

# Data Science Inference and Modeling

The textbook for the Data Science course series is [freely available online](#).

## Learning Objectives

- The concepts necessary to define estimates and margins of errors of populations, parameters, estimates, and standard errors in order to make predictions about data
- How to use models to aggregate data from different sources
- The very basics of Bayesian statistics and predictive modeling

## Course Overview

### Section 1: Parameters and Estimates

You will learn how to estimate population parameters.

### Section 2: The Central Limit Theorem in Practice

You will apply the central limit theorem to assess how close a sample estimate is to the population parameter of interest.

### Section 3: Confidence Intervals and p-Values

You will learn how to calculate confidence intervals and learn about the relationship between confidence intervals and p-values.

### Section 4: Statistical Models

You will learn about statistical models in the context of election forecasting.

### Section 5: Bayesian Statistics

You will learn about Bayesian statistics through looking at examples from rare disease diagnosis and baseball.

### Section 6: Election Forecasting

You will learn about election forecasting, building on what you've learned in the previous sections about statistical modeling and Bayesian statistics.

## Section 7: Association Tests

You will learn how to use association and chi-squared tests to perform inference for binary, categorical, and ordinal data through an example looking at research funding rates.

### Section 1 Overview

Section 1 introduces you to parameters and estimates.

After completing Section 1, you will be able to: - Understand how to use a sampling model to perform a poll. - Explain the terms population, parameter, and sample as they relate to statistical inference. - Use a sample to estimate the population proportion from the sample average. - Calculate the expected value and standard error of the sample average.

The textbook for this section is available [here](#)

### Assessment 1.1: Parameters and Estimates

#### 1. Polling - expected value of $S$

Suppose you poll a population in which a proportion  $p$  of voters are Democrats and  $1-p$  are Republicans. Your sample size is  $N=25$ . Consider the random variable  $S$ , which is the total number of Democrats in your sample.

What is the expected value of this random variable  $S$ ?

Possible Answers - ☐ A.  $E(S)=25(1-p)$  - ☒ B.  $E(S)=25p$  - ☐ C.  $E(S)=\sqrt{(25p(1-p))}$  - ☐ D.  $E(S)=p$

#### 2. Polling - standard error of $S$

Again, consider the random variable  $S$ , which is the total number of Democrats in your sample of 25 voters. The variable  $p$  describes the proportion of Democrats in the sample, whereas  $1-p$  describes the proportion of Republicans.

What is the standard error of  $S$ ?

Possible Answers - ☐ A.  $SE(S)=25p(1-p)$  - ☐ B.  $SE(S)=\sqrt{25p}$  - ☐ C.  $SE(S)=25(1-p)$  - ☒ D.  $SE(S)=\sqrt{(25p(1-p))}$

#### 3. Polling - expected value of $\bar{X}$

Consider the random variable  $\bar{X}$ , which is equivalent to the sample average that we have been denoting as  $\bar{X}$ . The variable  $N$  represents the sample size and  $p$  is the proportion of Democrats in the population.

What is the expected value of  $\bar{X}$ ?

Possible Answers - ☒ A.  $E(\bar{X})=p$  - ☐ B.  $E(\bar{X})=Np$  - ☐ C.  $E(\bar{X})=N(1-p)$  - ☐ D.  $E(\bar{X})=1-p$

#### 4. Polling - standard error of $\bar{X}$

What is the standard error of the sample average,  $\bar{X}$ ?

The variable  $N$  represents the sample size and  $p$  is the proportion of Democrats in the population.

Possible Answers - ☐ A.  $SE(\bar{X})=\sqrt{(Np(1-p))}$  - ☒ B.  $SE(\bar{X})=\sqrt{(p(1-p)/N)}$  - ☐ C.  $SE(\bar{X})=\sqrt{(p(1-p))}$  - ☐ D.  $SE(\bar{X})=\sqrt{N}$