

25. Kruskal's Algorithm (Minimum Spanning Tree)

Aim:

To find MST using Kruskal's algorithm.

Algorithm:

1. Sort all edges by weight.
2. Pick the smallest edge that does not form a cycle (using Union-Find).
3. Repeat until MST has $(V-1)$ edges.

CODE:

```
#include <stdio.h>
#define MAX 20

int parent[MAX];

int find(int i) {
    while (parent[i] != i)
        i = parent[i];
    return i;
}

void unionSet(int i, int j) {
    int a = find(i);
    int b = find(j);
    parent[a] = b;
}

void kruskal(int n, int cost[MAX][MAX]) {
    int mincost = 0, edge_count = 0;
    for (int i = 0; i < n; i++) parent[i] = i;

    printf("Edge : Weight\n");
```

```

while (edge_count < n - 1) {
    int min = 9999, a = -1, b = -1;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if (find(i) != find(j) && cost[i][j] < min) {
                min = cost[i][j];
                a = i;
                b = j;
            }
        }
    }
    unionSet(a, b);
    printf("%d - %d : %d\n", a, b, min);
    mincost += min;
    edge_count++;
}
printf("Minimum Cost: %d\n", mincost);
}

int main() {
    int n, cost[MAX][MAX];
    printf("Enter number of vertices: ");
    scanf("%d", &n);
    printf("Enter cost adjacency matrix (9999 if no edge):\n");
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            scanf("%d", &cost[i][j]);

    kruskal(n, cost);
    return 0;
}

```

Output

```
Enter number of vertices: 4
Enter cost adjacency matrix (9999 if no edge):
9999 10 6 5
10 9999 9999 15
6 9999 9999 4
5 15 4 9999
Edge : Weight
2 - 3 : 4
0 - 3 : 5
0 - 1 : 10
Minimum Cost: 19

=== Code Execution Successful ===
```

RESULT:

The program successfully executed and displayed the Kruskal's Algorithm.