## Integer Functions and Elementary Number Theory

## January 31, 2021

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\lfloor x \rfloor = the greatest integer less than or equal to x (the floor of x).
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[x] = the smallest integer greater than or equal to x (the ceiling of x).

 $\lfloor x \rfloor = \lceil x \rceil$  if and only if x is integer.

 $\lceil x \rceil = 1 + \lfloor x \rfloor$  if and only if x is not an integer.

$$\lfloor -x \rfloor = -\lceil x \rceil; \, x-1 < \lfloor x \rfloor \leq x \leq \lceil x \rceil < x+1$$

Congruence

 $x \equiv y \pmod{z}$ 

 $x\perp y$ x and y are relatively prime. i.e gcd is 1.

The 4 Laws.