

MATRIX: LINE ASSIGNMENT

0.1 Problem:

Construct a triangle XYZ in which $\angle Y = 30^\circ$, $\angle Z = 90^\circ$ and $XY + YZ + ZX = 11\text{cm}$.

0.2 Solution:

Input Parameters:

| Symbol | Value | Description |
|----------------|------------|-------------|
| $XY + YZ + ZX$ | 11cm | D |
| $\angle Z$ | 90° | Angle at Z |
| $\angle Y$ | 30° | Angle at Y |

Termux Command:

bash rncom.sh (Using Shell)

To Prove:

Given, $\angle Y = 30^\circ$, $\angle Z = 90^\circ$ and $XY + YZ + ZX = D\text{cm}$.

if $\angle Y = 30^\circ$ and $\angle Z = 90^\circ$ then $\angle X = 60^\circ$

Let us consider the coordinates of Y are X_0, Y_0 be $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$

Let 'z' be the distance between X and Y.

Let the coordinates of X be X_1, Y_1 respectively.

$$\text{i.e., } X = z \begin{pmatrix} \cos\theta \\ \sin\theta \end{pmatrix}$$

And the coordinates of Z be X_2, Y_2 respectively.

$$\text{i.e., } Z = z \begin{pmatrix} \cos\theta \\ 0 \end{pmatrix}$$

So, by finding the values of coordinates of the all sides we can form a required triangle.

Finding the Coordinates:

Given that $XY + YZ + ZX = D$.

i.e., $\|X - Y\| + \|Y - Z\| + \|Z - X\| = D$.

$$\Rightarrow z + z\cos\theta + z\sin\theta = D$$

$$\Rightarrow z = \frac{D}{1 + \cos\theta + \sin\theta}$$

By solving we get 'z', $[\because \theta = 30^\circ \text{ and } D = 11\text{cm}]$.

$$\therefore z = 4.64$$

Calculating the required vertices:

$$X = z \begin{pmatrix} \cos\theta \\ \sin\theta \end{pmatrix} = 4.64 \begin{pmatrix} \cos 30^\circ \\ \sin 30^\circ \end{pmatrix} = \begin{pmatrix} 4.02 \\ 2.32 \end{pmatrix}$$

$$Z = z \begin{pmatrix} \cos\theta \\ 0 \end{pmatrix} = 4.64 \begin{pmatrix} \cos 30^\circ \\ 0 \end{pmatrix} = \begin{pmatrix} 4.02 \\ 0 \end{pmatrix}$$

\therefore The vertices of the required $\triangle XYZ$ are:

$$X = \begin{pmatrix} 4.02 \\ 2.32 \end{pmatrix}, Y = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, Z = \begin{pmatrix} 4.02 \\ 0 \end{pmatrix}$$

The below python code realizes construction:

<https://github.com/19pa1a04e9/FWC-IITH/tree/main/Assignment-1/MATRICES/Line/line.py>

0.3 Plot:

