RICE
JONES GRADUATE SCHOOL OF BUSINESS

Hypothesis Testing *Difference in means test*

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Claim to be tested…

Difference between the population mean height of Men and Women Olympic athletes is 12.5 cm

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a thought exercise

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- **Subjective judgement**

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