

Assignment-6

Polynomial Regression Model:-

X	Y
7.6	157
7.1	174

Step 1: Read dataset $\eta = 0.0001$, epochs = 1, $m_1 = 1$, $m_2 = 1$, $c = -1$

Step 2: iter = 1

Step 3: sample $s = 1$

Step 4: $y_p = m_2(x_i)^2 + m_1x_i + c$

$$y_p = 1(7.6)^2 + 1(7.6) - 1 \\ = 64.36$$

Step 5: $E = \frac{1}{2}(y_i - y_p)^2$

$$= \frac{1}{2}(157 - 64.36)^2 = 4291.08$$

Step 6: $\frac{\partial E}{\partial m_1} = -[y_i - m_2x_i^2 - m_1x_i - c]x_i$

$$= -(157 - 64.36)(7.6)$$

$$= -704.06$$

$\frac{\partial E}{\partial m_2} = -[y_i - m_2x_i^2 - m_1x_i - c]x_i^2$

$$= -(157 - 64.36)(7.6)^2$$

$$= -5350.85$$

$\frac{\partial E}{\partial c} = -[y_i - m_2x_i^2 - m_1x_i - c]$

$$= -(157 - 64.36) = -92.64$$

$$\text{step 7: } \Delta m_1 = -\eta \frac{\partial E}{\partial m_1} = -(0.0001)(-704.06) \\ = 0.070406$$

$$\Delta m_2 = -\eta \frac{\partial E}{\partial m_2} = -(0.0001)(-5350.85) \\ = 0.535085$$

$$\Delta C = -\eta \frac{\partial E}{\partial C} = -(0.0001)(-92.64) \\ = 0.009264$$

$$\text{step 8: } m_1 = m_1 + \Delta m_1$$

$$= 1 + 0.070406 = 1.070406$$

$$m_2 = 1 + 0.535085 = 1.535085$$

$$C = -1 + 0.009264 = -0.9907$$

$$\text{step 9: } \text{sample} = \text{sample} + 1 = 2 \leq n_s$$

True

Step 4

$$\text{step 4: } y_p = m_2(x_i)^2 + m_1 x_i + C$$

$$= 1.5350(7.1)^2 + (1.0704)(7.1) + (-0.9907)$$

$$= 83.988$$

$$\text{step 5: } e = \frac{1}{2}(y_i - y_p)^2 = \frac{1}{2}(174 - 83.988)^2 = 4051.08$$

$$\text{step 6: } \frac{\partial E}{\partial m_1} = -(174 - 83.988)(7.1) = -639.0852$$

$$\frac{\partial E}{\partial m_2} = -(174 - 83.988)(7.1)^2 = -4537.504$$

$$\frac{\partial E}{\partial m_3} = -(174 - 83.988) = -90.012$$

$$\text{step 7: } \Delta m_1 = -\eta \frac{\partial E}{\partial m_1} = 0.0639$$

$$\Delta m_2 = -\eta \frac{\partial E}{\partial m_2} = 0.4537$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = 0.0009$$

$$\text{step 8: } m_1 = m_1 + \Delta m_1 = 1.0764 + 0.639$$

$$m_2 = 1.5350 + 0.4357 = 1.9887$$

$$c = -0.9907 + 0.0009 = -0.9898$$

$$\text{step 9: } \text{sample} = \text{sample} + 1 = 2 + 3$$

$$\text{sample} \leq n_s \quad \times \quad \boxed{\text{false}} \rightarrow \text{next step}$$

$$\text{step 10: } \text{iter} = \text{iter} + 1 = 1 + 1 = 2$$

$$\text{iter} > \text{epochs} \rightarrow \text{next step}$$

$$\text{step 11: } \boxed{\text{END}}$$