Greedy Algorithm

Greedy algorithm is an algorithm technique which always takes the best immediate, or local, solution while finding an answer.

It is a mathematical process that looks for simple, easy-to-implement solutions to complex, multi-step problems by deciding which next step will provide the most obvious benefit (perhaps why it is called greedy).

Greedy is a strategy to solve the complex problem or you can say optimization problem in simple and quicker way. This strategy has following to characteristics

- 1. Greedy-choice property: A global optimum can be arrived at by selecting a local optimum.
- 2. Optimal substructure: An optimal solution to the problem contains an optimal solution to sub problems.

Below is the list of famous greedy algorithms:

- -Prism's algorithm
- -Kruskal algorithm
- -Reverse-Delete algorithm
- -Dijkstra's algorithm
- -Huffman coding

EXAMPLE PROBLEM: ACTIVITY SELECTION PROBLEM (Activity selection problem is an example of greedy algorithm)

An activity-selection is the problem of scheduling a resource among several competing activity. Given M activities with their start and finish times, we have to find the maximum number of activities that can be performed by a single person, assuming that a person can only work on a single activity at a time.

GREEDY ALGO STEPS

- a) Sort the activities according to their finishing time
- b) Select the first activity from the sorted array and print it.
- c) Do following for remaining activities in the sorted array.
- d) If the start time of this activity is greater than the finish time of previously selected activity then select this activity and print it.

Consider the following 6 activities.

```
s_time[] = {1, 3, 0, 5, 3, 5, 6, 8, 8, 2}; // start time
f_time[] = {4, 5, 6, 7, 9, 9, 10, 11, 12, 18}; // finish time,
```

```
#include
void Activities(int s_time[], int f_time[], int n)
{
int i, j;
printf ("Selected Activities are:");
i = 1; printf("A%d ", i);
for (j = 1; j < n; j++) {
if (s_time[j] >= f_time[i]) {
printf ("A%d ", j+1); i = j;
}
int main() {
int s_time[] = {1, 3, 0, 5, 3, 5, 6, 8, 8, 2};
int f_time[] = {4, 5, 6, 7, 9, 9, 10, 11, 12, 18};
int n = sizeof(s_time)/sizeof(s_time[0]);
Activities(s, f, n);
return 0;
```

Example (that works) -Huffman code

Computer Data Encoding:

How do we represent data in binary?

Historical Solution:

Fixed length codes.

Encode every symbol by a unique binary string of a fixed length.

Examples: ASCII (7 bit code), EBCDIC (8 bit code), ...

American Standard Code for Information Interchange

b ₇ —				-		0 0	0 0	0 1	0 1	1 0	1 0	1 1	1 1
b ₁	_				-	. 0	1	. 0	1	0	1	. 0	1
Bits	p*	b₃ ⊥	b ₂ ↓	b ₁	CORATO Nov 1	0	1	2	3	4	5	6	7
	0	0	0	0	0	NUL	DLE	SP	0	@	Р	•	р
	0	0	0	1	1	SOH	DC1	- 1	1	Α	Q	a	q
	0	0	1	0	2	STX	DC2		2	В	R	ь	r
	0	0	1	1	3	ETX	DC3	H	3	C	S	С	S
	0	1	0	0	4	EOT	DC4	\$	4	D	T	d	t
	0	1	0	1	5	ENQ	NAK	%	5	Ε	U	e	u
	0	1	1	0	6	ACK	SYN	8.	6	F	V	f	٧
	0	1	1	1	7	BEL	ETB		7	G	W	g	W
	1	0	0	0	8	BS	CAN	(8	Н	X	h	X
	1	0	0	1	9	HT	EM)	9	- 1	Y	į.	У
	1	0	1	0	10	LF	SUB	•	:	J	Z	j	2
	1	0	1	1	11	VT	ESC	+	i i	K]	k	{
	1	1	0	0	12	FF	FC		<	L	1	- 1	
	1	1	0	1	13	CR	GS	-	=	M]	m	}
	1	1	1	0	14	SO	RS		>	N	Α	n	~
	1	1	1	1	15	SI	US	- 1	?	0	_	0	DEL

ASCII Example:

bs —				•	→,	0 0	0 1	1 0	0 1 1	1 0 0	1 0 1	1 1 0	1 1
Bits	b ₄	b₃ ↓	b₂ ↓	b₁ ↓	Course Nov:	0	1	2	3	4	5	6	7
	0	0	0	0	0	NUL	DLE	SP	0	@	P		P
	0	0	0	1	1	SOH	DC1	- 1	1	Α	Q	а	q
[0	0	1	0	2	STX	DC2	-	2	В	R	b	г
[0	0	1	1	3	ETX	DC3	Ħ	3	С	S	С	s
[0	1	0	0	4	EOT	DC4	\$	4	D	Т	d	t
[0	1	0	1	5	ENQ	NAK	%	5	E	U	e	u
[0	1	1	0	6	ACK	SYN	&	6	F	V	f	V
[0	1	1	1	7	BEL	ETB		7	G	W	g	W
	1	0	0	0	8	BS	CAN	(8	Н	X	h	X
[1	0	0	1	9	HT	EM)	9	- 1	Y	i.	У
[1	0	1	0	10	LF	SUB		- :	J	Z	j	Z
	1	0	1	1	11	VT	ESC	+	;	K	1	k	-{
[1	1	0	0	12	FF	FC		<	L	1	1	
	1	1	0	1	13	CR	GS	-	=	M	1	m	}
	1	1	1	0	14	SO	RS		>	N	Α.	n	~
	1	1	1	1	15	SI	US	1	?	0	_	0	DEL

AABCAA

A A B C A A 1000001 1000001 1000010 1000011 1000001

Total space usage in bits:

Assume an & bit fixed length code.

For a file of n characters

Need not bits.

Variable Length codes

Idea: In order to save space, use less bits for frequent characters and more bits for rare characters.

Example: suppose alphabet of 3 symbols: { A, B, C }.
suppose in file: 1,000,000
characters.
Need 2 bits for a fixed length
code for a total of
2,000,000 bits.

Variable Length codes - example

Suppose the frequency distribution of the characters is:

А	В	С		
999,000	500	500		

Encode:

Α	В	С
0	10	11

Note that the code of A is of length 1, and the codes for B and C are of length 2

Total space usage in bits:

Fixed code: $1,000,000 \times 2 = 2,000,000$

```
Varable code: 999,000 x 1
+ 500 x 2
500 x 2
```

1,001,000

A savings of almost 50%

How do we decode?

In the fixed length, we know where every character starts, since they all have the same number of bits.

0000010101010100100001010 A A A B B C C C B C B A A C C

How do we decode?

In the variable length code, we use an idea called Prefix code, where no code is a prefix of another.

None of the above codes is a prefix of another.

How do we decode?

```
Example: A = 0
B = 10
C = 11
```

So, for the string:
AAABBCCCBCBAACC the encoding:

0 0 010101111111101110 0 01111

Prefix Code

Decode the string

AAABBCCCBCBAACC

Desiderata:

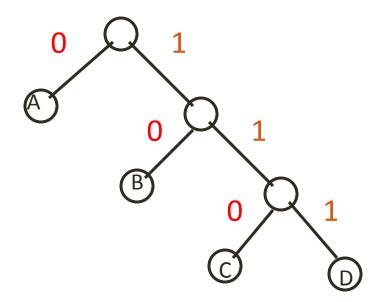
Construct a variable length code for a given file with the following properties:

- 1. Prefix code.
- 2. Using shortest possible codes.
- 3. Efficient.
- 4. As close to entropy as possible.

Idea

Consider a binary tree, with:

- 0 meaning a left turn
- 1 meaning a right turn.



Idea

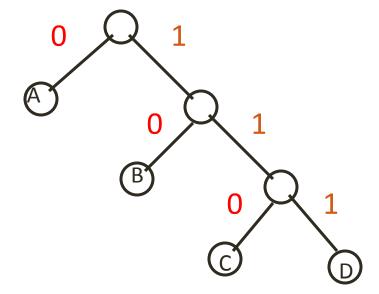
Consider the paths from the root to each of the leaves A, B, C, D:

A:0

B:10

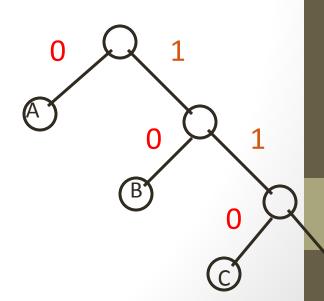
C:110

D: 111



Observe:

- 1. This is a prefix code, since each of the leaves has a path ending in it, without continuation.
- 2. If the tree is full then we are not "wasting" bits.
- 3. If we make sure that the more frequent symbols are closer to the root then they will have a smaller code.



Greedy Algorithm:

- 1. Consider all pairs: <frequency, symbol>.
- 2. Choose the two lowest frequencies, and make them brothers, with the root having the combined frequency.
- 3. Iterate.

Greedy Algorithm Example:

Alphabet: A, B, C, D, E, F

Frequency table:

Α	В	С	D	Е	F
10	20	30	40	50	60

Total File Length: 210

A 10

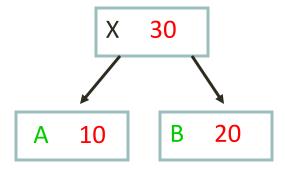
B 20

C 30

D 40

E 50

60

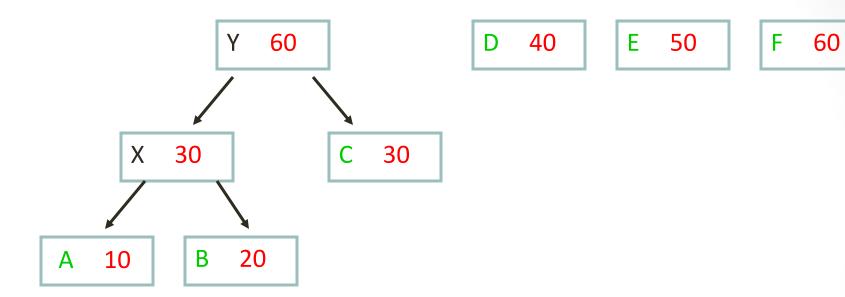


D 40

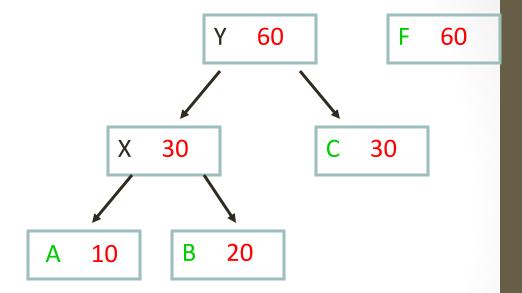
30

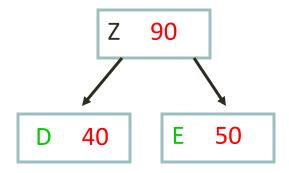
E 50

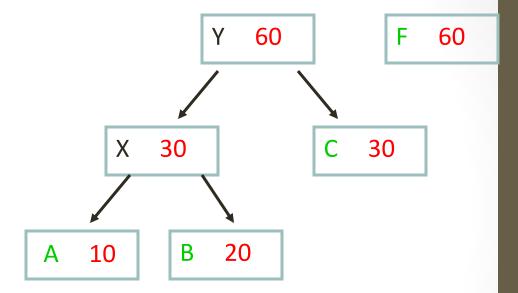
60

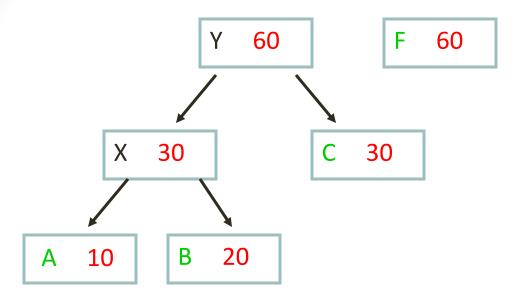


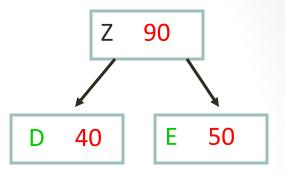


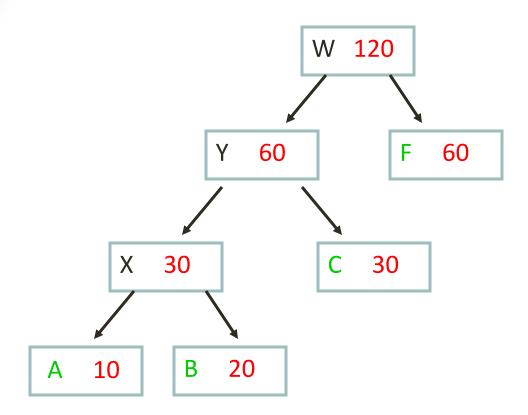


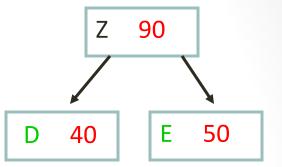


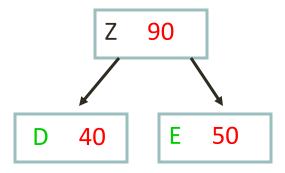


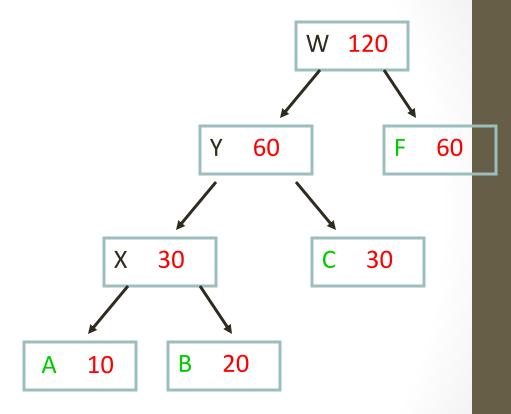


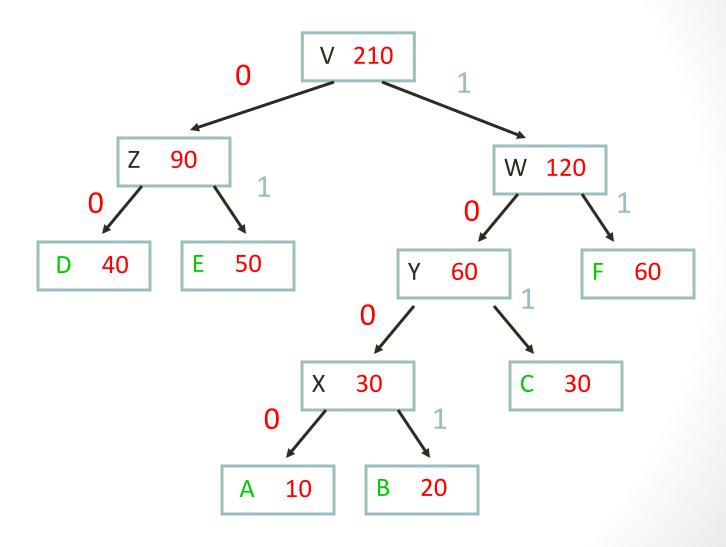












The Huffman encoding:

A: 1000

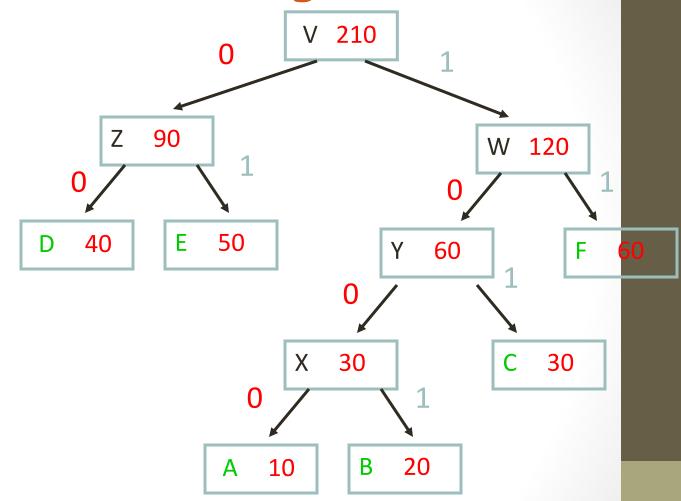
B: 1001

C: 101

D: 00

E: 01

F: 11



File Size: 10x4 + 20x4 + 30x3 + 40x2 + 50x2 + 60x2 =40 + 80 + 90 + 80 + 100 + 120 = 510 bits

Note the savings:

The Huffman code: Required 510 bits for the file.

Fixed length code:

Need 3 bits for 6 characters. File has 210 characters.

Total: 630 bits for the file.

Note also:

For uniform character distribution:

The Huffman encoding will be equal to the fixed length encoding.

Why?

Assignment.