# Research Shell

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## Overview

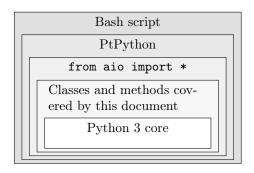
The Research Shell is in fact a Python3 shell wrapped by PtPython with some useful modules, classes and methods included. This document covers those items assuming, that a reader is familiar with Python syntax.

#### 1.1 Architecture of Research Shell

Look at Figure 1.1. It shows Research Shell wrappers from the top to the Python3 core. User calls a Bash script, which prepares and executes a command containing Python3 call, module PtPython loading, and then importing all useful libraries included in module aio. So to run the Research Shell you need to call:

#### research\_shell [python\_file\_name\_to\_execute]

If no argument, then the Research Shell appears and is ready to execute Python commands. If a script file is specified as an argument, then its content is executed after importing all modules and the shell closes.



 ${\bf Figure~1.1:~Research~Shell architecture.}$ 

There is also a special mode of Research Shell, called **Testcase Mode**. It makes easy to execute a complete testcases. The testcase is a directory having a regular structure:

testcase_name,	
data/	automatically added to the searching path
results/ .	
driver.py	

By running the command:

#### research\_shell\_drun

the Research Shell runs in the Testcase mode. In such case it checks if the driver.py file exists. If so, then it removes and recreates the results directory and goes there (so results is now the Current Directory). Now, a content of dirver.py is executed. In results directory a transcript.txt is created. To print something to the screen and also to the transcript file, you need to call the print(\*args) method of class Aio, i.e.:

# This text will be printed to the screen only:

```
print("Text on the screen only")
# This also appears in the transcript file:
Aio.print("Text on the screen and in the transcript")
```

### 1.2 Getting started with Research Shell in Siemens' infrastructure

There is a very simple way to start using the Research Shell having access to Siemens' infrastructure. First, login to any remote machine. Then, clone the *research* git repository:

```
git clone /wv/stsgit/research.git
```

After that, the following tree will be created in your Current Dir:

research/

Note: It is recommended to add the ./research/research\_shell/bin directory to your PATH environmental variable, but is not necessary to use the Research Shell.

To make sure you have all required Python modules installed and to install the missing ones, just run the script from utils directory:

```
bash ./research/research_shell/utils/install_python_libs
```

Once the script finishes, you can easy call the Research Shell:

```
./research/research_shell/bin/research_shell
```

The PTPython (Python) shell will appear. See next chapters to getting familiar with research-related modules, classes and functions, you can use together with standard Python ones in the Research Shell.

#### 1.2.1 Verifying the Research Shell installation

There is a testcase called research\_shell\_verifier especially usable to make sure, that all dependencies are installed correctly and if there is no error in core research procedures, like those ones to primitive polynomials searching, LFSR simulators etc. Tp run that testcase (as well as any other one), simply go to the main testcase directory:

```
\ensuremath{\mathsf{cd}} ./research/testcases/research_shell_verifier and call:
```

```
../../research_shell/bin/research_shell_drun
```

You can see a standard output stream printed on your screen during execution. Once finished, the transcript is available in ./results/transcript.txt file.

# Class Polynomial

Polynomial is an object intended to analyze polynomials over GF(2). An object of type Polynomial holds polynomial coefficients (as a list of positive integers) and a list of signs of those coefficients. Of course in case of GF(2) coefficient  $x_i = -x_i$ . However, negative coefficients make sense in case of some types of LFSRs, as Polynomial objects are used to create other objects, of type of Lfsr.

Below you can see an example of how to create a Polynomial object representing the polynomial of  $x^{16} + x^5 + x^2 + x^0$ :

Polynomial class includes also a couple of static methods, especially useful to search for primitive polynomials and other ones discussed in the next part of this chapter.

### 2.1 Polynomial object methods

```
Polynomial_object.__str__()
     Polynomial objects are convertible to strings.
     p1 = Polynomial ( [16, 5, 2, 0] )
     print (p1)
    \# >>> [16, 5, 2, 0]
Polynomial_object.__hash__()
     Polynomial objects are hashable. Can be used as dictionary keys.:
    p1 = Polynomial ( [16, 5, 2, 0] )
    d = \{\}
    d[p1] = "p1 value"
Polynomial_object.copy()
     Returns a deep copy of the Polynomial object.
     p1 = Polynomial ( [16, 5, 2, 0] )
    p2 = p1.copy()
     \mathbf{print}(p1 = p2)
    # >>> True
```

Returns symbolic derivative Polynomial.

```
\begin{array}{lll} p1 &= \mathbf{Polynomial} & ( & [16\,,\ 15\,,\ 2\,,\ 1\,,\ 0 ] &) \\ \mathbf{print} & (p1\,.\,derivativeGF2\,()) \\ \# >>> & [14\,,\ 0] \\ p2 &= \mathbf{Polynomial} & ( & [16\,,\ 14\,,\ 5\,,\ 2\,,\ 0] &) \\ p3 &= & p2\,.\,derivativeGF2\,() \\ \mathbf{print}\,(p3) \\ \# >>> & [4\,] \end{array}
```

#### Polynomial\_object.getBalancing()

Returns a difference between distances of furthest and closest coefficients.

#### Polynomial\_object.getCoefficients()

Returns a reference to the sorted list of (unsigned) coefficients.

```
\begin{array}{lll} \mathtt{p1} &= \mathbf{Polynomial} & ( & [16\,,\ 2\,,\ -5,\ 0] &) \\ \mathbf{print} & (\mathtt{p1.getCoefficients} & ()) \\ \# >>> & [16\,,\ 5\,,\ 2\,,\ 0] \end{array}
```

#### Polynomial\_object.getCoefficientsCount()

Returns count of the Polynomial object coefficients.

```
\begin{array}{lll} p1 &= \textbf{Polynomial} & ( & [16\,, & 5\,, & 2\,, & 0] & ) \\ coeffscount1 &= & p1\,.\,getCoefficientsCount\,() \\ \textbf{print}\,(\,coeffscount1\,) \\ \#>>> & 4 \end{array}
```

#### Polynomial\_object.getDegree()

Returns degree of the Polynomial object.

```
p1 = Polynomial ( [16, 5, 2, 0] )
deg1 = p1.getDegree()
print(deg1)
# >>> 16
```

#### Polynomial\_object.getDifferentTapCount(AnotherPolynomial)

Imagine, that the Polynomial\_object is a characteristic polynomial of a Ring Generator. Then this method compares the Polynomial\_object with another polynomial (also being a characteristic one of a Ring Generator) and returns a number of NOT matching taps. Tap direction (given by coefficient sign) does not matter.

```
\begin{array}{lll} p1 &= \textbf{Polynomial} & ( & [16\,,\,\,-5,\,\,2\,,\,\,0] & ) \\ p2 &= \textbf{Polynomial} & ( & [16\,,\,\,5\,,\,\,2\,,\,\,0] & ) \\ p3 &= \textbf{Polynomial} & ( & [16\,,\,\,5\,,\,\,1\,,\,\,0] & ) \\ p4 &= \textbf{Polynomial} & ( & [16\,,\,\,6\,,\,\,0] & ) \\ p1\,.\,getDifferentTapCount\,(p2) \\ \#>>> 0 \end{array}
```

```
p1.getDifferentTapCount(p3)

# >>> 1

p1.getDifferentTapCount(p4)

# >>> 2

p4.getDifferentTapCount(p1)

# >>> 1
```

#### Polynomial\_object.getMinDistance()

Returns a distance between closest Polynomial's coefficients.

```
\begin{array}{lll} p1 &= & \textbf{Polynomial} & ( & [16\,, \,\, 5\,, \,\, 2\,, \,\, 0] & ) \\ \# & & \text{distances}: & 11 & 3 & 2 \\ p1.\, getMinDistance\,() & & & \\ \# >>> & 2 & & \end{array}
```

#### Polynomial\_object.getReciprocal()

Returns a new, reciprocal Polynomial object.

```
p1 = Polynomial ( [16, 5, 2, 0] )

print(p1.getReciprocal())

\#>>> [16, 14, 11, 0]
```

#### Polynomial\_object.getSignedCoefficients()

Returns sorted list of signed coefficients.

```
\begin{array}{lll} p1 &= \textbf{Polynomial} & ( & [16\,,\ 2\,,\ -5,\ 0] \\ \textbf{print} & (p1.\,getSignedCoefficients\,()) \\ \# >>> & [16\,,\ -5,\ 2\,,\ 0] \end{array}
```

#### Polynomial\_object.getSigns()

Returns signs of all sorted coefficients (as a list of 1s and -1s).

```
p1 = Polynomial ( [16, -5, 2, 0] )

print(p1.getSigns())

# >>> [1, -1, 1, 1]
```

#### Polynomial\_object.isLayoutFriendly()

Returns True if a Ring Generator, based on the Polynomial\_object, is layout friendly. It checks if the minimum distance between successive coefficients is at least 2.

```
p1 = Polynomial ( [16, 15, 2, 1, 0] )
p1.isLayoutFriendly()
# >>> False
p2 = Polynomial ( [16, 14, 5, 2, 0] )
p2.isLayoutFriendly()
# >>> True
```

#### Polynomial\_object.isPrimitive()

Returns True if the given polynomial is primitive over GF(2). All coefficients are considered to be positive. Note, that the first call of this method may take more time than usual, because of prime dividers database loading. This methods bases on fast simulation of LFSRs described in [1].

```
p1 = Polynomial ( [16, 5, 2, 0] ) p1.isPrimitive()
```

```
# >>> False
p2 = Polynomial ( [4, 1, 0] )
p2.isPrimitive()
# >>> True
```

#### Polynomial\_object.iterateThroughSigns()

This is generator method. Each time yields new Polynomial object with other combinations of coefficient signs. Note, that the highest and lowest coefficients are untouched. All-positive and all-negative combinations are also not yielded.

```
\begin{array}{lll} \mathbf{p1} &= \mathbf{Polynomial} \; ( \; [16 \, , \; -5, \; 2 \, , \; 1 \, , \; 0 ] \; ) \\ \text{for pi in p1.iterateThroughSigns} () \colon \; \mathbf{print} (\, \mathrm{pi}) \\ \# >>> \; [16 \, , \; -5, \; 2 \, , \; 1 \, , \; 0 ] \\ \# >>> \; [16 \, , \; 5, \; -2, \; 1 \, , \; 0 ] \\ \# >>> \; [16 \, , \; -5, \; -2, \; 1 \, , \; 0 ] \\ \# >>> \; [16 \, , \; 5, \; 2 \, , \; -1, \; 0 ] \\ \# >>> \; [16 \, , \; -5, \; 2 \, , \; -1, \; 0 ] \\ \# >>> \; [16 \, , \; 5, \; -2, \; -1, \; 0 ] \end{array}
```

#### Polynomial\_object.nextPrimitive(Silent=True)

Tries to find next polynomial which is primitive over GF(2). Returns True if found, otherwise returns False. if Silent argument is False, then searching process is shown in the terminal.

```
p1 = Polynomial ( [16, 15, 2, 1, 0] )
p1.nextPrimitive()
# >>> True
print(p1)
# >>> [16, 12, 3, 1, 0]
p1.nextPrimitive()
# >>> True
print(p1)
# >>> True
print(p1)
# >>> [16, 6, 4, 1, 0]
```

#### Polynomial\_object.printFullInfo()

Prints (also to the transcript in testcase mode) full info about the Polynomial\_object. See the example below:

```
p1 = Polynomial ( [16, 5, 2, 0] )
p1.printFullInfo()
#
#
  Polynomial deg=16, bal=9
#
# Degree
                        16
# Coefficients count:
                        4
                        10(2)25
# Hex with degree
# Hex without degree:
# Balancing
# Is layout-friendly:
                        True
                        [16, 5, 2, 0]
# Coefficients
```

#### Polynomial\_object.setStartingPointForIterator(StartingPolynomial)

Polynomial object may be used as generators, to iterate through all possible polynomials with respect to some requirements (see createPolynomial() method). This one is used to set starting point for iterator. See the example below. Note, that StartingPolynomial may be another Polynomial

object, or a list of coefficients. The starting polynomial is checked to have the same degree and coefficients count as the Polynomial object.

```
p1 = Polynomial ([6,1,0])
for pi in p1: print(pi)
\# >>> [6, 1, 0]
\# >>> [6, 2, 0]
\# >>> [6, 3, 0]
\# >>> [6, 4, 0]
\# >>> [6, 5, 0]
p1.setStartingPointForIterator([6,3,0])
for pi in p1: print(pi)
\# >>> [6, 3, 0]
\# >>> [6, 4, 0]
\# >>> [6, 5, 0]
p1.setStartingPointForIterator( Polynomial([6,4,0]) )
for pi in p1: print(pi)
\# >>> [6, 4, 0]
\# >>> [6, 5, 0]
```

#### Polynomial\_object.toBitarray()

Returns a bitarray object representing the Polynomial.

```
p1 = Polynomial ( [16, 5, 2, 0] )
p1.toBitarray()
# >>> bitarray('10100100000000001')
```

#### Polynomial\_object.toHexString(IncludeDegree=True, shorten=True)

Returns a string of hexadecimal characters describing the Polynomial object.

```
p1 = Polynomial ( [16, 5, 2, 0] )
p1.toHexString()
# >>> '10(2)25'
p1.toHexString(IncludeDegree=False)
# >>> '25'
p1.toHexString(shorten=False)
# >>> '10025'
```

#### Polynomial\_object.toInt()

Returns an integer representing the Polynomial object.

```
\begin{array}{lll} p1 = Polynomial & ( & [16\,, \ 5\,, \ 2\,, \ 0] & ) \\ & bin(p1.toInt()) & \\ \#>>> & '0\,b1000000000100101' & \end{array}
```

#### Polynomial\_object.toMarkKassabStr()

Returns a string used by Mark Kassab's C++ code to add a polynomial to the internal database.

```
p1 = Polynomial ( [16, -5, 2, 0] )
p1.toMarkKassabStr()
#>>> 'add polynomial(16, 5, 2, 0);'
```

### 2.2 Static Polynomial methods

Takes a list of Polynomial objects and returns a filtered list, containing only primitives. Uses multithreading.

- Candidates list of polynomials to check,
- n if n > 0 then stops once n primitives found,
- Silent if False then prints more info during searching. Otherwise (default) prints only a progress bar.

```
Polynomial. checkPrimitives ([ [4,1,0], [4,2,0], [4,3,0] ]) # >>> [Polynomial([4, 3, 0]), Polynomial([4, 1, 0])]
```

Polynomial.createPolynomial(PolynomialDegree, PolynomialCoefficientsCount, PolynomialBalancing=0, LayoutFriendly=False, MinDistance=0)

Returns a first Polynomial object having a specified properties. Such object may be used then as iterator, to go through all polynomials having the same properties.

- PolynomialDegree degree of polynomial,
- PolynomialCoefficientsCount coefficients count, including degree and 0,
- PolynomialBalancing maximum allowed balancing. '0' means 'no limit'. See Polynomial.getBalancing on page 5 for more details,
- LayoutFriendly wheather the polynomial must be layout-friendly or not. See Polynomial.isLayoutFriendly on page 6,
- MinDistance minimum required distance between successive coefficients.

```
p = Polynomial.createPolynomial(16, 4, MinDistance=4)
p
# >>> Polynomial([16, 8, 4, 0])
for pi in p: print(pi)
# >>> [16, 8, 4, 0]
# >>> [16, 9, 4, 0]
# >>> [16, 10, 4, 0]
# >>> [16, 11, 4, 0]
# ...
# >>> [16, 12, 8, 0]
```

#### Polynomial.decodeUsingBerlekampMassey(Sequence)

Simply realizes a Berlekamp-Massey algorithm to decode a characteristic polynomial basing on a sequence generated by an LFSR.

• Sequence - any iterable object, like bitarray, string and so on, or pointer to Lfsr object.

```
# Decode a polynomial from a sequence: 

Polynomial.decodeUsingBerlekampMassey("110001")

# >>> Polynomial([4, 3, 0])

# Decode a characteristic polynomial of an LFSR: lfsr = Lfr([4,1,0], GALOIS)

Polynomial.decodeUsingBerlekampMassey(lfsr)

# >>> Polynomial([4, 1, 0])
```

### 2.3 Static Polynomial methods to search for primitives

Below are listed static Polynomial method intended to search for primitive ones. Each method has three versions:

- 1. list<\*>Primitives returning a list of primitive polynomials,
- 2. print<\*>Primitives printing found polynomials in a human-readable form,

3. first<\*>Primitive - returning a first found polynomial (or None if nothing found).

All those methods have the same arguments, so that below are listed only those having a name starting from list<\*>. Consider also using *interactive menu*, when working in interactive shell. It makes easier to configure below described searching methods (see page 34).

Polynomial.listAllPrimitivesHavingSpecifiedCoeffs(CoefficientList, CoeffsCount=0, DontTouchBounds=True, OddOnly=True)

Takes a list of all available coefficients. Tries to search for primitive polynomials having coefficients included in the given list.

- CoefficientList list of all available coefficients,
- CoeffsCount specify here how many coefficients must have the found primitive polynomials (0 = 'any'),
- DontTouchBounds if True then the highest and lowest coefficients (degree and 0) must always be included,
- OddOnly limit searching only to such candidates having odd coefficient count.

```
# Let's say we have a ring generator, having gated taps on such # positions, so that the most rich polynomial implemented by thus # ring generator is: # [16, 14, 13, 12, 10, 9, 8, 5, 4, 2, 1, 0] # Let's find how many primitive polynomials may we implement # using such register: len(Polynomial.listAllPrimitivesHavingSpecifiedCoeffs(\ [16, 14, 13, 12, 10, 9, 8, 5, 4, 2, 1, 0])) # >>> 49 # Let's determine also how many pentanomials may we implement # using our register: len(Polynomial.listAllPrimitivesHavingSpecifiedCoeffs(\ [16, 14, 13, 12, 10, 9, 8, 5, 4, 2, 1, 0], 5)) # >>> 7
```

Polynomial.listDensePrimitives(PolynomialDegree, m=0, Silent=True, StartingPolynomial=None) Search for dense primitives [2].

- PolynomialDegree degree of polynomial,
- n if n > 0 then stops once n primitives found,
- Silent if False then prints more info during searching. Otherwise (default) prints only a progress bar,
- StartingPolynomial you may specify a starting polynomial having the same properties as the ones passed to this method.

Polynomial.listEveryNTapsPrimitives(PolynomialDegree, EveryN, m=0, Silent=True, StartingPolynomial=Non

Search for well balanced (see page 5) polynomials having specified average distance between successive coefficients.

- PolynomialDegree degree of polynomial,
- EveryN average distance between successive coefficients.
- n if n > 0 then stops once n primitives found,
- Silent if False then prints more info during searching. Otherwise (default) prints only a progress bar,
- StartingPolynomial you may specify a starting polynomial having the same properties as the ones passed to this method.

Polynomial.listHybridPrimitives(PolynomialDegree, PolynomialCoefficientsCount, PolynomialBalancing=0, LayoutFriendly=False, MinDistance=0, m=0, NoResultsSkippingIteration=0, StartingPolynomial=None, MinNotMatchingTapsCount=0)

Search for polynomials which can create maximum length Hybrid LFSRa (see page 14).

- PolynomialDegree degree of polynomial,
- PolynomialCoefficientsCount coefficients count, including degree and 0,
- PolynomialBalancing maximum allowed balancing. '0' means 'no limit'. See Polynomial.getBalancing on page 5 for more details,
- LayoutFriendly wheather the polynomial must be layout-friendly or not. See Polynomial.isLayoutFriendly on page 6,
- MinDistance minimum required distance between successive coefficients,
- n if n > 0 then stops once n primitives found,
- Silent if False then prints more info during searching. Otherwise (default) prints only a progress bar,
- NoResultsSkippingIteration if specified to be > 0 then it breaks the searching process if no result within the given number, successive iterations,
- StartingPolynomial you may specify a starting polynomial having the same properties as the ones passed to this method,
- MinNotMatchingTapsCount using this parameter you can specify at least how many taps must differ all found polynomials. In other words, if you specify minimum k different taps and you get a result, so take any one of the found polynomials and compare with each one of the rest results you can consider, than each time at least k coefficients are different.

Polynomial.listPrimitives(PolynomialDegree, PolynomialCoefficientsCount, PolynomialBalancing=0, LayoutFriendly=False, MinDistance=0, m=0, Silent=True, MaxSetSize=10000, ExcludeList=[], ReturnAlsoAllCandidaes=False, FilteringCallback=None, NoResultsSkippingIteration=0, StartingPolynomial=None)

The most general method to search for primitive polynomials.

- PolynomialDegree degree of polynomial,
- PolynomialCoefficientsCount coefficients count, including degree and 0,
- PolynomialBalancing maximum allowed balancing. '0' means 'no limit'. See Polynomial.getBalancing on page 5 for more details,
- LayoutFriendly wheather the polynomial must be layout-friendly or not. See Polynomial.isLayoutFriendly on page 6,
- MinDistance minimum required distance between successive coefficients,
- n if n > 0 then stops once n primitives found,
- Silent if False then prints more info during searching. Otherwise (default) prints only a progress bar,
- MaxSetSize how many polynomials should be tested in parallel in one iteration,
- ExcludeList polynomials included in this list will e skipped from checking,
- ReturnAlsoAllCandidaes if True then as a result this method will return list of 2 lists: [[primitive\_polys], [all\_checked\_polys]],
- FilteringCallback if specified, then will be called for each candidate polynomial: callback(candidate\_polynomial) and should return True if the given polynomial should be checked, otherwise the given polynomial will be skipped from checking,
- NoResultsSkippingIteration if specified to be > 0 then it breaks the searching process if no result within the given number, successive iterations,

• StartingPolynomial - you may specify a starting polynomial having the same properties as the ones passed to this method.

Polynomial.listTapsFromTheLeftPrimitives(PolynomialDegree, PolynomialCoefficientsCount, MaxDIstance=3 m=0, Silent=True)

Search for such primitive polynomials having coefficients grouped near the left corner, like [10,9,8,7,0].

- PolynomialDegree degree of polynomial,
- PolynomialCoefficientsCount coefficients count, including degree and 0,
- MaxDistance maximum required distance between successive coefficients grouped near the left corner,
- n if n > 0 then stops once n primitives found,
- Silent if False then prints more info during searching. Otherwise (default) prints only a progress bar.

Polynomial.listTigerPrimitives(PolynomialDegree, PolynomialCoefficientsCount, PolynomialBalancing=0, LayoutFriendly=False, MinDistance=0, m=0, NoResultsSkippingIteration=0, StartingPolynomial=None, MinNotMatchingTapsCount=0)

Search for polynomials which can create maximum length Tiger LFSRa (see page 15).

- PolynomialDegree degree of polynomial,
- PolynomialCoefficientsCount coefficients count, including degree and 0,
- PolynomialBalancing maximum allowed balancing. '0' means 'no limit'. See Polynomial.getBalancing on page 5 for more details,
- LayoutFriendly wheather the polynomial must be layout-friendly or not. See Polynomial.isLayoutFriendly on page 6,
- MinDistance minimum required distance between successive coefficients,
- n if n > 0 then stops once n primitives found,
- Silent if False then prints more info during searching. Otherwise (default) prints only a progress bar,
- $\bullet$  NoResultsSkippingIteration if specified to be >0 then it breaks the searching process if no result within the given number, successive iterations,
- StartingPolynomial you may specify a starting polynomial having the same properties as the ones passed to this method,
- MinNotMatchingTapsCount using this parameter you can specify at least how many taps must differ all found polynomials. In other words, if you specify minimum k different taps and you get a result, so take any one of the found polynomials and compare with each one of the rest results you can consider, than each time at least k coefficients are different.

## Class Lfsr

Lfsr is an object type allowing to simulate and analyze any type of Linear Feedback Shift Register. Simulations are performed using bitarray objects, where bitarray\_object[N] holds value of Flip-Flop having index N. Lfsr objects are always simulated assuming, that data is shifted from higher to lower indexed flip-flop (from FF[1] to FF[0], from FF[2] to FF[1] and so on).

### 3.1 Lfsr types

#### 3.1.1 Fibonacci

Look at the Figure 3.1. It shows an example of Fibonacci LFSR implementing the polynomial of  $x^8 + x^6 + x^5 + x^2 + 1$ . There are couple of ways to create such Lfsr object:

```
# using existing Polynomial object: p1 = Polynomial([8,6,5,2,0])  
lfsr1 = Lfsr(p1, FIBONACCI)  
# using Polynomial created in place: lfsr1 = Lfsr(Polynomial([8,6,5,2,0]), FIBONACCI)  
# using coefficients list: lfsr1 = Lfsr([8,6,5,2,0], FIBONACCI)
```

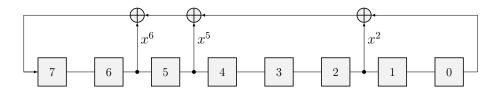


Figure 3.1: Fibonacci LFSR implementing polynomial  $x^8 + x^6 + x^5 + x^2 + 1$ .

#### 3.1.2 Galois

Figure 3.1 shows an example of Galois LFSR implementing the polynomial of  $x^8 + x^6 + x^5 + x^2 + 1$ . There are couple of ways to create such Lfsr object:

```
# using existing Polynomial object:  p1 = \mathbf{Polynomial} ([8,6,5,2,0])   lfsr1 = \mathbf{Lfsr}(p1, \text{ GALOIS})  # using Polynomial created in place:  lfsr1 = \mathbf{Lfsr}(\mathbf{Polynomial}([8,6,5,2,0]), \text{ GALOIS})  # using coefficients list:  lfsr1 = \mathbf{Lfsr}([8,6,5,2,0], \text{ GALOIS})
```

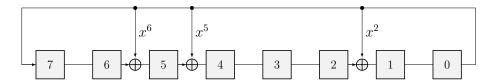


Figure 3.2: Galois LFSR implementing polynomial  $x^8 + x^6 + x^5 + x^2 + 1$ .

#### 3.1.3 Ring Generator

Ring generator is a structure discussed in [1]. Example of a Ring Generator is shown in the Figure 3.3 implementing the polynomial  $x^8 + x^6 + x^5 + x^2 + 1$ . Ways to create such object are:

```
# using existing Polynomial object:  p1 = \textbf{Polynomial}([8,6,5,2,0]) \\ lfsr1 = \textbf{Lfsr}(p1, RING\_GENERATOR) \\ # using Polynomial created in place: \\ lfsr1 = \textbf{Lfsr}(\textbf{Polynomial}([8,6,5,2,0]), RING\_GENERATOR) \\ # using coefficients list: \\ lfsr1 = \textbf{Lfsr}([8,6,5,2,0], RING\_GENERATOR)
```

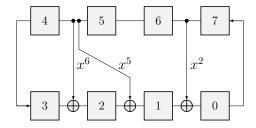


Figure 3.3: Ring Generator implementing polynomial  $x^8 + x^6 + x^5 + x^2 + 1$ .

#### 3.1.4 Ring with manually specified taps

If you wish to create a LFSR specifying a taps by hand, then choose Ring with manually specified taps. To create such object you need to specify a size of Lfsr (flip-flop count) and a list of tap definitions. Each tap is defined as another list: [source\_ff\_index, destination\_ff\_index]. For better understanding consider the example from Figure 3.4. You can see there the list of 3 taps: [[4,7], [8,2], [9,0]]. The first tap is [4,7] which is considered as from output of 4th flip-flop to a XOR gate at 7th flip-flop input. So be careful and remember: from <source> OUTPUT to the XOR at <destination> INPUT. You can create an Lfsr object implementing the structure shown in the Figure 3.4 that way:

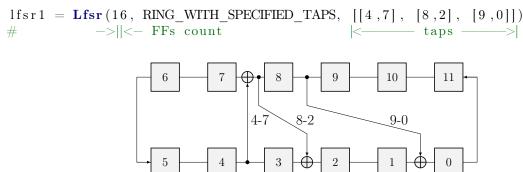


Figure 3.4: Ring with manually specified taps [[4,7], [8,2], [9-0]]

#### 3.1.5 Hybrid Ring Generator

Hybrid Ring Generator is very similar to Ring Generator. The only difference is, that taps direction is configurable. If the corresponding coefficient of polynomial (note: this polynomial is NOT the characteristic one!) is positive, then tap direction is down, as in case of Ring Generator. When the corresponding

coefficient is negative, then tap direction is up. Look at the example shown in the Figure 3.5. To create an Lfsr object representing the Hybrid Ring Generator mentioned in the example, use such code:

```
# using existing Polynomial object:  p1 = \frac{\textbf{Polynomial}}{\textbf{Polynomial}}([8,6,-5,-2,0])   lfsr1 = \frac{\textbf{Lfsr}}{\textbf{p1}}, \frac{\textbf{HYBRID}}{\textbf{RING}}  # using Polynomial created in place:  lfsr1 = \frac{\textbf{Lfsr}}{\textbf{Polynomial}}([8,6,-5,-2,0]), \frac{\textbf{HYBRID}}{\textbf{RING}}  # using coefficients list:  lfsr1 = \frac{\textbf{Lfsr}}{\textbf{lfsr}}([8,6,-5,-2,0], \frac{\textbf{HYBRID}}{\textbf{RING}})
```

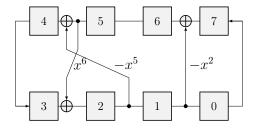


Figure 3.5: Hybrid Ring Generator implementing polynomial  $x^8 + x^6 - x^5 - x^2 + 1$ .

#### 3.1.6 Tiger Ring Generator

Tiger Ring Generator is a special case of Hybrid Ring Generator. In case of Tiger Ring taps are directed up-down-up-down etc. The most right tap is directed up, as shown in the example at Figure 3.6. The advantage of Tiger Ring Generator over Hybrid Ring Generator is, that signs of polynomial coefficients do not matter. Look at the code used to implement the Tiger Ring from the example:

```
# using existing Polynomial object:

p1 = Polynomial([8,6,5,2,0])

lfsr1 = Lfsr(p1, TIGER_RING)

# using Polynomial created in place:

lfsr1 = Lfsr(Polynomial([8,6,5,2,0]), TIGER_RING)

# using coefficients list:

lfsr1 = Lfsr([8,6,5,2,0], TIGER_RING)
```

Consider, that the polynomial coefficients in the code above are positive. As mentioned, their signs do not matter and the same result can also be obtained using such code:

```
\begin{array}{lll} {\rm lfsr}\,1 &=& {\bf Lfsr}\,([8\,,-6\,,5\,,-2\,,0]\,,\ {\rm TIGER\_RING}) \\ {\rm lfsr}\,2 &=& {\bf Lfsr}\,([8\,,-6\,,-5\,,-2\,,0]\,,\ {\rm TIGER\_RING}) \\ {\rm lfsr}\,3 &=& {\bf Lfsr}\,([8\,,6\,,-5\,,2\,,0]\,,\ {\rm TIGER\_RING}) \\ \#\ \dots\ {\rm etc}\,. \end{array}
```

As in case of Hybrid Ring Generators, the polynomial used to implement Tiger Rings is NOT their characteristic one.

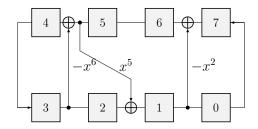


Figure 3.6: Tiger Ring Generator implementing polynomial  $x^8 - x^6 + x^5 - x^2 + 1$ .

### 3.2 Lfsr object methods

```
Lfsr_object.__str__()
    It returns a string containing binary value of the Lfsr object (left MSb).
    lfsr1 = Lfsr([4,1,0], GALOIS)
    str(lfsr1)
# >>> '0001'
```

```
# >>> 0001
lfsr1.next()
str(lfsr1)
# >>> '1001'
```

#### Lfsr\_object.clear()

Removes the fast simulation array of the Lfsr object, if exists. Use this method to clear memory if fast simulation of the Lfsr object is no longer necessary.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
# Check if the lfsr1 generates M-Sequence. That check requires
# the Fast Simulation Array to be created, so the array
# is built in the background.
lfsr1.isMaximum()
# >>> True
lfsr.clear()
```

Lfsr\_object.createPhaseShifter(OutputCount, MinimumSeparation=100,
MaxXorInputs=3, MinXorInputs=1, FirstXor=None)

Returns a PhaseShifter object. Needs some parameters to calculate phase shifting XORs:

- OutputCount how many outputs the Phase Shifter to have,
- MinimumSeparation minimum separation between Phase Shifter outputs,
- MaxXorInputs how many inputs the largest XOR gate may have,
- MinXorInputs how many inputs the smallest XOR gate may have,
- FirstXor you can specify a list of Lfsr output bits indexes making the first Phase Shifter XOR gate. If None (not specified), then the first output of the Phase SHifter is considered the Lfsr FF[0].

#### Lfsr\_object.getDual()

Returns a reference to taps list of the LFSR.

```
\begin{array}{l} lfsr1 &= \mathbf{Lfsr}\left(\left[4\,,1\,,0\right], \; RING\_GENERATOR\right) \\ lfsr1.getTaps\left(\right) \\ \#>>> \left[\left[3\,, \; \; 3\right]\right] \end{array}
```

```
Lfsr_object.getPhaseShiftIndexes(ListOfXoredOutputs: list, DelayedBy: int)
```

Given a sequence obtained by XORing outputs of specified flip-flops. This method returns a list of other flip-flop indexes, at XOR of which the sequence is delayed by specified clock cycles than the one mentioned in the above assumption.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
```

```
\# How to obtain a sequence observed at FF[0] delayed by 2 cycles? Ifsr1.getPhaseShiftIndexes([0], 2) \#>>> [2] \# ... so at FF[2] we an observe the same sequence as at FF[0] delayed \# by 2 cycles. \# How to obtain a sequence observed at XOR(FF[3], FF[0]) delayed \# by 5 cycles? Ifsr1.getPhaseShiftIndexes([3,0], 5) \#>>> [1, 3] \# ... so at XOR(FF[1], FF[3]) we can observe the same sequence as at \# XOR(FF[3], FF[0]) delayed by 5 cycles.
```

#### Lfsr\_object.getPeriod()

Does the standard simulation and finds a period of the Lfsr. May take much time! Consider using isMaximum() method if possible.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.getPeriod()
# >>> 15
```

#### Lfsr\_object.getSize()

Returns a size (flip-flops count) of the Lfsr object.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.getSize()
# >>> 4
```

#### Lfsr\_object.getValue()

Returns a reference to actual value of Lfsr (bitarray).

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.getValue()
# >>> bitarray('0001')
lfsr1.next()
lfsr1.getValue()
# >>> bitarray('1001')
```

#### Lfsr\_object.getMSequence(BitIndex=0, Reset=True)

Returns a bitarray object conteining the M-Sequence observed at selected bit.

- BitIndex at which flip-flop the sequence to observe,
- Reset if True then the .reset() method is called before simulation.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.getMSequence()
for value in values: print(value)
# >>> bitarray('111101011001000')
```

#### Lfsr\_object.getSequence(BitIndex=0, Reset=True, Length=0)

Returns a bitarray object containing a bit sequence observed at selected bit.

- BitIndex at which flip-flop the sequence to observe,
- Reset if True then the .reset() method is called before simulation,
- Length length of the requested sequence.0 means M-Sequence.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.getSequence(Length=6)
for value in values: print(value)
# >>> bitarray('111101')
```

#### Lfsr\_object.getValues(n=0, step=1, reset=True)

Does simulation of the Lfsr and returns a list of values.

- n how many values to return. Default os 0 meaning we want all values to get,
- step how many clock cycles per step. If step=N then consecutive values are obtained every N clock cycles,
- reset if True then the .reset() method is called before simulation.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
values = lfsr1.getValues()
for value in values: print(value)
# >>> bitarray('1000')
# >>> bitarray('1001')
# >>> bitarray('1011')
# ...
# >>> bitarray('0100')
```

#### Lfsr\_object.isMaximum()

Returns True if the Lfsr generates a M-Sequence. Uses fast simulation method [1] and checks also subcycles.

```
\begin{array}{l} {\rm lfsr}\,1 \ = \ {\bf Lfsr}\,(\left[\,4\;,1\;,0\,\right]\,,\ {\rm RING\_GENERATOR}) \\ {\rm lfsr}\,1\;.{\rm isMaximum}\,(\,) \\ \#>>> \ {\rm True} \end{array}
```

#### Lfsr\_object.next(steps=1)

Calculates (and also returns a reference to) the next value of the Lfsr. This is the core method of LFSR simulation flow. If the specified steps > 1, then it engages Fast Simulation method [1].

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.getValue()
# >>> bitarray('0001')
lfsr1.next()
# >>> bitarray('1001')
lfsr1.next(2)
# >>> bitarray('1111')
```

#### Lfsr\_object.printFastSimArray()

Prints the array used for fast simulation [1].

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.printFastSimArray()
# >>> 1001
               0001
                        0010
                                 0100
                        0001
                                 0010
# >>> 1101
               1001
               1111
                        1101
# >>> 1110
                                 1001
# >>> 1011
               0101
                        1010
                                 0111
```

#### Lfsr\_object.printValues(n=0, step=1, reset=True)

Does the same as Lfsr\_object.getValues(), but prints (to the screen and to the transcript as well) the result in human-readable form.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.printValues()
# >>> 0001
# >>> 1001
# >>> 1101
# >>> ...
# >>> 0010
```

#### Lfsr\_object.reset()

Sets 0s to all Lfsr flip-flops, besides FF[0] which is set to 1. Also returns a reference to actual value of the Lfsr.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.getValue()
# >>> bitarray('0001')
lfsr1.next()
# >>> bitarray('1001')
lfsr1.reset()
# >>> bitarray('0001')
```

#### Lfsr\_object.reverseTap(TapIndex)

Reverses tap in case of Lfsr object having taps, like Ring generator etc. Such fsr object have list of taps, so this method takes a tap index telling them which one to revert. Tap reversing is used to obtain a dual Lfsr, for example.

```
\begin{array}{l} {\rm lfsr1} = {\bf Lfsr} \left( \left[ 64 \,,\; 15 \,,\; 7 \,,\; 0 \right] ,\; {\rm RING\_GENERATOR} \right) \\ {\rm lfsr1.getTaps} \left( \right) \\ \# >>> \left[ \left[ 60 \,,\; 2 \right] ,\; \left[ 56 \,,\; 6 \right] \right] \\ \# \; {\rm let} \; {\rm 's \;\; revert \;\; the \;\; second \;\; tap:} \; \left[ 56 \,,\; 6 \right] ; \\ {\rm lfsr1.reverseTap} \left( 1 \right) \\ \# >>> \; {\rm True} \\ \# \; \dots {\rm True \;\; means \;\; the \;\; tap \;\; index \;\; and \;\; the \;\; Lfsr \;\; type \;\; are \;\; correct .} \\ {\rm lfsr1.getTaps} \left( \right) \\ \# >>> \; \left[ \left[ 60 \,,\; 2 \right] ,\; \left[ 7 \,,\; 55 \right] \right] \end{array}
```

#### Lfsr\_object.simulateForDataString(Sequence, InjectionAtBit=0, StartValue=None)

Performs a simulation for the Lfsr object having one injector. Step count (number of clock cycles) is equal to the length of a given Sequence. Returns the last Lfsr value.

- Sequence any iterable object, whose consecutive values are convertible to bool,
- InjectionAtBit index of flip-flop at which input the injector is placed,
- StartValue seed of the LFSR.

```
lfsr1 = Lfsr([4,1,0], GALOIS)
lfsr1.simulateForDataString('110010')
# >>> bitarray('1001')
```

#### Lfsr\_object.toVerilog(ModuleName, InjectorIndexesList=[])

Returns a string containing Verilog description of the Lfsr object.

- ModuleName name of the Verilog module,
- InjectorIndexesList a list containing indexes of flip-flops at which input injectors have to be placed.

```
lfsr1 = Lfsr([4,1,0], GALOIS)

print(lfsr1.toVerilog("MyModule", [0,2]))
```

```
# >>> module MyModule (
# >>>
         input wire clk,
# >>>
         input wire enable,
# >>>
         input wire reset,
# >>>
         input wire [1:0] injectors,
# >>>
         output reg [3:0] O
# >>> );
# >>>
#>>> always @ (posedge clk or posedge reset) begin
# >>>
         if (reset) begin
# >>>
          O \le 4'd0;
         end else begin
# >>>
# >>>
           if (enable) begin
# >>>
             O[0] <= O[1] ^ O[0] ^ injectors [0];
             O[1] <= O[2];
# >>>
             O[2] \ll O[3] ^ injectors [1];
# >>>
# >>>
             O[3] <= O[0];
# >>>
           end
         \quad \text{end} \quad
# >>>
# >>> end
# >>>
\#>>>  endmodule
```

#### 3.3 Lfsr static methods

Lfsr.checkMaximum(LfsrsList, n=0, SerialChunkSize=20, ReturnAlsoNotTested=False)

Takes a list of Lfsr objects and checks each one if can produce M-Sequence. Returns a list containing only maximum ones.

- LfsrsList list of Lfsr objects,
- ${\tt n}$  how many maximum Lfsrs you need. If the n is achieved, breaks the simulation. 0 means no limit,
- SerialChunkSize simulation are performed using multithreading. This value means how many Lfsrs can be simulated in series per one thread,
- ReturnAlsoNotTested using this argument makes sense with n > 0. if True, then it returns a list containing two other lists: [MaximumLfsrs, NotTestedLfsrs]

```
\begin{array}{lll} & \textbf{lfsr} \ 1 & = \textbf{Lfsr} \ ([5\,,1\,,0]\,, \ \text{GALOIS}) \\ & \textbf{lfsr} \ 2 & = \textbf{Lfsr} \ ([5\,,2\,,0]\,, \ \text{GALOIS}) \\ & \textbf{lfsr} \ 3 & = \textbf{Lfsr} \ ([5\,,3\,,0]\,, \ \text{GALOIS}) \\ & \textbf{Lfsr} \ . \text{checkMaximum} \ ([\, lfsr1\,\,, \ lfsr2\,\,, \ lfsr3\,]) \\ & \# >>> \ [\, Lfsr \ ([5\,, \ 2\,, \ 0]\,, \ LfsrType \,. \, Galois\,) \,, \\ & \# >>> \ Lfsr \ ([5\,, \ 3\,, \ 0]\,, \ LfsrType \,. \, Galois\,)] \end{array}
```

# Class ProgrammableLfsr

ProgrammableLfsr is a class intended to make easy to design and analyse any kind of LFSR with programmable feedback taps. To create a ProgrammableLfsr object one need to specify a list of configurable taps. Each configurable tap is described by a dictionary. Each key of such dictionary is a custom name, like "tapOn", or just a number - does not matter - and is used to make analysis reports readable. The corresponding value is a standard tap definition: [<source\_FF\_index>, <destination\_FF\_index>]. Consider some examples of configurable tap dictionaries:

- {'Tap1':[3 6]} mandatory (constant) tap from output of FF[3] to a XOR gate at input of FF[6]
- {'Tap1\_OFF': None, 'Tap1\_ON': [3,6]} gated tap from output of FF[3] to a XOR gate at input of FF[6]. Consider the value of the first key: None, which means no connection
- {'Sw1':[3,6], 'Sw2':[3,8]} switched tap: from output of FF[3] to a XOR gate at input of FF[6], or from output of FF[3] to a XOR gate at input of FF[8]
- {'Sw0':None, 'Sw1':[3,6], 'Sw2':[3,8]} like above, but this time there is a way to disable (no connection)
- {'Sw1': [3,6], 'Sw2': [4,8]} switched tap: from output of FF[3] to a XOR gate at input of FF[6], or from output of FF[8] to a XOR gate at input of FF[8]

Consider, that there is no required to make common source or common destination anywhere. See also ProgrammableLfsrConfig utility class on page 25

## 4.1 ProgrammableLfsr object methods

ProgrammableLfsr\_object.\_\_init\_\_(SizeOrProgrammableLfsrConfiguration, TapsList=[],
OperateOnTapsOnly=False)

ProgrammableLfsr object initializer.

- SizeOrProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to ProgrammableLfsrConfiguration size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference to Programmable size of the LFSR or a reference size of the LFSR or a
- TapsList list of Configurable Taps Dictionaries (see description on page 21)
- OperateOnTapsOnly as a result of analysis you may get a list of Lfsr objects. However, to save the memory, by setting this parameter to True, you may force to operate on tap lists only, so that tap lists will be returned instead of lists of Lfsr objects.

#### ProgrammableLfsr\_object.clear()

It simply deletes results of Programmable Lfsr analysis to save the memory

#### ProgrammableLfsr\_object.getAllPosssibleTaps()

Returns a list containing all connections (taps) possible to implement by the ProgrammableLfsr object. See the example on page 22

#### ProgrammableLfsr\_object.getSize()

Returns a size (flip-flop count) of the Programmable Lfsr object.

#### ProgrammableLfsr\_object.getPolynomialsAndLfsrsDictionary(Optimization=False)

Returns a dictionary, containing all primitive polynomials the ProgrammableLfsr object can implement and corresponding Lfsr' objects (or tap lists). If Optimization is set to True, then it tries to optimize all configurations of the programmable LFSR so that as less taps are used, as possible. See the example on page 22

#### ProgrammableLfsr\_object.getLfsrs(Optimization=True)

Returns a list containing all maximum Lfsrs implemented by the ProgrammableLfsr object. If Optimization is set to True, then it tries to optimize all configurations of the programmable LFSR so that as less taps are used, as possible. See the example on page 22

#### ProgrammableLfsr\_object.getPolynomials()

Returns a list containing all primitive polynomials implemented by the ProgrammableLfsr object. See the example on page 22

#### ProgrammableLfsr\_object.getUsedTaps()

Returns a list containing used connections (taps) after optimization. See the example on page 22

#### ProgrammableLfsr\_object.getUnusedTaps()

Returns a list containing unused connections (taps) after optimization. Removing those connections will not affect the primitive polynomials list implemented by this ProgrammableLfsr object. See the example on page 22

#### ProgrammableLfsr\_object.toVerilog(ModuleName, InjectorIndexesList=[])

Returns a string containing Verilog description of the ProgrammableLfsr object.

- ModuleName name of the Verilog module,
- InjectorIndexesList a list containing indexes of flip-flops at which input injectors have to be placed.

See the example on page 22

#### Example of Programmable Lfsr analysis:

```
# let's examine a 8-bit LFSR having: # - a gated tap from output of FF[6] to a XOR at input of FF[0], # - a gated tap from output of FF[5] to a XOR at input of FF[0], # - a switchable tap tap from output of FF[4] to a XOR at input of FF[3] # of from output of FF[3] to a XOR at input of FF[4] with no-connection (disable) option # - a switchable tap tap from output of FF[2] to a XOR at input of FF[3] # of from output of FF[4] to a XOR at input of FF[3] # with no-connection (disable) option
```

```
plfsr = ProgrammableLfsr(8, |
{ 'None': None, '4-3': [4, 3], '3-4': [3, 4]}, { 'None': None, '2-3': [2, 3], '4-2': [4, 2]}
], OperateOnTapsOnly = True)
plfsr.getPolynomialsAndLfsrsDictionary()
\#>>> \{ \text{Polynomial}([8\,,\ 5\,,\ 3\,,\ 2\,,\ 0])\colon\ [[[6\,,\ 0]\,,\ [3\,,\ 4]]\,,\ [[6\,,\ 0]\,,\ [2\,,\ 3]]] \}
plfsr.getPolynomialsAndLfsrsDictionary(True)
\# >>> \{Polynomial([8, 5, 3, 2, 0]): [[6, 0], [2, 3]]\}
# As we can see, such Programmable Lfsr can implement 2 maximum Lfsrs,
# but only 1 primitive polynomial.
# We can even get a simple list of primitive polynomials implemented
# by the 'plfsr':
plfsr.getPolynomials()
\# >>> [Polynomial([8, 5, 3, 2, 0])]
# ... and a simple list of all possible Lfsrs (tap lists in our case).
# So without optimization (all possible, maximum ones):
plfsr.getLfsrs(False)
\# >>> [[[6, 0], [3, 4]], [[6, 0], [2, 3]]]
# ... and with optimization:
plfsr.getLfsrs(True)
\# >>> [[[6, 0], [3, 4]]]
# DO you know all possible connections? Let's check it:
plfsr.getAllPosssibleTaps()
\# >>> [[6, 0], [5, 0], [4, 3], [3, 4], [2, 3], [4, 2]]
# Now determine, which connections are used:
plfsr..getUsedTaps()
\# >>> [[6, 0], [3, 4]]
# ... so it seems only 2 taps are required. So which ones are unused?
plfsr.getUnusedTaps()
\# >>> [[5, 0], [4, 3], [2, 3], [4, 2]]
# Finally, let's generate a verilog describingout Programmable Lfsr.
\# In addition assume we have injectors at FF[2,1,0]:
print(plfsr.toVerilog("MyProgrammableLfsr", [2,1,0]))
# module MyProgrammableLfsr (
    input wire clk,
    input wire enable,
    input wire reset,
#
#
    input wire [2:0] injectors,
#
    output reg [7:0] O
#);
#
# reg T0;
# reg T0 0;
# reg T1;
# reg T1 0;
\# reg T2;
\# reg T2_3;
\# \operatorname{reg} \operatorname{T2}_4;
\# reg T3;
# reg T3 3;
# reg T3_2;
#
# always @ (*) begin
#
    T0 <= 1'b0;
#
    if (config[0] = 1'd1) begin
#
      T0 \le O[6];
```

```
end
# end
#
# always @ (*) begin
  T1 <= 1'b0;
    if (config[1] = 1'd1) begin
#
      T1 <= O[5];
#
#
    end
\# end
# always @ (*) begin
    T2 <= 1'b0;
#
#
    if (config[3:2] = 2'd1) begin
#
      T2 <= O[4];
    end
    if (config[3:2] = 2'd2) begin
#
      T2 <= O[3];
#
    end
\# end
#
# always @ (*) begin
   T3 <= 1'b0;
#
    if (config[5:4] = 2'd1) begin
#
      T3 <= O[2];
#
#
    end
#
    if (config[5:4] = 2'd2) begin
#
      T3 \le O[4];
#
    end
\# end
#
# always @ (*) begin
#
    T0 0 <= 1, b0;
    if ((config[0:0] = 1'd1)) begin
#
#
      T0 \ 0 <= T0;
#
    end
# end
#
# always @ (*) begin
   T1 \ 0 <= 1'b0;
    if ((config[1:1] = 1'd1)) begin
#
#
      T1 \ 0 <= T1;
#
    end
# end
#
# always @ (*) begin
    T2 \ 3 <= 1, b0;
#
    if ((config[3:2] = 2'd1)) begin
#
      T2 3 \ll T2;
#
    end
# end
\# always @ (*) begin
    T2 \ 4 <= 1'b0;
#
    if ((config[3:2] = 2'd2)) begin
      T2 \ 4 \ll T2;
#
#
    end
\# end
#
# always @ (*) begin
```

```
#
    T3 \ 3 <= 1'b0;
    if ((config[5:4] = 2'd1)) begin
#
#
      T3 3 \ll T3;
#
    end
# end
#
# always @ (*) begin
    T3_2 <= 1, b0;
#
#
    if ((config[5:4] = 2'd2)) begin
#
      T3 \ 2 <= T3;
#
    end
# end
#
 always @ (posedge clk or posedge reset) begin
    if (reset) begin
#
     O \le 8' d0;
#
    end else begin
#
      if (enable) begin
        #
        O[1] \leftarrow O[2] \hat{} injectors[1];
#
        O[2] <= O[3] ^ T3 2 ^ injectors [0];
        O[3] <= O[4] ^ T2 3 ^ T3 3;
#
        O[4] <= O[5] ^ T2 ^ 4;
        O[5] <= O[6];
#
#
        O[6] <= O[7];
#
        O[7] <= O[0];
#
      end
#
    end
# end
\# endmodule
```

## 4.2 ProgrammableLfsrConfig utility class

ProgrammableLfsrConfig is a utility class making easier to create a configuration list for ProgrammableLfsr. Consider the example from page 22. Let's try to make the same ProgrammableLfsr object but this time using the ProgrammableLfsrConfig utility class:

```
# let's examine a 8-bit LFSR having:
\# - a gated tap from output of FF[6] to a XOR at input of FF[0],
\# - a gated tap from output of FF[5] to a XOR at input of FF[0],
\# - a switchable tap tap from output of FF[4] to a XOR at input of FF[3]
       of from output of FF[3] to a XOR at input of FF[4]
       with no-connection (disable) option
\# - a switchable tap tap from output of FF[2] to a XOR at input of FF[3]
       of from output of FF[4] to a XOR at input of FF[2]
       with no-connection (disable) option
config = ProgrammableLfsrConfiguration(8)
config.addGated(6,0)
\# >>> \{'6-0 \text{ off ': None, '}6-0 \text{ on ': } [6, 0]\}
config.addGated(5,0)
\# >>> \{ 5-0 \text{ off ': None, '5-0 on ': [5, 0]} \}
config. addSwitched (None, [4,3], [3,4])
\# >>> \{ \text{'None': None, '} 4-3': [4, 3], '3-4': [3, 4] \}
\verb|config.addS| witched| (\verb|None|, [2|, 3]|, [4|, 2]|)
\#>>> \{ \text{'None': None, '2-3': [2, 3], '4-2': [4, 2]} \}
plfsr = ProgrammableLfsr(config, OperateOnTapsOnly=True)
```

Consider also a way to create all-combinations switch:

- SourceList list of source FFs indexes
- DestinationList list of destination FFs indexes
- IncludeNone if True, then None will also be included in the resultant taps switch

```
 \begin{array}{l} config = ProgrammableLfsrConfiguration\,(8) \\ config.\,addAllCombinationsSwitch\,([1\,,2]\,,\ [4\,,5]) \\ \#>>> \{\,'1-4\,'\colon\,[1\,,\ 4]\,,\ `1-5\,'\colon\,[1\,,\ 5]\,,\ `2-4\,'\colon\,[2\,,\ 4]\,,\ `2-5\,'\colon\,[2\,,\ 5]\} \\ config.\,addAllCombinationsSwitch\,([1\,,2]\,,\ [4\,,5]\,,\ True) \\ \#>>> \{\,'None\,'\colon\,None\,,\ `1-4\,'\colon\,[1\,,\ 4]\,,\ `1-5\,'\colon\,[1\,,\ 5]\,,\ `2-4\,'\colon\,[2\,,\ 4]\,,\ `2-5\,'\colon\,[2\,,\ 5]\} \\ \end{array}
```

## Class Nlfsr

NLFSR (Non-Linear Feedback Shift Register) is very similar to LFSR (Linear Feedback Shift Register) with the only difference: feedback taps may be results of a non-linear function of register's flip-flops. Consider the example from Fig. 5.1. We can see there a 10-bit register having two taps: from FF[4] to a XOR at input of FF[5] and from (FF[7] AND FF[3]) to a XOR at input of FF[0]). This may be strictly implemented using Nlfsr object by:

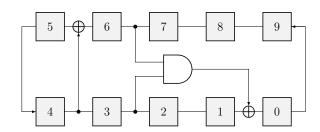


Figure 5.1: Example of Nonlinear Feedback Shift Register.

If is worth nothing, that tap description of Nlfsr is different than tap description of Lfsr. The difference is, that while each tap is still defined by a list, but the first item is not a source, but destination tap and the second item is a list of ANDed sources. So, each tap of Nlfsr looks like:

```
[ <destination_FF>, [<source_FF_1>, <source_FF_2>, ...] ].
```

As you can see, source values may only be ANDed. However, there is still a way to make a tap implementing other nonlinear function. All indexes given in tap list may also be negative numbers. If a source index is negative, then it considers NOT(source). If a destination index is negative, then it considers NAND instead of AND. See example taps description:

- [2, [-3,4]] AND(NOT(FF[3]), FF[4]) to a XOR at input of FF[2]
- [-2, [3,4]] NAND(FF[3], FF[4]) to a XOR at input of FF[2]
- [-2, [-3,-4]] NAND(NOT(FF[3]), NOT(FF[4])) = OR(FF[3], FF[4]) to a XOR at input of FF[2]

Keep in mind, that there is not any fast simulation method for NLFSRs. The only way to determine the period of NLFSR is simply simulate it step-by-step. To make it as fast as possible, he Research Shell implements a C++ based subroutine.

## 5.1 Nlfsr object methods

Not all Nlfsr object methods will be described. Nlfsr class bases on Lfsr class, so almost all methods are inherited from LFSR.

```
Nlfsr_object.__init__(Size, Config=[])
```

Object initializer.

- Size size (flip-flop count) of the NLFSR,
- Config list of taps definition (see page 27)

```
Nlfsr_object.__str__()
```

It returns a string containing binary value of the Nlfsr object (left MSb). See also Lfsr.\_\_str\_\_ on page 16

#### Nlfsr\_object.getArchitecture()

Returns a string containing human-readable description of taps.

```
MyNLFSR = Nlfsr(10, [[5, [4]], [0, [3,7]]])
print(MyNLFSR.getArchitecture())
# >>> 0 <= 3 AND 7
# >>> 5 <= 4
```

#### Nlfsr\_object.getFullInfo(Header=False)

Returns a string containing some information about NLFSR. Dependently on Header value, the first line is a header (see the example below). Next lines are human-readable description of taps. Last four lines are simplified equations - update functions - of the NLFSR. First update function - NLFSR as is; the second - complementary; third - reversed, and finally - reversed-complementary.

```
MyNLFSR = Nlfsr(10, [ [5, [4]], [0, [3,7]] ])

print(MyNLFSR.getFullInfo(True))

# >>> 10-bit NLFSRs and taps list and equations:

# >>> 0 <= 3 AND 7

# >>> 5 <= 4

# >>> 2, (4, 8)

# >>> C 2, 4, 8, (4, 8)

# >>> R 8, (6, 2)

# >>> CR 2, 6, 8, (6, 2)
```

#### Nlfsr\_object.next(steps=1)

See Lfsr.next on page 18.

#### Nlfsr\_object.printFullInfo()

Prints the full information (without header) about the NLFSR. Does the same as Aio.print(NlfsrObject.getFullInfo(Fa

```
MyNLFSR = Nlfsr(10, [ [5, [4]], [0, [3,7]] ])
MyNLFSR.printFullInfo()

# >>> 0 <= 3 AND 7

# >>> 5 <= 4

# >>> 2, (4, 8)

# >>> C 2, 4, 8, (4, 8)

# >>> R 8, (6, 2)

# >>> CR 2, 6, 8, (6, 2)
```

# Network and distributed computing

#### 6.1 UDP

Research Shell includes a few classes making UDP networking easier: UdpSender to send messages and UdpMonitor to receive them.

It is well known that UDP packets, dependent on MTU size, does not allow to transmit large amounts of data. However, UdpSender and UdpMonitor can automatically divide huge data into small fragments and that is realized i the background.

#### 6.1.1 UDP Monitor

This class is used to create monitor objects, which are working using a separate thread and may call a specified function if data arrives or may print the data to the screen. Below the object-related methods are listed:

UdpMonitor\_object.\_\_init\_\_(PortList, Callback=None, BufferSize=4096, ReturnString=False, BindToIp="")

UdpMonitor object initializer.

- PortList port or list of ports to listen,
- Callback function to call when new UDP message is received. If None then incoming messages will be printed to the screen,
- BufferSize size of socket buffer. If too small, then some messages may be lost,
- ReturnString messages are returned as bytes, but you may force to convert it into str by specifying this parameter True,
- BindToIp in case of many network interfaces you may bind the listener to a specified one by giving its IP.

```
# Simply look what is received on 1234 port:
UdpMonitor(1234).start()
# Receive and process incoming messages on 1235 and 1236 ports:
def Cbk(args):
   DATA = args[0]
   FROM_IP = args[1]
   FROM_PORT = args[2]
Monitor2 = UdpMonitor([1235, 1236], Callback=Cbk)
Monitor1.start()
```

```
UdpMonitor_object.start()
Starts UDP monitor.
```

```
Starts CD1 momtor.
```

<sup>#</sup> Simply look what is received on 1234 port:

```
UdpMonitor (1234). start ()
```

#### UdpMonitor\_object.stop()

Stops UDP monitor. It is worth nothing, that there is a risk than one message will be received even after UdpMonitor atopping!

```
# Simply look what is received on 1234 port during 10s:
Monitor = UdpMonitor(1234)
Monitor.start()
sleep(10)
Monitor.stop()
```

#### 6.1.2 UDP Sender

The UdpSender object is intended to make UDP messages sending easier. Its related methods:

```
UdpSender_object.__init__(Port=None, DestinationIp=None)
```

UdpMonitor object initializer.

- Port you may specify a default port if the UdpSender object is used to send data on known port,
- DestinationIp you may specify a default destination IP when this UdpSender object is used to send data to one destination

```
# Simply send dta to 192.168.0.1:80:
UdpSender(80, "293.268.0.2").send("Hi!")
# Periodically send broadcast messages on 81 port:
Sender = UdpSender(81)
while(1):
    Sender.send("Hi all!")
    sleep(1)
```

UdpSender\_object.send(Data, Ip=None, Port=None)

Send given data to a specified host.

- Data bytes or str data to send,
- Ip destination IP, If not specified, tries to use the default one, if still None then sends broadcast message,
- Port destination port. If not specified, uses the default one.

```
# Simply send dta to 192.168.0.1:80: UdpSender(80).send("Hi!", "293.268.0.2")
```

## 6.2 Distributed computing

The Research Shell is equipped with a utility to make distributed computing simple. The main goal is: I have some tasks to do. Is any other Research Shell ready to take one of them and execute?.

So, two classes are available: RemoteAioNode - a ready-to-work instance, and RemoteAioScheduler - a task scheduler.

Using the RemoteAIoScheduler one can request any number of tasks (by specifying a string containing a Research Shell code) and then the scheduler will try to find ready-to-work nodes, queuing, sending tasks and receiving responses - all in the background.

Let's say you requested a task. Here is what happens then:

1. The RemoteAloScheduler considered, its task queue is not empty. It sends a UDP broadcast message telling others, that there "Hi, I am <IP>:<Port> and I have some task to do".

- 2. Ready to work nodes respond, telling "Hi, I am <IP>:<Port> and I am ready to work".
- 3. The scheduler sends queuing tasks to those ready-to-work nodes and moves those task to the end of its task queue.

On the other hand, when a node finishes the requested task:

- 1. The node receives the result to the scheduler.
- 2. Once the scheduler receives the response, it removes the task from its task queue.

That simple mechanism makes the task scheduling independent of nodes failures, appearing and disappearing, and so on.

It is also possibility to specify the scheduler address when RemoteAioNode is initialized (or later) in case if the node cannot, for any reason, receive scheduler's broadcast messages.

Finally, it is worth nothing that th scheduler may (and it is enabled by default) use the local machine to perform scheduled tasks without any networking.

### 6.3 RemoteAioNode object

RemoteAioNode object creates a node, which is used to process requested tasks.

```
RemoteAioNode_object.__init__(Port=3099, CustomServers=[], Enable=True)
```

Object initializer.

- Port the port at which the node will listen for broadcast messages from schedulers in the LAN. If for any reason there is impossible to configure the node to work on the same port as schedulers, see the CustomServers parameter,
- CustomServers list of addresses of schedulers which the node should ping. The reason why to configure this parameters is i.e. if node works on another port than a scheduler, or if the node cannot receive broadcast messages from a scheduler because both are part of different subnets. The CustomServers may be a list of addresses, or may be a string containing single IP. In case of list, each address may be a string, containing IP, or a list, containing IP and port. In any case, if no port specified, then it assumes the same port as the one at which the node is listenning,
- Enable if *True* then the node automatically starts its background processes.

```
# Start a simple, standard node
RemoteAioNode()
# Create a simple node, but not start it automatically
Node = RemoteAioNode(Enable=False)
Node.start()
# Start a node and include a specified scheduler address:
RemoteAioNode(CustomServers="10.10.2.100")
# Start a node working at different port than the scheduler:
RemoteAioNode(Port=4000, CustomServers=[["10.10.2.100", 3099]])
```

#### RemoteAioNode\_object.addCustomServer(Ip, Port)

Add a custom server address to the node (see the node initializer).

```
RemoteAioNode_object.start()
```

Start the background process of the node.

```
RemoteAioNode_object.stop()
```

Stop the background process of the node.

### 6.4 RemoteAioScheduler object

RemoteAIoScheduler is the one object which takes tasks and tries to process them as fast as possible, using local machine (if allowed) and any available RemoteAioNode. It has a few methods making task scheduling easier - all are listed below.

RemoteAioScheduler\_object.\_\_init\_\_(Port=3099, Enable=True, LocalExecution=False)

RemoteAIoScheduler object initializer.

- Port the port at which the scheduler sends the broadcasts messages and listens for incoming packets,
- Enable if True then it automatically starts its background processes (otherwise it will not process requested tasks)
- LocalExecution whether to use the local machine to process tasks together with other available nodes or not. IT IS NOT RECOMMENDED enabling the local execution when you plan to schedule extensive jobs, especially using multi-threading. It is a high risk that the scheduler may get not enough resources to coordinate all jobs and network communication.

```
# Create a standard scheduler S = RemoteAioScheduler()
```

#### RemoteAioScheduler\_object.addTask(Code)

RemoteAloScheduler object initializer.

• Code - a string containing a code to be executed.

This method returns a RemoteAioTask object. Look at the example below to see how to use it in your code.

```
S = RemoteAioScheduler()
task = S.addTask("2 * 2")
while not task:
sleep(0.01)
result = task.Response
print(result)
# >>> 4
```

#### RemoteAioScheduler\_object.map(CodeList, ShowStatus=False)

This method is used to request for execution of many tasks. It returns an ordered list or results. See the example below:

- CodeList each item of this list is a string containing Python (Research Shell) code to executed,
- ShowStatus if True, then it will periodically (1s) visualize mapped tasks, where each task is a colorised: yellow = in progress, green = done.

```
S = RemoteAioScheduler()
codelist = [
   "2*2",
   "3*3",
   "4*4"
]
results = S.map(codelist)
print(results)
# >>> [4, 9, 16]
```

#### ${\tt RemoteAioScheduler\_object.mapGenerator(CodeList,\ ShowStatus=False)}$

This is not a method, but a generator. It yields ordered results as soon as possible. See the example below.

- CodeList each item of this list is a string containing Python (Research Shell) code to executed,
- ShowStatus if True, then it will periodically (1s) visualize mapped tasks, where each task is a colorised: yellow = in progress, green = done.

```
S = RemoteAioScheduler()
codelist = [
   "[2, 2*2]",
   "[3, 3*3]",
   "[4. 4*4]"
]
for result in S.mapGenerator(codelist):
   print(result)
# >>> [2, 4]
# >>> [3, 9]
# >>> [4, 16]
```

#### RemoteAioScheduler\_object.mapUnorderedGenerator(CodeList, ShowStatus=False)

This is not a method, but a generator. It yields UNORDERED results as soon as possible. See the example below.

- CodeList each item of this list is a string containing Python (Research Shell) code to executed,
- ShowStatus if True, then it will periodically (1s) visualize mapped tasks, where each task is a colorised: yellow = in progress, green = done.

```
S = RemoteAioScheduler()
codelist = [
    "[2, 2*2]",
    "[3, 3*3]",
    "[4. 4*4]"
]
for result in S.mapUnorderedGenerator(codelist):
    print(result)
# this is the example output. It may differ
# as the mapping is unordered:
# >>> [3, 9]
# >>> [2, 4]
# >>> [4, 16]
```

#### RemoteAioScheduler\_object.start()

Start the background process of the scheduler.

#### RemoteAioScheduler\_object.stop()

Stop the background process of the scheduler.

# Interactive menu

# Bibliography

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