

chapter - 2

⑩ program to handle different type of lists

Aim:

To Write a program that correctly processes

- An empty List
- A List with one element
- A List with all identical elements
- A List with negative numbers

* Pseudocode

Start

Read List A

$n = \text{Length of A}$

If $n \leq 1$

print A

else

Sort A in ascending order

print A

ENDIF

STOP

* Test cases

Input

[]

[1]

[7, 7, 7, 7]

[-5, -1, -3, -2, -4]

Output

[]

[1]

[7, 7, 7, 7]

[-5, -4, -3, -2, -1]

⑪ Aim

Selection Sort

To Sort a given array of elements in ascending order using Selection Sort Algorithm

Pseudocode

Start

Read n

Read array A[n]

for $i = 0$ to $n - 2$

min = i

for $j = i + 1$ to $n - 1$

If $A[j] < A[\text{min}]$

min = j

END If

END For

SWAP A[i] and A[min]

end for

Print A

STOP

* Input

[5, 2, 9, 1, 5, 6]

* output

[1, 2, 5, 5, 6, 9]

⑩ Bubble Sort

Aim:

To sort a list of elements in ascending order using Bubble Sort

* pseudocode

Start

Read n

Read array A[n]

for i = 0 to n-2

Swapped = 0

for j = 0 to n-i-2

if A[j] > A[j+1]

Swap A[j], A[j+1]

Swapped = 1

end if

end for

if Swapped = 0

Break

end if

end for

print A

Stop

* Input

[5, 1, 4, 2, 8]

* output

[1, 2, 4, 5, 8]

(2)

TEST CASES:

Insertion Sort

Aim:

To implement insertion sort that correctly sorts an array containing duplicate elements and to study its behaviour

* pseudocode:

InsertionSort (A, n)

```
{
  for i = 1 to n-1
  { key = A[i];
    j = i-1;
    while (j >= 0 && A[j] > key)
```

```
    { A[j+1] = A[j];
```

```
      j = j-1;
```

```
    A[j+1] = key;
```

* Input

[64, 25, 12, 22, 11]

[29, 10, 14, 31, 13]

[3, 5, 2, 1, 4]

[1, 2, 3, 4, 5]

(Already Sorted)

[5, 4, 3, 2, 1]

(Reverse Sorted)

(2) Array with duplicates

Input:

[3, 1, 4, 1, 5, 9, 2, 6, 8, 3]

Output:

[1, 1, 2, 3, 3, 4, 5, 6, 8, 9]

(3) ALL Identical Elements

Input:

[5, 5, 5, 5, 5]

Output:

[5, 5, 5, 5, 5]

output

[11, 12, 22, 25, 64]

[10, 13, 14, 29, 31]

[1, 2, 3, 4, 5]

[1, 2, 3, 4, 5]

[1, 2, 3, 4, 5]

(22)

Kth missing positive integer

Aim:

To find the Kth missing positive integer from a given array of strictly increasing positive integers

* Pseudocode:

findKthPositive(arr, n, k)

left = 0;

right = n-1;

while (left <= right)

mid = (left + right) / 2;

missing = arr[mid] - (mid + 1);

if (missing < k)

left = mid + 1;

else

right = mid - 1;

return k + left;

* Input

arr = [2, 3, 4, 7, 11]

k = 5

* output

output: 9

(23)

peak elementAim: To find the index of a peak element in a given 0-indexed integer array using an $O(\log n)$ time complexity algorithm.

* Pseudocode:

findPeakElement(nums, n)

low = 0;

high = n-1;

while (low < high)

mid = (low + high) / 2;

if (nums[mid] < nums[mid + 1])

low = mid + 1;

else

high = mid;

return low;

* Input:

nums = [1, 2, 3, 1]

* Output:

Output: 2

(24)

Index of first occurrence

Aim:

to find the index of the first occurrence of the string needle in the string haystack.

If needle is not present, return -1.

* Pseudocode

Stringer (haystack, needle)

{
 n = Length(haystack);

 m = Length(needle);

 if (m == 0)

 return 0;

 for i = 0 to n - m {

 j = 0;

 while (j < m && haystack[i + j] == needle[j])

 j++;

 if (j == m)

 return i;

 return -1;

}

* Inputs

haystack = "sad but sad"

needle = "sad"

* Output

output: 0

(27)

Given an array of string words, return all strings in words that is a substring of another word.

Aim: To find and return all strings from given array that are substrings of another string in the same array

* Pseudocode:

findSubstrings(words, n) {

 result = empty List;

 for i = 0 to n - 1 {

 for j = 0 to n - 1 {

 if (i != j && isSubstring(words[i], words[j]))

 add words[i] to result;

 break

```

    }
    }
    return result;
}

```

Q8. Brute force approach

Aim: Find the closest pair of points in a set of 2D points using the brute force method.

* Pseudocode

```

closestPair(points, n)
{
    minDist = INFINITY;
    for i = 0 to n-2 {
        for j = i+1 to n-1 {
            dist = sqrt((points[i].x - points[j].x)^2 + (points[i].y - points[j].y)^2);
            if (dist < minDist) {
                minDist = dist;
                P1 = points[i];
                P2 = points[j];
            }
        }
    }
}

```

print P1, P2, minDist;

* Input

points = [(1, 2), (4, 7), (7, 8), (3, 1)]

* Output

Closest pair: (1, 2) & (3, 1)

minimum distance: 1.414213562373095

Closest pair of points (Brute force)Aim:

To find the closest pair of points in a given set of 2D points using the brute force approach and analyze its time complexity

Euclidean distance = function

$$\text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

* pseudocode:distance (P₁, P₂)

```

{
    return sqrt ((P1.x - P2.x) * (P1.x - P2.x) + (P1.y -
    P2.y) * (P1.y - P2.y));
}

```

closest pair (points, n)

```

{
    minDist = Infinity;

```

```

    for i = 0 to n-2

```

```

        {
            for j = i+1 to n-1

```

```

                {
                    d = distance (points[i], points[j]);

```

```

                    if (d < minDist) {
                        minDist = d;

```

```

                        P1 = points[i];

```

```

                        P2 = points[j];
                    }
                }
            }
        }
    }
}

```

```

print P1, P2, minDist;
}

```

* Input

points = [(1, 2), (4, 5), (7, 8), (3, 1)]

* Output

Closest pair : (1, 2) - (3, 1)

minimum distance : 1.4142135623730951

Aim:

To write a program that finds the convex hull of a given set of 2D using the brute force approach

* Pseudocode

```

for each point i in points
  foreach point j in points
    if i != j
      pos = neg = 0
      for each point k in points
        val = cross-product(i, j, k)
        if val > 0 then pos++
        else if val < 0 then neg++
      if pos == 0 or neg == 0
        mark i and j as hull points
print hull points in counter-clockwise order

```

* Input

points = [(1,1), (4,6), (8,1), (0,0), (3,3)]

* output

Convex Hull = [(0,0), (1,1), (8,1), (4,6)]

Travelling SalesmanAim:

To develop a program that solves the Travel Salesman problem (TSP) using an exhaustive Search (brute force) approach by generating all possible permutations of cities and find the shortest possible tour

* Pseudocode

```

function tsp(cities, n)
  start = cities[0]
  mindist = INFINITY
  for each permutation P of cities(1 to n-1)
    dist = 0
    curr = start
    for each city in P

```


dist + = distance(curr, city)

curr = city

dist + = distance(curr, start)

if dist < mindist

mindist = dist

bestpath = (start, p, start)

return mindist, bestpath

* Input:

cities = [(1, 2), (4, 5), (7, 1), (3, 6)]

* Output

shortest distance: 7.0710678118654755

shortest path: [(1, 2), (4, 5), (7, 1), (3, 6), (1, 2)]

30

Assignment problem

Aim: To develop a program that solves the Assignment problem using an Exhaustive (brute force) Search approach by checking all possible worker task

* pseudocode

function total-cost (assign, cost, n)

Sum = 0

for i = 0 to n-1

Sum + = cost[i][assign[i]]

return Sum

function assignment-problem (cost, n)

mincost = INFINITY

for each permutation p of tasks 0 to n-1

Currcost = total-cost (p, cost, n)

if Currcost < mincost

mincost = Currcost

bestAssign = p

return bestAssign, mincost

* Input

Cost matrix =

[[3, 10, 7],

[8, 8, 12],

[4, 6, 9]]

* Output

Optimal assignment:

[(worker 1, task 2), (worker 2, task 1), (worker 3, task 3)]

Total cost: 19

Knapsack using Exhaustive SearchAim:

To develop a program that solves the 0-1 Knapsack problem using Exhaustive Search.

* procedure:* pseudocode:

max = 0

for each subset S of items

if weight(S) \leq Capacity

if value(S) > max

max = value(S)

best = S

return best, max

* Input

Items: 3

weights: [2, 3, 1]

values: [4, 5, 3]

Capacity: 4

* output

optimal Selection: [0, 2]

Total value: 7