## Problem 17-2

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- $x_i$  Decision variable for building a factory in location i
- $x'_i$  Decision variable for building a distribution center in location j
- $y_{i,j,l}^s$  Amount of product l that is sent to distribution center j from factory i in scenario s
- $z_{j,h,l}^s$  Amount of product l that is sent from distribution center j to customer h in scenario s
- $u_{h,l}^s$  Amount of unsatisfied demand of product l for customer h in scenario s

$$\begin{aligned} & \min & & \sum_{i \in I} c_i x_i + \sum_{j \in J} c_j' x_j' \\ & & \sum_{s \in S} p^s [ \\ & & \sum_{i \in I} \sum_{j \in J} f_{i,j} \sum_{l \in L} x_{i,j,l}^s + \\ & & \sum_{j \in J} \sum_{h \in H} f_{j,h}' \sum_{l \in L} z_{i,j,l}^s + \\ & & \sum_{l \in L} g_l \sum_{h \in H} u_{h,l}^s \end{aligned}$$

Factory Capacity Constraint

$$\sum_{j \in J} x_{i,j,l}^s \le r_{i,l} \quad \forall i \in I, \forall l \in L, \forall s \in S$$

Factory to Distribution Center Constraint

$$\sum_{l \in L} x_{i,j,l}^s \leq r_{i,j}' \quad \forall i \in I, \forall j \in J, \forall s \in S$$

Distribution Center to Customer Constraint

$$\sum_{l \in L} z_{j,h,l}^s \leq r_{j,h}'' \quad \forall h \in H, \forall j \in J, \forall s \in S$$

Unsatisfied Demand

$$\sum_{j \in J} z_{j,h,l}^s = d_{h,l}^s - u_{h,l}^s \quad \forall h \in H, \forall l \in L, \forall s \in S$$