 19 25 46 78 102 114
 - Step 2 (middle element is $103 > 78$): -
1 5 6 18 19 25 46 78 102 114
 - Step 3 (middle element is $103 > 102$): -
1 5 6 18 19 25 46 78 102 114
 - Step 4 (middle element is $114 > 103$): -
1 5 6 18 19 25 46 78 102 114
 - Step 5 (searched value is absent):

Sorting

SORTING

- Sorting is one of the most important operations performed by computers.

SORTING

- The efficiency of data handling can often be substantially increased if the data are sorted according to some criteria of order.

SORTING



- For example:
 - It would be practically impossible to find a name in the telephone directory if the names were not alphabetically ordered.
 - The same can be said about dictionaries, book indexes, payrolls, bank accounts, student lists, and other alphabetically organized materials.

SORTING

- The first step is to choose the criteria that will be used to order data.
 - Very often, the sorting criteria are natural, as in the case of numbers.
- A set of numbers can be sorted in ascending or descending order.
 - Ascending: (1, 2, 5, 8, 20)
 - Descending: (20, 8, 5, 2, 1)

SORTING

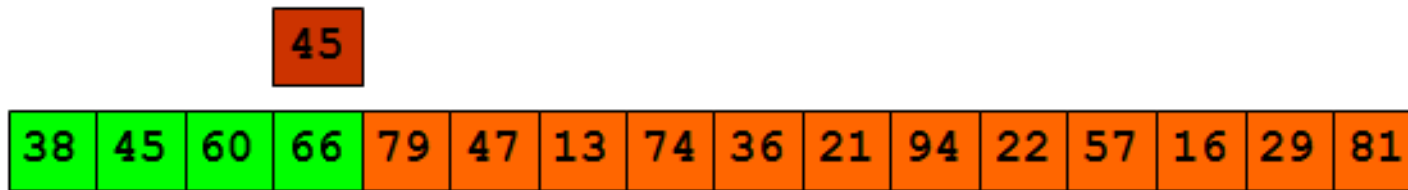
- Names in the phone book are ordered alphabetically by last name, which is the natural order.
- For alphabetic and non-alphabetic characters, the American Standard Code for Information Interchange (ASCII) code is commonly used.

SORTING

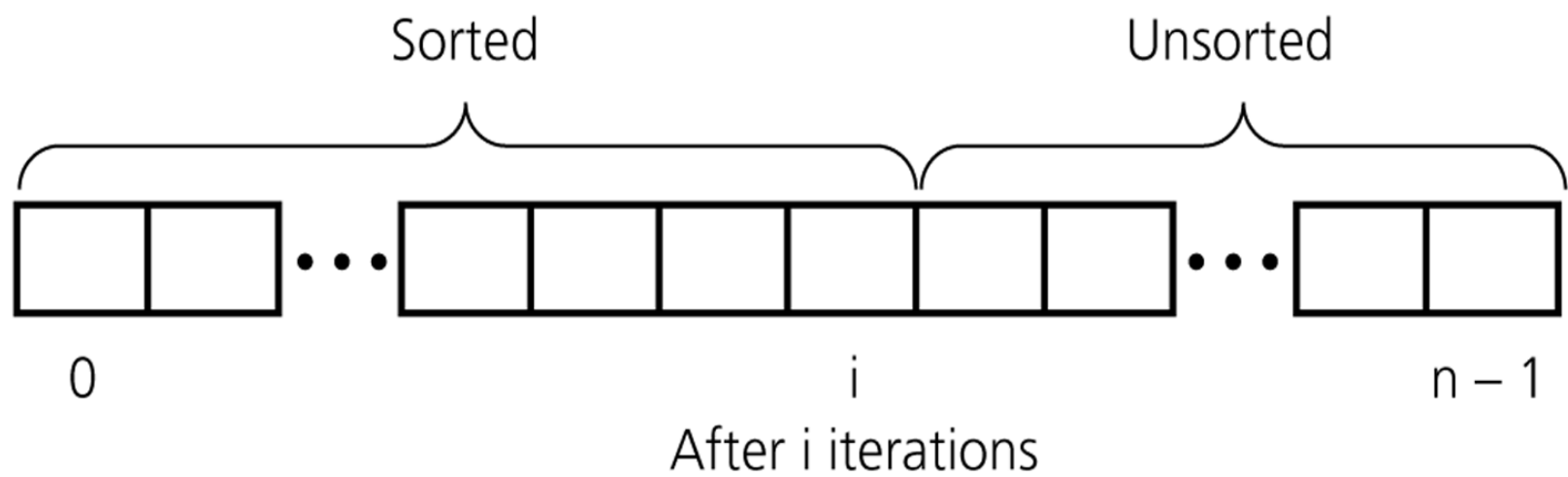
- There are many sorting algorithms and we will focus on the following:
 - Insertion sort
 - Selection sort
 - Bubble sort
 - Quicksort

Insertion Sort

- while some elements unsorted:
 - Using linear search, find the location in the sorted portion where the 1st element of the unsorted portion should be inserted
 - Move all the elements after the insertion location up one position to make space for the new element



the fourth iteration of this loop is shown here



Initial array:

29	10	14	37	13
-----------	----	----	----	----

29	29	14	37	13
----	----	----	----	----

10	29	14	37	13
-----------	-----------	----	----	----

10	29	29	37	13
----	----	----	----	----

10	14	29	37	13
-----------	-----------	-----------	----	----

10	14	29	37	13
-----------	-----------	-----------	-----------	----

10	14	14	29	37
----	----	----	----	----

Sorted array:

10	13	14	29	37
-----------	-----------	-----------	-----------	-----------

Copy 10

Shift 29

Insert 10; copy 14

Shift 29

Insert 14; copy 37, insert 37 on top of itself

Copy 13

Shift 37, 29, 14

Insert 13

One more example

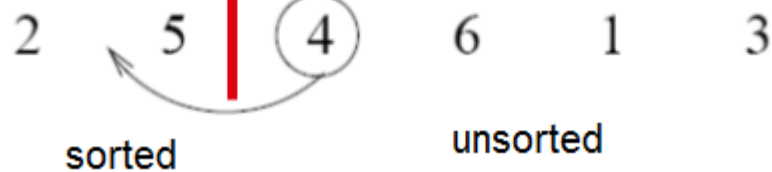
input array

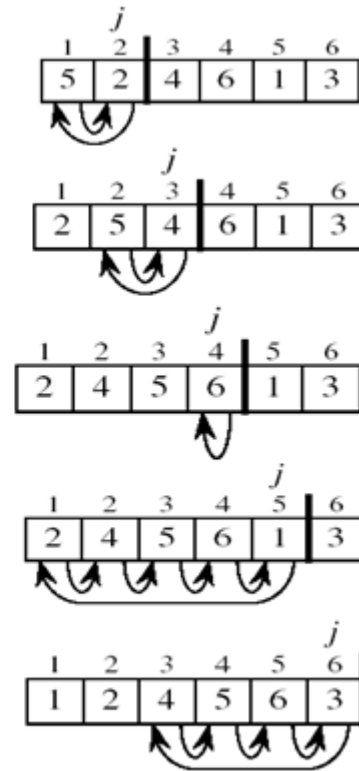
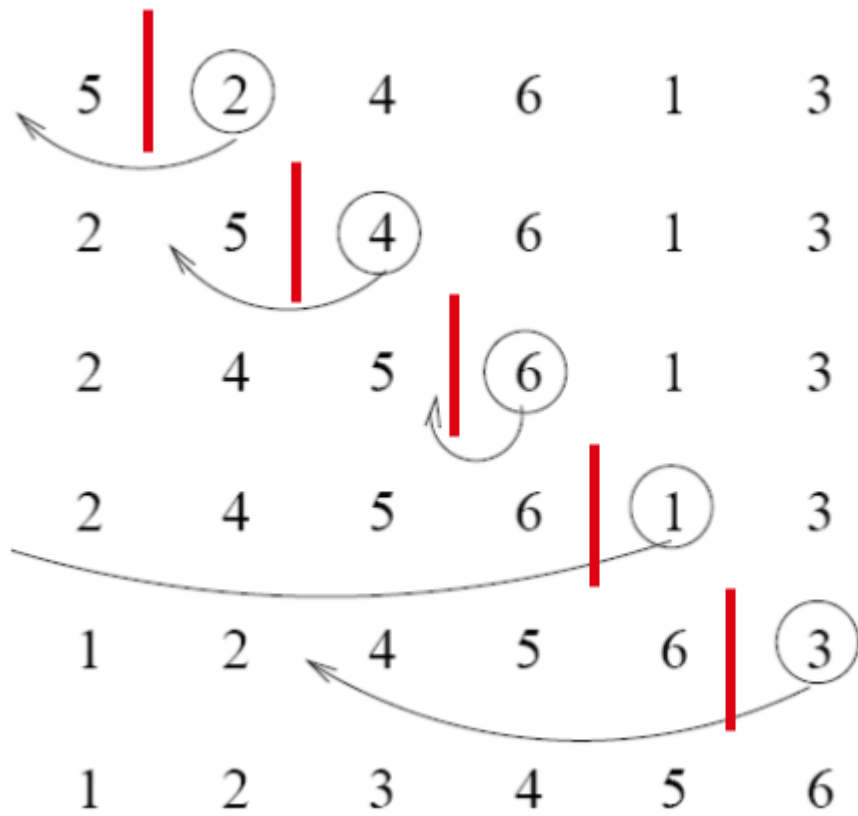
5 2 4 6 1 3

at each iteration, the array is divided in two sub-arrays:

left sub-array

right sub-array





C function

```
public void insertionSort(Comparable[] arr) {  
    for (int i = 1; i < arr.length; ++i) {  
        Comparable temp = arr[i];  
        int pos = i;  
        // Shuffle up all sorted items > arr[i]  
        while (pos > 0 &&  
                arr[pos-1].compareTo(temp) > 0) {  
            arr[pos] = arr[pos-1];  
            pos--;  
        } // end while  
        // Insert the current item  
        arr[pos] = temp;  
    }  
}
```

Selection Sort

Selection Sort Algorithm

- Given an array of items, arrange the items so that they are sorted from smallest to largest.
- **Select** next item, in turn, that will be appended to the sorted part of the array:
 - Scan the array to find the smallest value, then swap this value with the value at cell 0.
 - Scan the remaining values (all but the first value), to find the next smallest, then swap this value with the value at cell 1.
 - Scan the remaining values (all but the first two) to find the next smallest, then swap this value with the value at cell 2.
 - Continue until the array is sorted.

Example: Selection Sort

[0]	[1]	[2]	[3]	[4]	
5	1	3	7	2	find min
1	5	3	7	2	swap to index 0
1	5	3	7	2	find min
1	2	3	7	5	swap to index 1
1	2	3	7	5	find min
1	2	3	7	5	swap to index 2
1	2	3	7	5	find min
1	2	3	5	7	swap to index 3

```
public static void selectionSort(int[] data) {  
  
    for (int numSort = 0; numSort < data.length-1; numSort++){  
  
        // find the next minimum  
        int minPos = numSort ; // initial position of next min  
        for (int pos = numSort+1 ; pos < data.length; pos++) {  
            if (data[minPos] > data[pos])  
                minPos = pos; // found new min  
        }  
  
        // swap min to next position in sorted list  
        int temp = data[minPos];  
        data[minPos] = data[ numSort ];  
        data[ numSort ] = temp;  
    }  
}
```

Bubble Sort

- Simplest sorting algorithm
- Idea:
 - 1. Set flag = false
 - 2. Traverse the array and compare pairs of two consecutive elements
 - 1.1 If $E1 \leq E2$ -> OK (do nothing)
 - 1.2 If $E1 > E2$ then Swap($E1, E2$) and set flag = true
 - 3. repeat 1. and 2. while flag=true.

Bubble Sort

1	1	23	2	56	9	8	10	100
2	1	2	23	56	9	8	10	100
3	1	2	23	9	56	8	10	100
4	1	2	23	9	8	56	10	100
5	1	2	23	9	8	10	56	100

---- finish the first traversal ----

1	1	2	23	9	8	10	56	100
2	1	2	9	23	8	10	56	100
3	1	2	9	8	23	10	56	100
4	1	2	9	8	10	23	56	100

---- finish the second traversal ----

...

C function

```
public void bubbleSort (Comparable[] arr) {  
    boolean isSorted = false;  
    while (!isSorted) {  
        isSorted = true;  
        for (i = 0; i<arr.length-1; i++)  
            if (arr[i].compareTo(arr[i+1]) > 0) {  
                Comparable tmp = arr[i];  
                arr[i] = arr[i+1];  
                arr[i+1] = tmp;  
                isSorted = false;  
            }  
    }  
}
```

Quick Sort

- Quicksort is also based on the *divide-and-conquer* paradigm.
- It works as follows:
 1. First, it partitions an array into two parts,
 2. Then, it sorts the parts independently,
 3. Finally, it combines the sorted subsequences by a simple concatenation.

The quick-sort algorithm consists of the following three steps:

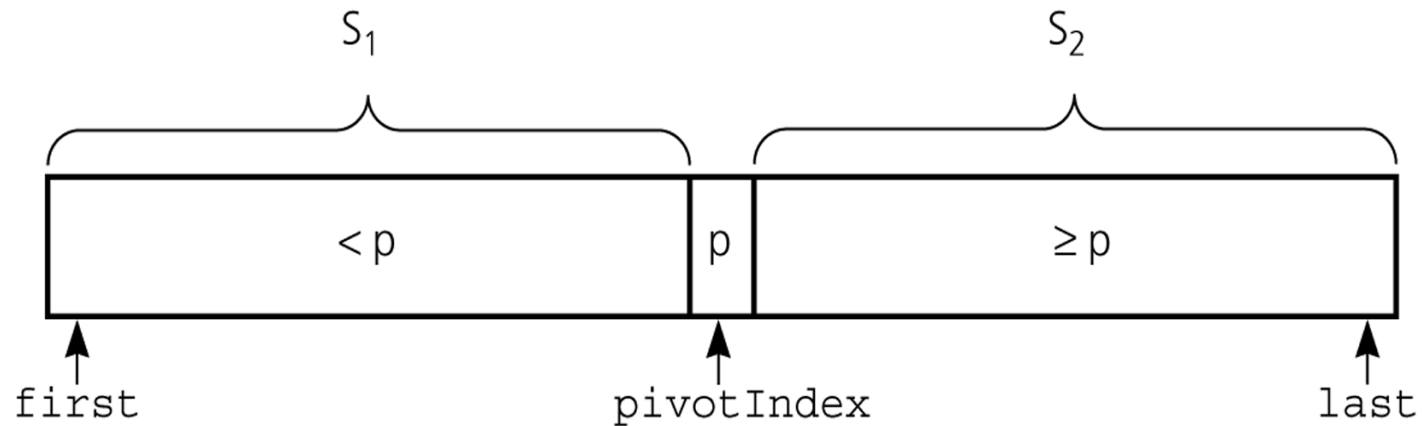
1. **Divide**: Partition the list.

- To partition the list, we first choose some element from the list for which we hope about half the elements will come before and half after. Call this element the **pivot**.
- Then we partition the elements so that all those with values less than the pivot come in one sublist and all those with greater values come in another.

2. **Recursion**: Recursively sort the sublists separately.

3. **Conquer**: Put the sorted sublists together.

- Partitioning places the pivot in its correct place position within the array.



- Arranging the array elements around the pivot p generates two smaller sorting problems.
 - sort the left section of the array, and sort the right section of the array.
 - when these two smaller sorting problems are solved recursively, our bigger sorting problem is solved.

QUICKSORT

- *Example:*

- Sort {1, 12, 5, 26, 7, 14, 3, 7, 2} using quicksort.

1	12	5	26	7	14	3	7	2
---	----	---	----	---	----	---	---	---

QUICKSORT

1	12	5	26	7	14	3	7	2
---	----	---	----	---	----	---	---	---

- Unsorted

1	12	5	26	7	14	3	7	2
↑				↑				↑
i				pivot value				j

- Pivot value = 7

1	12	5	26	7	14	3	7	2
	↑							↑
	i							j

- $12 \geq 7 \geq 2$. swap

1	2	5	26	7	14	3	7	12
			↑				↑	
			i				j	

- $26 \geq 7 \geq 7$, swap

QUICKSORT

1	2	5	7	7	14	3	26	12
---	---	---	---	---	----	---	----	----

1	2	5	7	7	14	3	26	12
---	---	---	---	---	----	---	----	----



i



j

- $7 \geq 7 \geq 3$, swap

1	2	5	7	3	14	7	26	12
---	---	---	---	---	----	---	----	----



j



i

- $i > j$, stop partition

1	2	5	7	3
---	---	---	---	---

14	7	26	12
----	---	----	----

- run quicksort recursively

QUICKSORT

1	2	5	7	3
---	---	---	---	---



pivot value

1	2	5	7	3
---	---	---	---	---



i



j

1	2	3	7	5
---	---	---	---	---



j



i

1	2	3
---	---	---

7	5
---	---

1	2	3
---	---	---

5	7
---	---

- Pivot value = 5
- $5 \geq 5 \geq 3$. swap
- $i > j$, stop partition
- run quicksort recursively

QUICKSORT

14	7	26	12
----	---	----	----



pivot value

14	7	26	12
----	---	----	----



i

j

7	14	26	12
---	----	----	----



j

i

7	14	26	12
---	----	----	----

- Pivot value = 7
- $14 \geq 7 \geq 7$. swap
- $i > j$, stop partition
- run quicksort recursively

QUICKSORT

14	26	12
----	----	----



pivot value

14	26	12
----	----	----



i

j

14	12	26
----	----	----



j

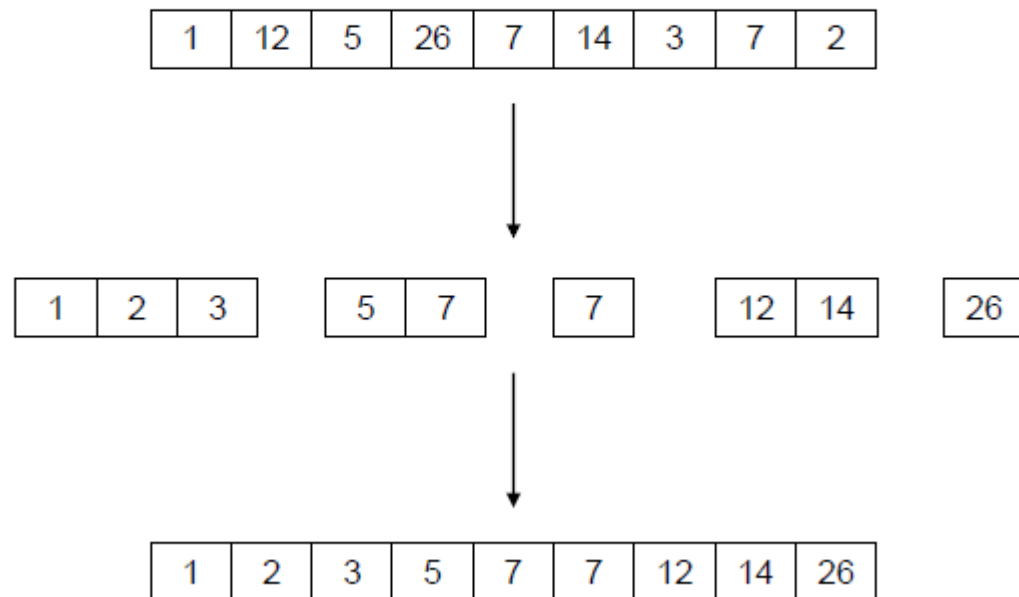
i

14	12	26
----	----	----

12	14	26
----	----	----

- Pivot value = 26
- $26 \geq 26 \geq 12$. swap
- $i > j$, stop partition
- run quicksort recursively

QUICKSORT



```
1. void quickSort(int arr[], int left, int
   right) {
2.     int i = left, j = right;
3.     int tmp;
4.     int pivot = arr[(left + right) / 2];
5.
6.     /* partition */
7.     while (i <= j) {
8.         while (arr[i] < pivot)
9.             i++;
10.        while (arr[j] > pivot)
11.            j--;
12.
```

```
13.         if (i <= j) {
14.             tmp = arr[i];
15.             arr[i] = arr[j];
16.             arr[j] = tmp;
17.             i++;
18.             j--;
19.         }
20.     };
21.
22.     /* recursion */
23.     if (left < j)
24.         quickSort(arr, left, j);
25.     if (i < right)
26.         quickSort(arr, i, right);
27. }
```