

Date : _____

19K41A05B0

Page No. : (1)

Artificial Intelligence (AI) - Assignment #07.

Outlook	Temperature	Humidity	Windy	Hours to play
Rainy	Hot	high	False	25
Rainy	Hot	high	True	30
Overcast	Hot	high	False	46
Sunny	mild	high	False	45
Sunny	cool	normal	False	52
Sunny	cool	normal	True	23
Overcast	cool	normal	True	43
Rainy	mild	high	False	35
Rainy	cool	normal	False	38
Sunny	mild	normal	False	46
Rainy	mild	normal	True	48
Overcast	mild	high	True	52
Overcast	hot	normal	False	49
Sunny	mild	high	True	30

Step 2 :- calculate, SD, CN, μ_{mean}

$$\mu_{mean} = \sum x / n$$

$$= \frac{25 + 30 + 46 + 45 + 52 + 23 + 43 + 35 + 38 + 46 + 48 + 52 + 44 + 30}{14}$$

$$= \frac{557}{14} = 39.78$$

$$SD = \sqrt{\frac{\sum (x - \mu_{mean})^2}{n}}$$

$$SD = 9.67$$

$$CN = \frac{SD}{\mu_{mean}} \times 100 = \frac{9.67}{39.78} \times 100 = 24.30$$

Step 3 :- dataset is split on different attributes the SD of each branch is calculated.

$SD(attr) = \sum w(branch) SD(branch)$ and result is standard deviation reduction

$$SDR = SD - SD(attr)$$

$$\therefore SD(Target) = 9.67$$

Outlook

	μ_{mean}	SD	CV	n	$w(V)$
Rainy	35.2	8.7	24.7	5	5/14
Overcast	46.25	4.03	8.42	4	4/14
Sunny	39.2	12.2	31.0	5	5/14

Date : _____

Page No. : (3)

$$SD(Outlook) = \frac{5}{14} (8.7) + \frac{4}{14} (4.03) + \frac{5}{14} (12.2)$$
$$= 8.59$$

$$SD.R(Outlook) = SD(Target) - (Outlook)SD = 9.67 - 8.59$$
$$= \underline{\underline{1.08}}$$

Temp:-

	mean	SD	CV	n	w(v)
hot	36.25	10.34	30.6	4	4/14
cool	39	12.14	31.1	4	4/14
mild	42.6	3.38	19.65	6	6/14

$$SD(Temp) = \frac{4}{14} (10.34) + \frac{4}{14} (12.14) + \frac{6}{14} (3.38) = \underline{\underline{10.01}}$$

$$SDR(Temp) = 9.67 - 10.01 = -0.34$$

Humidity:-

	mean	SD	CV	n	w(v)
high	37.51	10.11	26.92	7	7/14
normal	42	9.4	27.4	7	7/14

$$SD(humidity) = \frac{7}{14} \times 10.11 + \frac{7}{14} \times 9.14 = 9.77$$

$$SDR(humidity) = 9.67 - 9.77$$
$$= -0.1$$

windy :-

	mean	SD	CV	n	w(v)
True	37.6	11.6	30.8	6	6/14
False	41.3	8.41	20.3	8	8/14

$$SD(\text{windy}) = \frac{6}{14} \times 11.6 + \frac{8}{14} \times 8.41 = 9.77$$

$$SDR(\text{windy}) = 9.67 - 9.77 = -0.1$$

The value that has highest SDR is considered as root value node (ie decision node).

Considering termination Criteria.

CV is 10% or CV is (n ≤ 4)

Outlook

Outcast has CV of 8% which is less than threshold value therefore we need not to further split

Outlook

Outcast

Hours
played
46.25

we need to split into sunny and Runny

Outlook	Temp	humidity	windy	hours played
Sunny	mild	high	false	45
Sunny	cool	normal	false	52
Sunny	cool	normal	True	23
Sunny	mild	normal	false	46
Sunny	mild	high	True	30

$$\text{mean} = 39.2$$

$$SD = 12.2$$

$$CV = 31.0$$

Temp:-

	mean	SD	CV	n	w(v)
mild	40.3	8.76	22.23	3	3/5
cool	37.5	20.50	54.66	2	2/5

$$SD(\text{Temp}) = \frac{3}{5}(8.76) + \frac{2}{5}(20.50) = 13.576$$

$$= 12.2 - 13.576 = -1.37$$

Humid:-

	mean	SD	CV	n	w(v)
high	37.5	10.6	28.26	2	2/5
Normal	40.3	15.30	37.96	3	3/5

Date : _____

Page No. : (6)

$$SD(\text{humid}) = \frac{2}{5}(10.6) + \frac{3}{5}(15.3) + 64(10.6) + 0.6(15.3)$$

$$= 13.42$$

$$SD(\text{humid}) = 12.2 - 13.42 = -1.22$$

Windy :-

	mean	SD	CV	n	w(v)
False	47.66	3.78	7.94	3	3/5
True	26.5	4.94	18.65	2	2/5

$$SD(\text{windy}) = \frac{3}{5}(3.78) + \frac{2}{5}(4.94)$$

$$= 4.23$$

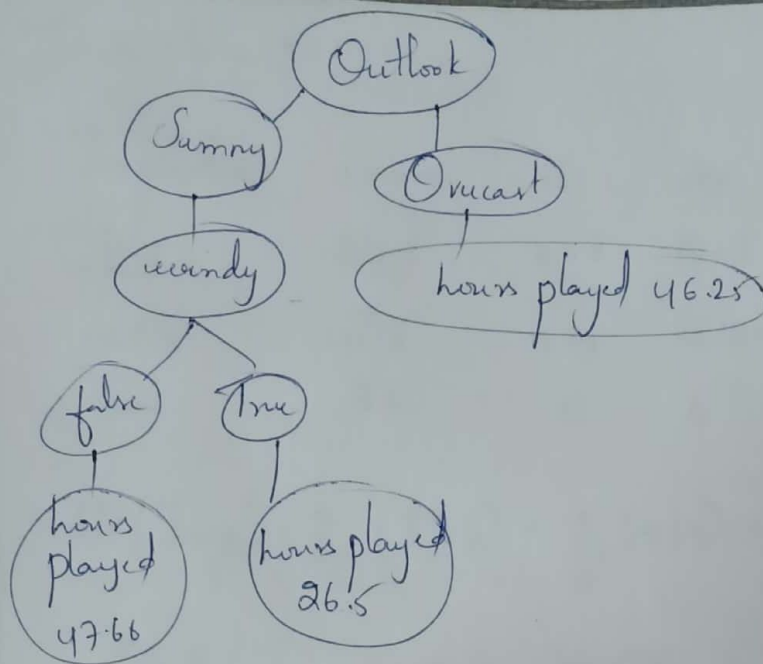
$$SD(\text{windy}) = 12.2 - 4.23 = 7.97$$

then check for highest SDR

In outlook, among Temp, humidity & windy
SDR value is high for windy.

$$SDR = 7.97$$

Then, check for CV value both true and false
satisfy CV value



Rainy :-

Outlook	Temperature	Humidity	Windy	Hours to Play
Rainy	hot	high	false	25
Rainy	hot	high	True	30
Rainy	mild	high	false	35
Rainy	cool	normal	false	38
Rainy	mild	normal	True	48

mean = 35.2

SD = 8.7

CV = 24.9

Date : _____

Page No. : (8)

Temperature :-

Temperature	mean	SD	CV	n	w(v)
hot	27.5	3.53	12.13	2	2/5
mild	41.5	9.19	22.144	2	2/5
cool	38	0	0	1	1/5

$$SD(Temp) = \frac{2}{5}(3.53) + \frac{2}{5}(9.19) + \frac{1}{5} \times 0 = 5.088$$

$$\begin{aligned} SDR(Temp) &= SD - SD(Temp) \\ &= 8.7 - 5.088 \\ &= 3.612 \end{aligned}$$

Humidity :-

Humidity	mean	SD	CV	n	w(v)
high	30	5	16.66	3	3/5
normal	43	7.07	16.44	2	2/5

$$\begin{aligned} SD(humidity) &= \frac{3}{5}(5) + \frac{2}{5}(7.07) \\ &= 5.828 \end{aligned}$$

$$\begin{aligned} SDR(humidity) &= SD - SD(humidity) \\ &= 8.7 - 5.828 \\ &= 2.872 \end{aligned}$$

Date : _____

Page No. : (9)

windy %

windy	mean	SD	CV	n	w(v)
False	32.66	6.80	20.85	3	3/5
True	39	12.72	32.5	2	2/5

$$SD(windy) = \frac{3}{5} (6.80) + \frac{2}{5} (12.72)$$

$$= 9.168$$

$$SDR(windy) = SD - SD(windy)$$

$$= 8.7 - 9.168$$

$$= -0.468$$

Among Temp, humidity and windy the SDR value is high for Temperature (ie 3.612)

Then, check for CV value for hot, mild and cool satisfy CV value.

