

# Bayesian data analysis – Assignment 2

## General information

- The recommended tool in this course is R (with the IDE R-Studio). You can download R [here](#) and R-Studio [here](#). There are tons of tutorials, videos and introductions to R and R-Studio online. You can find some initial hints [here](#).
- The format of the report should follow the instruction in the R markdown template that can be found at [here](#).
- Report all results in a single, **anonymous** \*.pdf -file and return it to [peergrade.io](#).
- Many of the exercises can be checked using the R package `markmyassignment`. Information on how to install and use the package can be found [here](#).
- The course has its own R package with data and functionality to simplify coding. To install the package just run the following:

```
1. install.packages("devtools")  
2. devtools::install_github("avehtari/BDA_course_Aalto",  
  subdir = "rpackage")
```

- Many of the exercises can be checked automatically using the R package `markmyassignment`. Information on how to install and use the package can be found [here](#).
- Additional self study exercises and solutions for each chapter in BDA3 can be found [here](#).
- If you have any suggestions or improvements to the course material, please feel free to submit a Pull Request to the public repository!

## Information on this assignment

This exercise is related to Chapters 1 and 2. The maximum amount of points from this assignment is 3. You may find an additional discussion about choosing priors by Andrew Gelman useful, they can be found [here](#).

**Reading instructions:** Chapter 1 and 2 in BDA3, see [here](#) and [here](#).

**Grading instructions:** The grading will be done in peergrade. All grading questions and evaluations for assignment 2 can be found [here](#)

To use `markmyassignment` for this assignment, run the following code in R:

```
> library(markmyassignment)  
> exercise_path <-  
  "https://github.com/avehtari/BDA_course_Aalto/blob/master/exercises/tests/ex2.yml"  
> set_assignment(exercise_path)
```

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## Inference for binomial proportion (Computer)

Algae status is monitored in 274 sites at Finnish lakes and rivers. The observations for the 2008 algae status at each site are presented in file `algae.txt` ('0': no algae, '1': algae present). The data can also be accessed from the `aaltobda` R package as follows:

```
> library(aaltobda)
> data("algae")
> head(algae)

[1] 0 1 1 0 0 0
```

Let  $\pi$  be the probability of a monitoring site having detectable blue-green algae levels.

Use a binomial model for observations and a  $\text{Beta}(2, 10)$  prior for  $\pi$  in Bayesian inference. Formulate Bayesian model likelihood  $p(y|\pi)$ , prior  $p(\pi)$ , and the resulting posterior  $p(\pi|y)$ . Here it is not necessary to derive the posterior distribution as it has already been done in the book. Also, it is not necessary to write out the distributions; it is sufficient to use label-parameter format, e.g.  $\text{Beta}(\cdot, \cdot)$ . Although recommended, any plotting is not required in this exercise.

As a test case, we provide some results for the following data. It is also possible to check the functions below with `markmyassignment`.

```
> algea_test <- c(0, 1, 1, 0, 0, 0)
```

Use your model to answer the following questions:

- a) What can you say about the value of the unknown  $\pi$  according to the observations and your prior knowledge? Summarize your results with a point estimate (i.e.  $E(\pi|y)$ ) and a 90% interval estimate.

```
> beta_point_est(prior_alpha = 2, prior_beta = 10, data = algea_test)

[1] 0.2222222

> beta_interval(prior_alpha = 2, prior_beta = 10, data = algea_test, prob = 0.9)

[1] 0.06810774 0.43431787
```

- b) What is the probability that the proportion of monitoring sites with detectable algae levels  $\pi$  is smaller than  $\pi_0 = 0.2$  that is known from historical records?

```
> beta_low(prior_alpha = 2, prior_beta = 10, data = algea_test, pi_0 = 0.2)

[1] 0.1382122
```

- c) What assumptions are required in order to use this kind of a model with this type of data?
- d) Make prior sensitivity analysis by testing a couple of different reasonable priors. Summarize the results by one or two sentences.

**Hint!** With a conjugate prior, a closed-form posterior is Beta form (see equations in the book). Useful functions: `dbeta`, `pbeta`, `qbeta` in R.