Analysis of Optimizers to Regulate Occupant's Actions for Building Energy Management

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Abstract—Occupants and their actions play major roles in building energy management as reported by previous studies, which involves finding the optimal schedule of user actions, under a given physical context, in order to minimize their dissatisfaction. However, comparison and performance analysis of various optimizers, for the concerned problem, have not been studied previously, which is essential to gain insight into the underlying characteristics of the problem. In this work, the performance of four popular and contemporary multi-objective optimization algorithms viz. DEMO, NSGA-II, NSGA-III, and θ -DEA, for estimating the optimal schedule has been analyzed in terms of their abilities to find minimal average indoor conditions, to discover more number of alternative trade-off solutions (flexibility) and to promptly converge to a smaller minimal net dissatisfaction value (speed of convergence). Results show that NSGA-II has slightly better capabilities than NSGA-III and θ -DEA, but it clearly outperforms DEMO. The recently developed population dynamics indicators are also applied to support the observed features of the optimizers. The proposed analyzing paradigm can also be used when the optimization problem is extended to include several other objectives.

I. INTRODUCTION

Energy management in buildings is an essential concern as a majority (as much as 40%) of the global energy is consumed by buildings [1]–[3]. The primary goal of this energy management is to improve the comfort of occupants without increasing the energy consumption. On one hand, the depletion in natural resource bank at an alarming rate and, on the other hand, the ever-growing demand of the inhabitants, is at the cross-roads which is demanding the research community for developing intelligent energy regulation strategies. Recently, it came to light that there is a considerable impact of actions of occupants on the building energy management [2], [3]. Thus, it is imperative to analyze and propose actions, given a physical context, such that dissatisfaction of the occupants could be minimized without increasing the energy input.

Building energy management has been studied over two decades. However, the contemporary researches focuses on the following aspects. Studies [3], [4] show that the inhabitants can reduce their thermal and/or air quality dissatisfaction

(using Differential Evolution for Multi-objective Optimization (DEMO)) by following a proposed optimal schedule of actions (opening and closing of doors and windows). However, besides regulating user actions, other energy managing devices like HVAC (Heating, Ventilation and Air Conditioning) system is needed to reduce dissatisfaction when the outdoor temperature is much higher than the preferred range of temperature [4]. The impact of occupant's actions is studied by relating the degree of changes between actions (cause) and comfort (effect) [3] which helps the occupants to prioritize the necessary changes in their schedule. Analysis of energy consumption during both occupied and non-occupied hours shows that changes in occupant's actions can help in limiting this excess energy consumption [2]. Variation in the amount of coordination between energy managing devices and occupants can address multiple levels of comfort ranges and occupancies [1]. While some studies [1], [2] consider both devices and occupants as energy controlling agents, others [3], [4] concentrate only on the role of occupants in energy management system.

In this work, the experimental database from [3], [4] has been re-used to provide the physical context. For the first time in this application, the optimization performance of DEMO is compared with other popular and/or contemporary multiobjective optimization algorithms viz. Non-dominated Sorting Genetic Algorithm or NSGA-II [5], NSGA-III [6] and θ -Dominance based Evolutionary Algorithm or θ -DEA [7]. The comparison is made in terms of the ability of the algorithms to minimize the indoor temperature and CO₂ concentration, flexibility of the algorithms to find higher number of tradeoff solutions such that the users have more alternatives and the speed of convergence. Moreover, the recently developed population dynamics indicators [8] are also applied to summarize the population movement such that the features of the underlying landscape of the problem and the ability of the optimizers to deal with these features could be analyzed.

In the rest of the paper, the experimental details are outlined in Section II, the essential observations are noted in Section III, and the paper is concluded in Section IV with future directions.

II. EXPERIMENTAL PARADIGM

This energy management problem aims to propose schedules of actions to the building occupants in order to minimize their dissatisfaction. The dissatisfaction depends on the variations in occupant's actions (like opening/closing of doors/windows) and on environmental factors (like outside temperature, outside CO₂ concentration, wind speed, solar radiation, etc.). The experiment involves simulating indoor conditions (like indoor temperature, indoor CO₂ concentration, etc.) based on random actions and recorded environmental factors, and searching for the actions that can lead to more comfortable indoor conditions when similar environmental factors appear. A physical model of the building [3] is used for this simulation purpose. This entire experimental framework is shown in Fig. 1.

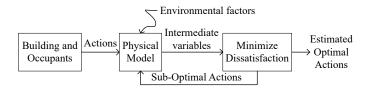


Fig. 1. Experimental Framework

A. Details of Testbed

The experimental database from [3], [4] is utilized where data is acquired from a research office at Grenoble Institute of Technology, France, which is fitted with 27 sensors and where four researchers work. In the experimental setup, HVAC system is not present. Some of the sensors measure temperature, wind speed, solar illuminance, CO₂ concentration, moisture, etc. while the other sensors detect motions, measure acoustic pressure, power consumption, etc. to estimate the number of occupants [9], [10]. Data acquisition is performed during working hours (8 am to 8 pm), for a period of 100 days from 1st April 2015 to 9th July 2015. For performance analysis, the entire period is divided into 10 groups (Group 1 to Group 10), each of 10 days, as done in [4]. This database has a two-fold purpose:

- To assist in tuning of the physical model to match simulated indoor conditions with recorded indoor conditions by rerunning recorded actions from the database
- To generate indoor conditions, corresponding to hypothetical schedules of actions, in order to quantify the dissatisfaction of the occupant, during optimization

B. Optimization Problem Formulation

The mathematical formulation of the underlying optimization problem [3], [4] is given by Eq. (1) where A represents the set of actions, D_{th}^k and D_{air}^k represents the average thermal and air quality dissatisfaction at the k-th hour, respectively.

$$\mbox{Minimize: } D(A) = \left\lceil \frac{\sum_{k=1}^{12} D_{th}^k(A)}{12}, \frac{\sum_{k=1}^{12} D_{air}^k(A)}{12} \right\rceil \ \ \, (1)$$

1) Representation of Candidate Solution: In absence of HVAC system, the only controllable parameters that can influence the indoor conditions are the actions (opening/closing of doors/windows) of the occupants. Thus, the solution vector of the optimization problem is encoded as a 24-dimensional binary vector as shown in Fig. 2, where its elements are the status of door/window at every hour (from 8 am to 8 pm).

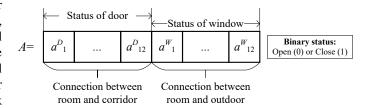


Fig. 2. Candidate Solution of the Optimization Problem

2) Optimization Objectives: The algorithm searches for optimal actions such that thermal dissatisfaction (Eq. (2)) and CO_2 based air quality dissatisfaction (Eq. (3)) are minimized. These criteria are dependent on indoor temperature (T_{in}^k in ${}^{\circ}C$) and indoor CO_2 concentration (C_{in}^k in ppm) at the k-th hour which are, in turn, dependent on the schedule of occupant's actions (A).

$$D_{th}^{k}(T_{in}^{k}) = \begin{cases} \frac{21 - T_{in}^{k}}{21 - 18} & \text{, if } T_{in}^{k} < 21\\ 0 & \text{, if } 21 \le T_{in}^{k} \le 23\\ \frac{T_{in}^{k} - 23}{26 - 23} & \text{, if } T_{in}^{k} > 23 \end{cases}$$
 (2)

$$D_{air}^{k}(C_{in}^{k}) = \begin{cases} 0 & \text{, if } C_{in}^{k} \le 400\\ \frac{C_{in}^{k} - 400}{1500 - 400} & \text{, if } C_{in}^{k} > 400 \end{cases}$$
(3)

When outdoor temperature is moderately high, opening windows can lead to increase in T_{in} and C_{in} , thereby improving D_{th} while deteriorating D_{air} . Such situations lead to the conflicting nature of the objectives and thus, presents a multi-objective optimization (MOO) problem.

3) Stopping Criteria: For this work, Pareto-optimality [3] is the scenario where thermal dissatisfaction cannot be decreased unless air quality based dissatisfaction is increased or viceversa. Assuming solutions have converged to this Pareto-optimal state, the optimization procedure is terminated after 300 iterations i.e. $I^{max} = 300$.

C. Significant Pareto-optimal Solutions

The optimization algorithm results in a Pareto-optimal set (solution set/schedules of actions in decision space) and the Pareto-front (objectives/dissatisfaction corresponding to the Pareto-optimal set). The occupants, based on their preference, is allowed to choose one of the solutions as their preferred optimal schedule of actions. In this work, further investigation is performed on three schedules corresponding to the following points of the Pareto-front (PF):

- Minimal average D_{th} : At the boundary of PF
- Minimal average D_{air} : At the boundary of PF
- Equally best compromise: Point having minimum net dissatisfaction $(D^*: min(D_{th} + D_{air}))$ value

III. RESULTS AND DISCUSSIONS

The proposed approach has been implemented in a Computer with 8GB RAM having an Intel Core i7 processor @ 2.20GHz running Python 3.4. Four state-of-the-art MOO algorithms viz. DEMO [3], [4], [11], NSGA-II [5], NSGA-III [6] and θ -DEA [7], have been used for the experiment and the results obtained are compared with each other to report the best optimization algorithm under a given preference. For each of the algorithms, the median values of the results are noted as obtained over the 50 executions where each execution consists of 300 iterations of the optimization algorithm. All the parameters of DEMO have been set as specified in [3], [4]. Since the candidate solution is a binary sequence, single point crossover and binary mutation have been used for NSGA-II, NSGA-III and θ -DEA. The crossover point is chosen randomly at every iteration and the mutation probability is set at a value of 1/24 i.e. the inverse of the length of a candidate solution.

A. Recommended Optimizers for Optimal Comfort

Different MOO algorithms result in different PF and thus, different alternatives are presented to the occupant according to the MOO algorithm used. From a chosen schedule, the physical model is used to simulate the indoor conditions. It should be noted that due to the inertia present in the physical variables, T_{in}^k and C_{in}^k are not only dependent on the actions at the k-th hour [3] but also on the initial indoor conditions and all the actions up to the k-th hour. Thus, the plots of average T_{in} (and C_{in}) per hour against time resulting from a schedule are crucial for decision making. Examples of such plots are shown in Fig. 3 for an experimental day (April 20, 2015) where the main difference appears towards the last two hours (6-8pm). The minimum average area under the step curve which indicates the average temperature or CO₂ concentration for the entire day is considered as an indicator of the best optimizer. Based on this indicator, the best optimizer is noted in Table I. Due to lack of space, results corresponding to only one day from each of the 10 groups are mentioned in this paper.

TABLE I RECOMMENDED OPTIMIZERS BASED ON AVERAGE TEMPERATURE AND AVERAGE ${\rm CO}_2$ Concentration

	Average Tempera	ture (in °C)	Average CO ₂ concentration (in ppm)		
Group	@ Minimal D_{th}	@ Occupant's	@ Minimal Dair	@ Occupant's	
(Date)	(Best optimizer)	Usual	(Best optimizer)	Usual	
1	20.9862	21.3120	601.0635	791.0627	
(April 08)	(DEMO)		(NSGA-II/NSGA-III)		
2	21.4320	21.6176	599.9790	1062.6929	
(April 20)	(θ-DEA)		(NSGA-II)		
3	22.6554 (NSGA-II/	24.1531	573.5144 (NSGA-II/	887.2458	
(April 27)	NSGA-III/θ-DEA)		NSGA-III/θ-DEA)		
4	23.358	23.9480	542.0127	807.3179	
(May 05)	(NSGA-III/θ-DEA)		(NSGA-II/NSGA-III)		
5	21.6399	23.2467	573.8091	816.6128	
(May 20)	(DEMO)		(DEMO)		
6	22.0747	22.5711	474.4113 (NSGA-II/	605.4587	
(May 28)	(NSGA-II/NSGA-III)		NSGA-III/θ-DEA)		
7	27.054	27.4792	440.6978	498.9001	
(June 05)	(NSGA-III)		(NSGA-II/NSGA-III)		
8	24.9376	25.6832	453.6374	439.0857	
(June 19)	(θ-DEA)		(NSGA-II)		
9	25.1341	25.7144	447.6200	441.4343	
(June 23)	(NSGA-III)		(NSGA-III)		
10	29.2638	29.4705	507.2125	459.1590	
(July 01)	(NSGA-II/NSGA-III)		(NSGA-III)		

It is observed from Table I that the minimum average indoor temperature has been attained by NSGA-III (in 6 out of 10 cases) whereas minimum average CO₂ concentration is attained by NSGA-II (in 7 out of 10 cases). Thus, when the occupants are interested solely in minimizing either D_{th} or D_{air} , correspondingly NSGA-III or NSGA-II is the optimizer of choice. The superior performance for NSGA-II can be accounted to the use of crowding distance based ranking strategy which has a tendency to discover boundary points of the Pareto-front [12]. On the other hand, NSGA-III has no such intrinsic tendency. The extent of exploration of the objective space depends on the distribution of the reference lines which partition the objective space into multiple neighborhoods along which the optimization occurs. Better performance of NSGA-III can be accounted to a good distribution of the reference lines which is simple to set for this experiment as the objective space is two-dimensional. For the concerned application, the number of reference lines has been considered to be equal to the number of candidates in a population.

B. Optimizer Discovering Majority of Pareto-front

As mentioned before, the MOO algorithms result in a set of trade-off solutions and occupants are allowed to choose the schedule as per their preference. Thus, it is very important that the resultant Pareto-front is densely sampled. After combining the non-dominated solution set from the four MOO algorithms and filtering out the dominated solutions, a non-dominated solution set is obtained whose constituent solutions are the result of one of the MOO algorithms. The proportion of this solution set discovered by a particular MOO algorithm indicates its ability towards providing more options for the occupants. This resulting fractions are mentioned in Table II for one of the experimental days in each of the group.

OVERALL FRACTION OF NON-DOMINATED SOLUTIONS DISCOVERED BY MOO ALGORITHMS (BEST VALUE IN BOLDFACE)

Group	Date	DEMO	NSGA-II	NSGA-III	θ-DEA
1	April 08	0.1304	0.2899	0.2899	0.2899
2	April 20	0.0000	0.3333	0.3333	0.3333
3	April 27	0.0000	0.3333	0.3333	0.3333
4	May 05	0.0000	0.3333	0.3333	0.3333
5	May 20	0.2500	0.2500	0.2500	0.2500
6	May 28	0.0000	0.3390	0.3390	0.3220
7	June 05	0.0000	0.3774	0.3585	0.2642
8	June 19	0.2500	0.2500	0.2500	0.2500
9	June 23	0.2500	0.2500	0.2500	0.2500
10	July 01	0.2597	0.2208	0.2597	0.2597
Mean 0.1		0.1140	0.2977	0.2997	0.2886
Standard Deviation		0.1256	0.0523	0.0441	0.0380

It is observed from Table II that NSGA-II and NSGA-III have equal abilities to discover the solutions in the Pareto-front. The performance of θ -DEA in this regard is also comparable. Moreover, the variation in the performance in terms of these fractions is very small for NSGA-II, NSGA-III and θ -DEA which indicates steady performance. However, DEMO lies far behind the other MOO algorithms in its capability to discover much of the Pareto-front. This is because of the fact

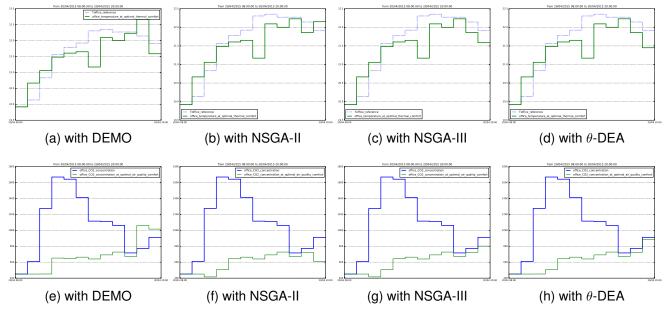


Fig. 3. Variation of (a-d) Indoor Temperature (T_{in}^k) and (e-h) Indoor CO_2 concentration (C_{in}^k) against Time for Occupant's Usual Schedule (blue) as compared with Best Schedules (green) Corresponding to Minimal Thermal (D_{th}) and Air Quality (D_{air}) Dissatisfaction

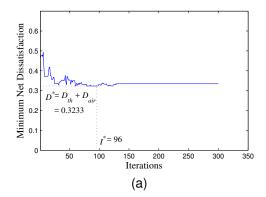
that DEMO performs ranking based on net dissatisfaction [3], [4] which is strictly a convergence based ranking and hence, fails at preserving the diversity of solutions in the final solution set. On the other hand, NSGA-II [5], NSGA-III [6] and θ -DEA [7] have their inherent diversity preserving mechanisms.

C. Speed of Convergence and the Minimal Net Dissatisfaction

Considering equal preference among both the objectives, net dissatisfaction is just the sum of thermal and air quality dissatisfaction. In presence of multiple non-dominated solutions resulting from a MOO algorithm, the schedule corresponding minimum net dissatisfaction (D^{\star}) is presented to the occupant as the equally best compromise among the objectives. A MOO algorithm which swiftly achieves the lowest value of D^{\star} is preferred.

Let I^{\star} be the iteration by which D^{\star} is reached and after which subsequent change in D^{\star} over next 10 iterations is less than 10^{-5} (implying D^{\star} is practically constant). The concept of I^{\star} and D^{\star} is demonstrated in Fig. 4 for an experimental day (April 08, 2015) from the results of DEMO. The ratio of I^{\star} to the allowed maximum number of iterations (I^{max}) indicates the speed of convergence of a MOO algorithm. This ratio ($I^{\star}:I^{max}$) along with the corresponding value D^{\star} is mentioned in Table III for one of the experimental days in each of the 10 groups.

It can be observed from Table III that the genetic algorithms (NSGA-II, NSGA-III) in general attain a better value of minimal net dissatisfaction as compared to differential evolution (DEMO). This can be attributed to the fact that the candidate solution is a binary sequence and NSGA-II, NSGA-III, and θ -DEA use binary crossover and binary mutation operations, whereas, DEMO is inherently designed for continuous func-



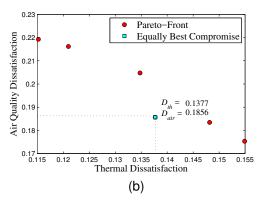


Fig. 4. Illustration of Parameters for Speed of Convergence and Minimal Net Dissatisfaction

tion optimization [11] and hence, does not act suited for this problem even after small modifications done in [3], [4].

NSGA-II is computationally faster per iteration as compared

TABLE III
SPEED OF CONVERGENCE TO THE MINIMAL NET DISSATISFACTION BY
MOO ALGORITHMS (BEST VALUE IN BOLDFACE)

Speed of Convergence $(I^*: I^{max})$							
Group	Date	DEMO	NSGA-II	NSGA-III	θ-DEA		
1	April 08	0.3200	0.0533	0.1267	0.0900		
2	April 20	0.1333	0.1033	0.1267	0.0800		
3	April 27	0.8367	0.1300	0.1167	0.1000		
4	May 05	0.3167	0.1333	0.0867	0.0867		
5	May 20	0.1467	0.0700	0.0700	0.0733		
6	May 28	0.1667	0.0867	0.1433	0.1333		
7	June 05	0.4967	0.1033	0.0967	0.0467		
8	June 19	0.0800	0.0800	0.0533	0.0867		
9	June 23	0.0900	0.3967	0.5833	0.5267		
10	July 01	0.2733	0.1000	0.1400	0.1000		
N	Mean		0.1257	0.1543	0.1323		
Standard Deviation		0.2328	0.0984	0.1537	0.1403		
	Mini	mal Net D	issatisfaction	` /			
Group	Date	DEMO	NSGA-II	NSGA-III	θ-DEA		
1	April 08	0.3233	0.3233	0.3233	0.3233		
2	April 20	0.2544	0.2254	0.2254	0.2254		
3	April 27	0.2632	0.2627	0.2638	0.2632		
4	May 05	0.3357	0.3114	0.3084	0.3084		
5	May 20	0.1242	0.0813	0.0813	0.0813		
6	May 28	0.1266	0.1221	0.1221	0.1221		
7	June 05	1.6968	1.6555	1.6555	1.6557		
8	June 19	0.6034	0.6034	0.6034	0.6034		
9	June 23	0.6680	0.6680	0.6680	0.6680		
10	July 01	2.1938	2.1938	2.1956	2.1972		
Mean		0.6589	0.6447	0.6447	0.6448		
Standard Deviation		0.7105	0.7111	0.7116	0.7120		

to NSGA-III and θ -DEA although their orders are same. This can be accredited to the use of adaptive normalization which is additionally employed by NSGA-III and θ -DEA. It must be understood that speed of an algorithm per iteration and convergence speed are different. In this regard, the performance of NSGA-II, NSGA-III and θ -DEA are practically same although the performance of NSGA-II based on the mean values of speed of convergence and minimal net dissatisfaction is slightly superior to the others.

D. Summary of Population Movement

Several indicators are introduced in [8] which summarizes the population movement as a collection of plots. These indicators are inspired from radial plot visualisation method [13]. The indicators used for this work are plotted in Fig. 5 for three days in different groups and are summarized as follows:

- 1) Convergence: It is the fraction of reference lines which has shown improvements [8]. DEMO has a spiky plot (Fig. 5a, 5e, 5i) which indicates lack of convergence uniformly across the distributed set of reference lines. On the other hand, NSGA-II, NSGA-III and θ -DEA has promptly converged to its approximate PF.
- Diversity: It is the average degree of deviation of the spread of candidates across the reference lines from an ideal uniform spread of candidates [8]. DEMO has poor divergence than NSGA-II, NSGA-III and θ-DEA (Fig. 5b, 5f, 5j).

- 3) Innermost Radius: It is minimum radius (distance from origin) of a candidate across all reference lines, indicating convergence. Better convergence of NSGA-II, NSGA-III and θ -DEA than DEMO is supported by Fig. 5c, 5g, 5k. It can also be noted that during summer (Group 10, July 01, Fig. 5k), the achieved optima is much higher than other cases.
- 4) Inner Band: It is the difference between maximum and minimum inner radius, each defined over all the reference lines. Unlike the others, DEMO has convergence based ranking which helps it to achieve a close to zero inner band (Fig. 5d, 5h, 5l) indicating that all solutions have reached the same radius. NSGA-II, NSGA-III and θ-DEA have higher inner bands showing that these algorithms have higher tendencies to harbor outliers.

IV. CONCLUSION AND FUTURE SCOPE

The main objective of this work is to study and report the most suited contemporary multi-objective optimization algorithms (DEMO, NSGA-II, NSGA-III and θ -DEA) for determining the Pareto-optimal set of schedules for opening and closing of doors and windows such that a compromise between minimal thermal and CO_2 based air quality dissatisfaction is attained.

Performance analysis is performed to determine the ability of the algorithms to attain minima along each objective, the ability of the algorithm to generate more alternatives for the end-user and the convergence speed of the algorithms. The results show that NSGA-II has superior tendency to outperform the other algorithms, however, the performance of NSGA-III and θ -DEA does not lie far behind. In most of the cases, DEMO has not resulted in solutions which are as good as the solutions generated by the other algorithms. Specific characteristics of each of the algorithms responsible for the performance have been highlighted.

The experiment dealing with thermal and air quality dissatisfaction is a preliminary step towards a bigger goal where other criteria like humidity based air quality dissatisfaction, total energy usage, cost of consumption due to variable tariff, and many more come in to picture. Hence, the bi-objective problem will turn into a many-objective optimization problem. The performance of the popular multi-objective optimization algorithms have to be re-evaluated in a similar way as proposed in this work, in order to determine the best one suited for the application. It should also be mentioned that the preference of an occupant towards each criteria and the preference of multiple occupants are essential while choosing an alternative schedule from the proposed set of solutions. Integrating such preferences into the framework are the other open areas of research for efficient building energy management.

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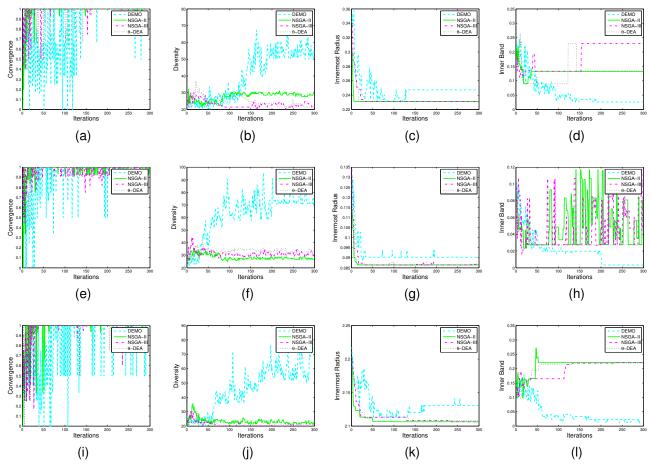


Fig. 5. Comparison of Population Movement across Iterations Representing Optimization based on Data Collected on Different Days: (a-d) Group 1 - April 08, (e-h) Group 6 - May 28, (i-l) Group 10 - July 01

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