

MATRIX: LINE ASSIGNMENT

0.1 Problem:

Construct a triangle XYZ in which $\angle Y = 30^\circ$, $\angle Z = 90^\circ$ and $XY + YZ + ZX = 11\text{cm}$.

0.2 Solution:

Input Parameters:

Symbol	Value	Description
$XY + YZ + ZX$	11cm	Sum of Distances
$\angle Z$	90°	Angle at Z
$\angle Y$	30°	Angle at Y

Termux Command:

`bash rncm.sh (Using Shell)`

To Prove:

Given, $\angle Y = 30^\circ$, $\angle Z = 90^\circ$ and $XY + YZ + ZX = 11\text{cm}$.

if $\angle Y = 30^\circ$ and $\angle Z = 90^\circ$ then $\angle X = 60^\circ$

Let us consider the coordinates of Y are X_0, Y_0 be $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$

Let 'r' be the distance between X and Y.

Let the coordinates of X be X_1, Y_1 respectively.

$$\text{i.e., } X = r \begin{pmatrix} \cos\theta \\ \sin\theta \end{pmatrix}$$

And the coordinates of Z be X_2, Y_2 respectively.

$$\text{i.e., } Z = r \begin{pmatrix} \cos\theta \\ 0 \end{pmatrix}$$

So, by finding the values of coordinates of the all sides we can form a required triangle.

Finding the Coordinates:

Given that $XY + YZ + ZX = 11$.

i.e., $\|X - Y\| + \|Y - Z\| + \|Z - X\| = 11$.

$$\Rightarrow r + r\cos\theta + r\sin\theta = 11.$$

By solving we get 'r', $[\because \theta = 30^\circ]$.

$$\therefore r = 4.64.$$

Calculating the required vertices:

$$X = r \begin{pmatrix} \cos\theta \\ \sin\theta \end{pmatrix} = 4.64 \begin{pmatrix} \cos 30^\circ \\ \sin 30^\circ \end{pmatrix} = \begin{pmatrix} 4.02 \\ 2.32 \end{pmatrix}$$

$$Z = r \begin{pmatrix} \cos\theta \\ 0 \end{pmatrix} = 4.64 \begin{pmatrix} \cos 30^\circ \\ 0 \end{pmatrix} = \begin{pmatrix} 4.02 \\ 0 \end{pmatrix}$$

\therefore The vertices of the required $\triangle XYZ$ are:

$$X = \begin{pmatrix} 4.02 \\ 2.32 \end{pmatrix}, Y = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, Z = \begin{pmatrix} 4.02 \\ 0 \end{pmatrix}$$

The below python code realizes construction:

<https://github.com/19pa1a04e9/FWC-IITH/tree/main/Assignment-1/MATRICES/Line/line.py>

0.3 Plot:

